AS

# Mathematics 

7356/2 - Paper 2
Mark scheme

June 2018

Version/Stage: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

## Mark scheme instructions to examiners

## General

The mark scheme for each question shows:

- the marks available for each part of the question
- the total marks available for the question
- marking instructions that indicate when marks should be awarded or withheld including the principle on which each mark is awarded. Information is included to help the examiner make his or her judgement and to delineate what is creditworthy from that not worthy of credit
- a typical solution. This response is one we expect to see frequently. However credit must be given on the basis of the marking instructions.

If a student uses a method which is not explicitly covered by the marking instructions the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

## Key to mark types

| $M$ | mark is for method |
| :--- | :--- |
| $R$ | mark is for reasoning |
| A | mark is dependent on M marks and is for accuracy |
| B | mark is independent of M marks and is for method and accuracy |
| E | mark is for explanation |
| F | follow through from previous incorrect result |

## Key to mark scheme abbreviations

| CAO | correct answer only |
| :--- | :--- |
| CSO | correct solution only |
| ft | follow through from previous incorrect result |
| 'their' | Indicates that credit can be given from previous incorrect result |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| sf | significant figure(s) |
| dp | decimal place(s) |

## AS/A-level Maths/Further Maths assessment objectives

| AO |  | Description |
| :--- | :--- | :--- |
| AO1 | AO1.1a | Select routine procedures |
|  | AO1.1b | Correctly carry out routine procedures |
|  | AO1.2 | Accurately recall facts, terminology and definitions |
|  | AO2.1 | Construct rigorous mathematical arguments (including proofs) |
|  | AO2.2a | Make deductions |
|  | AO2.2b | Make inferences |
|  | AO2.3 | Assess the validity of mathematical arguments |
|  | AO2.4 | Explain their reasoning |
|  | AO2.5 | Use mathematical language and notation correctly |
| AO3.1a | Translate problems in mathematical contexts into mathematical processes |  |
|  | AO3.1b | Translate problems in non-mathematical contexts into mathematical processes |
|  | AO3.2a | Interpret solutions to problems in their original context |
|  | AO3.2b | Where appropriate, evaluate the accuracy and limitations of solutions to problems |
|  | AO3.3 | Translate situations in context into mathematical models |
|  | AO3.4 | Use mathematical models |
|  | AO3.5a | Evaluate the outcomes of modelling in context |
|  | AO3.5b | Recognise the limitations of models |
|  | AO3.5c | Where appropriate, explain how to refine models |

Examiners should consistently apply the following general marking principles

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to students showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the student to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Work erased or crossed out

Erased or crossed out work that is still legible and has not been replaced should be marked. Erased or crossed out work that has been replaced can be ignored.

## Choice

When a choice of answers and/or methods is given and the student has not clearly indicated which answer they want to be marked, mark positively, awarding marks for all of the student's best attempts. Withhold marks for final accuracy and conclusions if there are conflicting complete answers or when an incorrect solution (or part thereof) is referred to in the final answer.

| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1}$ | Circles correct answer | AO1.1b | B 1 | $\frac{-1}{6 x}+C$ |
|  |  | Total |  | $\mathbf{1}$ |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{2}$ | Ticks correct answer | AO1.1b | B1 | Figure 3 |
|  |  | Total |  | $\mathbf{1}$ |
|  |  |  |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 3 | Expresses $2 \log _{a} 6$ as $\log _{a} 6^{2}$ or $\log _{a} 36$ divides by 3 inside the log term (PI) e.g. $2 \log _{a}\left(\frac{6}{3}\right)$ scores M1 but not $2 \frac{\log _{a} 6}{\log _{a} 3}$ | A01.1a | M1 | $\begin{gathered} \log _{a}\left(6^{2} / 3\right) \\ \log _{a} 12 \end{gathered}$ |
|  | Obtains correct final answer (condone the omission of base a) CAO | A01.1b | A1 |  |
|  | Total |  | 2 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Solves to find $\tan 2 \theta$ (allow M1 even if only $+\sqrt{ } 3$ given PI by any correct final value of $\theta$ ) | A01.1a | M1 | $\begin{gathered} \tan 2 \theta= \pm \sqrt{ } 3 \\ \tan 2 \theta=\sqrt{ } 3 \rightarrow 2 \theta=60^{\circ}, 240^{\circ}, 420^{\circ}, \\ 600^{\circ} \\ \tan 2 \theta=-\sqrt{3} \rightarrow 2 \theta=120^{\circ}, 300^{\circ}, 480^{\circ}, \\ 660^{\circ} \\ \theta=30^{\circ}, 60^{\circ}, 120^{\circ}, 150^{\circ}, 210^{\circ}, 240^{\circ}, \\ 300,330^{\circ} \end{gathered}$ |
|  | Obtains at least 3 correct final values for $\theta$ ignore extra incorrect terms or terms outside range | A01.1b | A1 |  |
|  | Obtains at least 3 correct final values of $\theta$ from $\tan 2 \theta=\sqrt{ } 3$ and at least 3 correct values from $\tan 2 \theta=-\sqrt{3}$ ignore extra incorrect terms or terms outside range | A01.1a | M1 |  |
|  | Obtains complete set of exactly 8 correct values for $\theta$ | A01.1b | A1 |  |
|  | Total |  | 4 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| $\mathbf{5}$ | Expands the bracket and obtains <br> any correct form (PI) | AO1.1b | B 1 |  |
|  | Integrates at least one of 'their' <br> terms correctly | AO1.1a | M 1 | $f(x)=f^{\prime}(x)=4 x^{2}-12+\frac{9}{x^{2}}$ |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 6(a) | Selects a method leading to any calculation pertaining to one of the following methods seen (not necessarily correct); gradients of sides, lengths of sides or intersection or lengths of diagonals | AO3.1a | M1 | Grad BC $=-5 / 2=$ Grad DA <br> $\operatorname{Grad} A B=2 / 5=\operatorname{Grad} D C$ <br> Both pairs of opposite sides have equal gradient so parallel, so $A B C D$ is a parallelogram <br> Grad $B C \times \operatorname{grad} A B=-1$ <br> $\mathrm{ABC}=90^{\circ}$ therefore all angles in ABCD are $90^{\circ}$ so ABCD is a rectangle |
|  | Finds gradients of all 4 sides or lengths of all 4 sides or midpoints of both diagonals correctly | A01.1b | A1 |  |
|  | Proves one angle is $90^{\circ}$ by using gradients or Pythagoras | A01.1a | M1 |  |
|  | Completes proof that ABCD is a rectangle. There must be a clear statement that there are 2 pairs of parallel sides and all angles are 90 | AO2. 1 | R1 |  |
|  | Note, there are various ways of proving that ABCD is a rectangle <br> ( $1-5$ below score M1 A1 M1 before final required statement for relevant R1 stating how their method used proves a rectangle) <br> 1. As in the typical solution shown: show that both pairs of opposite sides are parallel, show that one angle is $90^{\circ}$. <br> 2. Show that each pair of opposite sides is equal in length, show that one angle is $90^{\circ}$. <br> 3. Show that one pair of opposite sides is parallel and equal in length, show that one angle is $90^{\circ}$. <br> 4. Show that the diagonals bisect (the midpoint of one is also the midpoint of the other) and are equal in length. <br> 5. Show that each pair of opposite sides are parallel and length of the two diagonals are the same <br> NB May be expressed using vectors <br> NB Diagonals $A C$ and $B D=\sqrt{377}$ |  |  |  |
| (b) | Finds correct lengths of two adjacent sides (accept to at least 1dp accuracy) | A01.1a | M1 | $\begin{aligned} & \mathrm{AB}(=\mathrm{DC})=\sqrt{ } 261=3 \sqrt{ } 29 \\ & \mathrm{BC}(=\mathrm{DA})=\sqrt{ } 116=2 \sqrt{ } 29 \end{aligned}$ |
|  | Obtains correct area (AWRT) | AO1.1b | A1 | Area $=174$ |
|  | Total |  | 6 |  |



