A

## AQAE

Surname $\qquad$
Other Names
Centre Number
Candidate Number $\qquad$
Candidate Signature

## GCSE <br> MATHEMATICS

Higher Tier Paper 2 Calculator 8300/2H

Thursday 7 June 2018 Morning
Time allowed: 1 hour 30 minutes

For this paper you must have:

- a calculator
- mathematical instruments.

At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]

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## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## ADVICE

- In all calculations, show clearly how you work out your answer.


## DO NOT TURN OVER UNTIL TOLD TO DO SO

Answer ALL questions in the spaces provided

1 Here is a circle.


Circle the word that describes the shaded part. [1 mark]
segment chord sector arc

2 Circle the number that is in standard form. [1 mark]
$0.25 \times 10^{4}$
$6 \times 10^{7}$
$38 \times 10^{-3}$
$4 \times 10^{\frac{1}{2}}$
$3 y$ is $1 \frac{1}{2}$ times $x$.
Circle the ratio that is equivalent to $y: x$
[1 mark]
$2: 5$
$5: 2$
3: 2
$2: 3$

4 Work out 40 as a percentage of 10
Circle your answer. [1 mark]
$4 \% \quad 25 \% \quad 300 \%$ 400\%
[Turn over]

5 Match each sequence to its description.
One has been done for you. [4 marks]


## BLANK PAGE

## [Turn over]

6 The table shows information about the population of a city.

| Population in 2001 | Population in 2011 |
| :--- | :--- |
| 420000 | 480000 |

Liam claims,
"From 2011 to 2021 the population of the city will increase by the same percentage as from 2001 to 2011"

He works out,
population increase from 2001 to 2011
= 480000 - 420000
$=60000$
population in 2021
$=480000+60000$
$=540000$
Does the population of 540000 match his claim? You MUST show your working. [3 marks]

## Answer



7 On three days, Ali throws darts at a target. Here are his results.

|  | Number of <br> throws | Number of <br> hits | Number of <br> misses |
| :--- | :--- | :--- | :--- |
| Monday | 20 | 15 | 5 |
| Tuesday | 30 | 22 | 8 |
| Wednesday | 40 | 17 | 23 |
| Total | 90 | 54 | 36 |

7 (a) Work out TWO different estimates for the probability of Ali hitting the target. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
and $\qquad$

# 7 (b) Which of your two answers is the better estimate for the probability of Ali hitting the target? 

Give a reason for your answer. [1 mark]

Answer $\qquad$
$\qquad$

## Reason

$\qquad$
$\qquad$
[Turn over]

## 12

8 Theo starts with savings of $£ 18$ James starts with no savings.

Each week from now,
Theo will save $£ 4.50$ and James will save $£ 4$
In how many weeks will Theo and James have savings in the ratio 15:8? [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]

9 The length of each side of a regular pentagon is 8.4 cm to 1 decimal place.

9 (a) Complete the error interval for the length of one side. [2 marks]
$\qquad$
$\qquad$ $\ldots \mathrm{cm} \leqslant$ length $<$ cm

9 (b) Complete the error interval for the perimeter. [1 mark]
$\qquad$ cm $\leqslant$ perimeter $<$
cm

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## [Turn over]

A container is a hemisphere of radius 30 cm


Sand fills the container at a rate of $4000 \mathrm{~cm}^{3}$ per minute.

Does it take LESS THAN a quarter of an hour to fill the container?
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]


11 Two ordinary fair dice are rolled.
11 (a) Complete the tree diagram. [1 mark]

1st dice


11 (b) Work out the probability that BOTH dice land on a number less than 3
[1 mark]

Answer

11 (c) Work out the probability that EXACTLY ONE of the dice lands on a number less than 3
[2 marks]

Answer
[Turn over]


Take the sides of all squares of the grid to be 1 cm long.
A straight line is drawn on the centimetre grid.


Fay assumes that the scale is
1 cm represents 1 unit.
12 (a) Use her assumption to work out the gradient of the line. [1 mark]
$\qquad$
$\qquad$

Answer

12 (b) In fact, the scale is $1 \mathbf{c m}$ represents 2 units. Which statement is correct?
Tick ONE box. [1 mark]


The answer to part (a) is too big


The answer to part (a) stays the same

The answer to part (a) is too small

13 Show that, for $x \neq-1$ $\frac{8 x^{2}-8}{4 x+4}$ simplifies to the form $a x+b \quad$ where $a$ and $b$ are integers. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

14 The scale drawing represents a garden.
Water from a sprinkler at $P$ reaches up to
20 metres from $P$.
Water from a sprinkler at $Q$ reaches up to
25 metres from $Q$.