| Q 8 | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :---: |
| (a) | Produces a combined diagram <br> showing circles intersecting at <br> origin and (0, 10) or two separate <br> diagrams. Allow reasonable 'hand <br> drawn' circles which illustrate <br> symmetry. Circles must cut the $x$ <br> axis again. Do not accept circles <br> that go off the page. | AO2.2a | B1 |  |
| (b) | Deduces that $y$ coordinate of centre <br> is 5. (PI by any use of (y - 5) in any <br> circle equation or marked on <br> diagram or seen as a y coordinate <br> or used in Pythagoras) | AO2.2a | B1 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 9 | Uses $\tan \theta=\frac{\sin \theta}{\cos \theta}$ correctly (PI) (OE) | A01.1a | M1 | $\tan 15^{\circ}=\frac{\sqrt{ }(2-\sqrt{3})}{\sqrt{ }(2+\sqrt{3})}$ |
|  | Squares and multiplies by appropriate $\frac{\text { conjugate }}{\text { conjugate }}$ or vice versa | A01.1b | A1 | $\begin{aligned} \tan ^{2} 15^{\circ} & =\frac{2-\sqrt{3}}{2+\sqrt{3}} \times \frac{2-\sqrt{3}}{2-\sqrt{3}} \\ & =(2-\sqrt{3})^{2} \end{aligned}$ |
|  | Obtains correct values of $a$ and $b$ ( $a=7, b=-4$ ) <br> If no explicit evidence of the use of conjugate $\frac{\text { conjugate }}{}$ seen award max $1 / 3$ (M1 A0 R0) | AO2. 1 | R1 | $\tan ^{2} 15^{\circ}=7-4 \sqrt{ } 3$ |
|  | Total |  | 3 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 10 | The 3 appropriate ${ }_{n} \mathrm{C}_{\mathrm{r}}$ seen (ignore any extras) (PI by 55, 165 and 330 OE) | AO3.1a | M1 | ${ }_{n} \mathrm{C}_{2}{ }_{n} \mathrm{C}_{3}{ }_{n} \mathrm{C}_{4}$ |
|  | Forms a correct equation, accept $\frac{3}{2}\left({ }_{n} \mathrm{C}_{2}+{ }_{n} \mathrm{C}_{3}\right)={ }_{n} \mathrm{C}_{4}$ <br> Allow $\binom{n}{r}$ notation (condone $x$ terms in equation) | A01.1a | M1 | $\begin{aligned} \frac{3}{2}\left(\frac{n!}{(n-2)!2!}\right. & \left.+\frac{n!}{(n-3)!3!}\right) \\ & =\frac{n!}{(n-4)!4!} \end{aligned}$ <br> $\frac{3}{2}\left(\frac{n(n-1)}{2}+\frac{n(n-1)(n-2)}{}\right)$ |
|  | Obtains completely correct equation in terms of factorials. Reaching second line of typical solution scores M1 M1 A1 | A01.1b | A1 | $\begin{aligned} & 2\left(\frac{n(n-1)(n-2)(n-3)}{24}\right. \\ & =\frac{6}{24} \\ & 18+6 n-12=n^{2}-5 n+6 \end{aligned}$ |
|  |  |  |  | $0=n^{2}-11 n=n(n-11)$ |
|  | Reduces to a quadratic or solves the quartic (may involve calculator functions) | A01.1a | M1 |  |
|  | Chooses the correct solution. (The correct value of $n$ scores $5 / 5$ may be found by trial and error) | AO3.2a | A1 |  |
|  | Total |  | 5 |  |


| Q | Marking Instructions (I) | AO | Marks | Typical Solution (using $r$ ) |
| :--- | :--- | :---: | :---: | :---: |
| $\mathbf{1 1}$ | Obtains correct weld length in <br> terms of $h$ and $r$ | AO1.1b | B1 | Length of weld $=w=h+2 \pi r$ <br> Volume $=8000=\pi r^{2} h$ |
|  | Obtains formula for $h$ in terms of $r$ <br> or vice versa using volume $=8000$ | AO3.1b | M1 | So $h=\frac{8000}{\pi r^{2}}$ |


| Q | Marking Instructions (II) | AO | Marks | Typical Solution (using $h$ ) |
| :---: | :---: | :---: | :---: | :---: |
| 11 |  |  |  | Length of weld $=w=h+2 \pi r$ |
|  |  |  |  | Volume $=8000=\pi r^{2} h$ |
|  |  |  |  | $r=\sqrt{\frac{8000}{\pi h}}$ |
|  |  |  |  | $w=h+2 \pi \sqrt{\frac{8000}{\pi h}}$ |
|  |  |  |  | $=h+\sqrt{32000 \pi} h^{-\frac{1}{2}}$ |
|  |  |  |  | For minimum length of weld $\frac{d w}{d h}=0$ |
|  |  |  |  | $1-\frac{1}{2} \sqrt{32000 \pi} h^{-\frac{3}{2}}=0$ |
|  |  |  |  | leading to $h^{3}=8000 \pi$ |
|  |  |  |  | $h=29.3 \mathrm{~cm}$ |
|  |  |  |  | $r=9.32 \mathrm{~cm}$ |
|  |  |  |  | $\frac{d^{2} w}{d h^{2}}=\frac{3}{4} \sqrt{32000 \pi} h^{-\frac{5}{2}}$ |
|  |  |  |  | which is positive, so this is a minimum for $w$ |
|  | Total |  | 9 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 12(a) | Uses model to form one correct equation (PI by $a=200$ ) (ACF) Accept $1.105 a+1.221 b=331$ | A03.1b | M1 | $\begin{aligned} & 290=a+b \\ & 331=a \mathrm{e}^{0.1}+b \mathrm{e}^{0.2} \end{aligned}$ |
|  | Forms a second correct equation (ACF) | A01.1a | M1 | $290 \mathrm{e}^{0.1}=a \mathrm{e}^{0.1}+b \mathrm{e}^{0.1}$ <br> $b=\frac{\left(331-290 e^{0.1}\right)}{\left(e^{0.2}-e^{0.1}\right)}=90.3=90$ to the nearest integer <br> so $a=200$ |
|  | Obtains correct $a$ AWRT 200 and $b$ AWRT 90 (AG) <br> Only award if both previous M1's achieved. Do not award marks retrospectively for correct values of $a$ and $b$ used in part (b) | A01.1b | A1 |  |
| (b) | Substitutes $t=3$ and evaluates CAO | AO3.4 | B1 | $200 e^{0.3}+90 e^{0.6}=434$ |
| (c) | Forms inequality (accept < or >) (condone use of equation) FT 'their' value of $a$, but $b$ must be 90 | A01.1a | M1 | $\begin{aligned} & 90 e^{0.2 t}>200 e^{0.1 t} \\ & e^{0.1 t}>\frac{200}{90} \\ & 0.1 t>\ln \left(\frac{200}{90}\right) \\ & t>10 \ln \left(\frac{200}{90}\right)=7.985 \end{aligned}$ <br> Just less than 8 so during 2024 |
|  | Uses logs or calculator to solve 'their' inequality (or equation) If using trial and error must see $t=7$ and $t=8$ tested | A01.1a | M1 |  |
|  | Interprets final result. (Do not accept 2025) | AO3.2a | A1 |  |
| (d) | Gives one limitation of the model. Eg. Model must break down as both $n_{\mathrm{A}}$ and $n_{\mathrm{B}}$ will tend to infinity / model assumes nothing changes / no attempt to control the diseases / all the trees have died / finite number of trees / cure for the disease might be found / other factors such as drought could affect the model / etc. | AO3.5b | E1 | Eventually all of the trees will die so the model will no longer be accurate. |
|  | Total |  | 8 |  |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 3}$ | Circles correct answer |  | AO1.1b | B1 |
|  |  | Total |  | $\mathbf{1}$ |


| $\mathbf{Q}$ | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 4}$ | Circles correct answer | AO1.1b | B1 | 24.8 |
|  |  | Total |  | $\mathbf{1}$ |