## SCALE: 1 cm represents 5 m

Take the sides of all squares of the grid to be 1 cm long.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Using a pair of compasses, show the region that water from BOTH sprinklers reaches. [2 marks]
[Turn over]

## 15100 men and 100 women took a test. SCORES

|  | Median | Interquartile <br> range | Range |
| :--- | :--- | :--- | :--- |
| Men | 28 | 7.5 | 31 |
| Women | 30 | 9 | 37 |

Using this data, which statement MUST be true? Tick ONE box. [1 mark]


Men had a higher average score than women


Men had more consistent scores than women


A woman had the highest score


A man had the lowest score

## BLANK PAGE

## [Turn over]

16 Some concrete has volume $3.8 \mathrm{~m}^{3}$
16 (a) The density of the concrete is $2400 \mathrm{~kg} / \mathrm{m}^{3}$ Work out the mass of the concrete. [2 marks]
$\qquad$
$\qquad$
$\qquad$

Answer kg

16 (b) The $3.8 \mathrm{~m}^{3}$ of concrete is made into the shape of a cylinder.
The base has radius 0.5 metres.


Work out the height of the cylinder. [2 marks]
$\qquad$
$\qquad$
$\qquad$

Answer m
[Turn over]

17 A ball is thrown vertically upwards.
The graph shows the height of the ball above the ground after it is thrown.

Height
(m)

Height of ball


Time (s)

17 (a) For how many seconds is the ball at a height of MORE THAN 2 metres? [1 mark]
$\qquad$
Answer S

17 (b) After how many seconds is the ball at instantaneous rest when it is in the air? [1 mark]

Answer S

17 (c) Work out the average speed of the ball when it is moving downwards. [2 marks]
$\qquad$
$\qquad$
$\qquad$

Answer m/s
[Turn over]


18 The solution of $3^{x}=300$ lies between two consecutive integers.

Work out the two integers. [1 mark]
$\qquad$
$\qquad$

Answer
and $\qquad$

19 A pentagon is made from a square and an isosceles triangle.

The diagram is not drawn accurately.


## Work out the perimeter of the pentagon. [4 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer cm
[Turn over]

20 Here is an inflated swimming ring with dimensions in centimetres.


The volume of the ring, $V \mathrm{~cm}^{3}$, is given by

$$
V=0.25 \pi^{2}(b-a)^{2}(b+a)
$$

Work out the volume when $a=20$ and $b=30$ Give your answer to 3 significant figures. [3 marks]
$\qquad$

## Answer $\mathrm{cm}^{3}$

## [Turn over]

$\square$

21 Liz and Tia are walking towards a shop along different straight paths.
The diagram shows their positions at 2 pm
The diagram is not drawn accurately.


21 (a) Assume they walk at the same speed.
Who will arrive at the shop first?
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

21 (b) In fact, Liz walks at a faster speed than Tia. How does this affect the answer to part (a)? [1 mark]
$\qquad$
$\qquad$
[Turn over]

22 A circle, centre $O$, passes through (5, 0).


What is the equation of the circle?
Circle your answer. [1 mark]

$$
\begin{array}{ll}
x^{2}+y^{2}=25 & x^{2}+y^{2}=5 \\
x^{2}+y^{2}=10 & x^{2}+y^{2}=100
\end{array}
$$

23 Solids $X$ and $Y$ are similar.
$X$ has volume $64 \mathrm{~cm}^{3}$
$Y$ has volume $343 \mathrm{~cm}^{3}$
The surface area of $X$ is $176 \mathrm{~cm}^{2}$
Work out the surface area of Y . [3 marks]
$\qquad$
$\qquad$
$\qquad$

Answer
cm ${ }^{2}$
[Turn over]


24 A tank is a cuboid measuring 50 cm by 35 cm by 20 cm
All lengths are to the NEAREST CENTIMETRE.
A container has a capacity of EXACTLY 34 litres.
1 litre $=1000 \mathrm{~cm}^{3}$
Which has the greater capacity?
Tick ONE box.


Show working to support your answer. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## [Turn over]

25 The Venn diagram shows some information about 150 students.
$\xi=150$ students
$\mathrm{C}=$ students who study Chemistry
P = students who study Physics
$\xi$


The probability that a Physics student, chosen at random, also studies Chemistry is $\frac{5}{12}$

One of the 150 students is chosen at random.
Work out the probability that the student does NOT study either Chemistry or Physics. [4 marks]
$\qquad$
$\qquad$
$\qquad$

## 41

## Answer

[Turn over]

$$
\begin{aligned}
& \text { A curve has equation } \quad y=4 x^{2}+5 x+3 \\
& \text { A line has equation } \quad y=x+2 \\
& \text { Show that the curve and the line have EXACTLY } \\
& \text { one point of intersection. } \\
& \text { Do NOT use a graphical method. [4 marks] }
\end{aligned}
$$

$\qquad$
$\qquad$
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$\qquad$

27 Prove algebraically that 2.75 converts to the fraction $\frac{124}{45}$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## 44

$$
f(x)=5-x \text { and } g(x)=3 x+7
$$

28 (a) Simplify $f(2 x)+g(x-1)$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

28 (b) Solve $\mathrm{g}^{-1}(x)=2 x$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$
$x=$

END OF QUESTIONS

## 46

## There are no questions printed on this page

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-5$ |  |
| $6-9$ |  |
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