## Accept probabilities as percentages in all questions

| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 15(a) | Calculates $P(X \leq 2)$ or $P(X \leq 3)$ using the binomial dist | AO3.4 | M1 | $\begin{gathered} P(X \leq 2)=0.55(177 \ldots) \\ (P(X \leq 3)=0.80(589 \ldots) \\ \\ P(X \geq 3)=1-P(X \leq 2)=0.448 \end{gathered}$ |
|  | Obtains correct answer <br> AWRT 0.448 | A01.1b | A1 |  |
| 15(b) | Calculates the cube of their answer to (a). Do not accept as part of a larger calculation or multiples of their cube. | A01.1a | M1 | $\begin{aligned} & 0.448 \ldots{ }^{3} \\ = & 0.090(3 \mathrm{dp}) \end{aligned}$ |
|  | Obtains correct answer( FT if AWFW 0.0899 to 0.0901 ) | A01.1b | A1F |  |
| 15(c) | States first appropriate assumption in context | AO3.5b | E1 | The probability of hitting the bullseye is fixed at 0.3 or <br> Hitting the bullseye with each dart is independent of hitting the bullseye with any other dart or <br> There are 2 possible outcomes, hit bullseye or does not hit bullseye |
|  | States second appropriate assumption in context Accept probability of hitting bullseye 'is constant' Do not accept 'fixed number of trials' | AO3.5b | E1 |  |
|  | Total |  | 6 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 16 | Sets up enumerated population using valid numbering stating range used (PI) | AO2.4 | E1 | Give each student a number from (000)1 to 3200 or equivalent <br> Generate random four digit integers using calculator |
|  | Explains how to obtain sample with respect to a specified range of random numbers. Accept random number generator / calculator set to give numbers from 1 to 3200 Do not accept 'drawn from a hat' (impractical for 3200 population) | AO2.4 | E1 |  |
|  | Explains how to deal with repeats and random numbers outside range (PI by both 'different' numbers and 'numbers from 1 to 3200' seen). | AO2.4 | E1 | Ignore repeats and any (random) numbers outside the range <br> Continue until 60 different numbers have been identified and select the students given those numbers |
|  | Explains how to select the 60 (expresses idea of matching numbers to students or selecting them) | AO2.4 | E1 |  |
|  | Total |  | 4 |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :--- | :---: | :---: | :--- |
| $\mathbf{1 7}$ | Comments on the lack of common <br> units or mentions any of these units <br> grams(g)/kg/millilitres(ml)/litres(l) | AO2.3 | E1 | There are no units stated so they <br> could all be different |
|  | Develops the point to show their <br> knowledge of the large data set, <br> must see grams (g) and <br> millilitres(ml) | AO2.4 | E1 | Butter and margarine would be <br> measured in grams whilst oils <br> would be measured in millilitres |
|  | Total |  |  |  |
|  |  | $\mathbf{2}$ |  |  |


| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 18 (a) | Identifies Donovan | AO1.2 | B1 | First Outlier Donovan <br> Reason <br> A data entry error has been made (should be 5 not 50) |
|  | Infers a reason for Donovan <br> - a data entry error has been made <br> - Donovan gets nervous/stressed under exam conditions and performed poorly in most recent test <br> - Donovan is not a very good player despite a lot of practice <br> - Just started playing so practised longer hours but performed poorly in exam <br> - External factors/illness <br> Accept other reasonable reason linking Donovan's practice time to their performance in the exam. | AO2.2b | E1 |  |
|  | Identifies Collins | AO1.2 | B1 |  |
|  | Infers a reason for Collins <br> - a data entry error has been made <br> - naturally very good piano player so does little practice <br> - 'Lucky' test score <br> Accept other reasonable reason linking Collins's practice time to their performance in the exam. | AO2.2b | E1 |  |
| 18(b)(i) | Describes correlation correctly, at least strong positive. Accept non - linear correlation, but do not accept numerical value to indicate strength | AO2.5 | B1 | Strong Positive Correlation |
| 18(b)(ii) | Interprets correlation in context (as given in typical solution OE) Do not accept the better you do in the exam the more you practised | AO3.2a | E1 | Students who complete more practice perform better in the exam |
|  | Total |  | 6 |  |

## Accept percentages throughout this question

| Q | Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 19 | States both hypotheses correctly for one-tailed test accept 'population proportion' $=0.7$ or $70 \%$, but NOT $x=$ or $\bar{x}=$ or $\mu=$ | AO2.5 | B1 | ```\(X=\) number of seeds which germinate \(\mathrm{H}_{0}: p=0.7\) \(\mathrm{H}_{1}: p>0.7\)``` <br> Under null hypothesis $X \sim \mathrm{~B}(20,0.7)$ |
|  | States model used PI can also be implied by 0.0278 or 0.00684 | AO3.3 | M1 |  |
|  | Calculates <br> $P(X \geq 18)$ or $P(X \geq 19)$, (PI by <br> $0.035(5)$ or 0.0076) but not $P(X=18) \text { or } P(X=19)$ | A01.1a | M1 | $\begin{aligned} P(X \geq 18)=1 & -P(X \leq 17) \\ & =1-0.965 \end{aligned}$ |
|  | Obtains correct probability for $P(X \geq 18)$ | A01.1b | A1 | $=0.035$ |
|  | Evaluates binomial model by comparing $0.035(5)$ or 0.0076 with 0.05 but not $P(X=18)$ or $P(X=19)$ | AO3.5a | M1 | $0.035<0.05$ |
|  | Infers $\mathrm{H}_{0}$ rejected (FT 0.0076), condone 'accept $\mathrm{H}_{1}$ ' | AO2.2b | A1F | Reject $\mathrm{H}_{0}$ |
|  | Concludes correctly in context. 'Sufficient evidence' or equivalent required. Only award for full complete correct solution. | AO3.2a | R1 | There is sufficient evidence to conclude that the new seeds are more likely to germinate. |
|  | Total |  | 7 |  |


| Q | Alternative Marking Instructions | AO | Marks | Typical Solution |
| :---: | :---: | :---: | :---: | :---: |
| 19 | States both hypotheses correctly for one-tailed test accept 'population proportion' $=0.7$ or $70 \%$, but NOT $x=$ or $\bar{x}=$ or $\mu=$ | AO2.5 | B1 | $X=$ number of seeds which germinate <br> $\mathrm{H}_{0}: p=0.7$ <br> $\mathrm{H}_{1}: p>0.7$ <br> Under null hypothesis $X \sim \mathrm{~B}(20,0.7)$ $\begin{aligned} & P(X \geq 17)=0.1071>0.05 \text { and } \\ & P(X \geq 18)=0.0355<0.05 \end{aligned}$ <br> Hence $X \geq 18$ is critical region <br> $X=18$ is in critical region <br> Reject $\mathrm{H}_{0}$ <br> There is sufficient evidence to conclude that the new seeds are more likely to germinate. |
|  | States model used PI can also be implied by 0.0716 or 0.0278 | AO3.3 | M1 |  |
|  | Finds $P(X \geq 17)$ and $P(X \geq 18)$ but not $P(X=17)$ or $P(X=18)$ accept 0.035 | A01.1a | M1 |  |
|  | Identifies correct critical region | A01.1b | A1 |  |
|  | Evaluates Binomial model by comparing $X=18$ with critical region (condone CR of $X \geq 17$ ) | AO3.5a | M1 |  |
|  | Infers $\mathrm{H}_{0}$ rejected, condone 'accept $\mathrm{H}_{1}{ }^{\prime}$ FT CR of $X \geq 17$ | AO2.2b | A1F |  |
|  | Concludes correctly in context. 'Sufficient evidence' or equivalent required. Only award for full complete correct solution. | AO3.2a | R1 |  |
|  | Total |  | 7 |  |
| TOTAL |  |  |  |  |
|  |  |  |  |  |  |

