# GCSE <br> MATHEMATICS <br> 8300/1H 

Higher Tier Paper 1 Non-Calculator
Mark scheme
November 2018
Version: 1.0. Final

* $18 \mathrm{bG} 8300 \mathrm{IH} / \mathrm{MS}^{*}$

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special case. Marks awarded for a common misinterpretation which has some mathematical worth.

M dep $\quad$ A method mark dependent on a previous method mark being awarded.

B dep A mark that can only be awarded if a previous independent mark has been awarded.
oe
Or equivalent. Accept answers that are equivalent. eg accept 0.5 as well as $\frac{1}{2}$
[a, b] Accept values between a and b inclusive.
[a, b) $\quad$ Accept values $\mathrm{a} \leq$ value $<\mathrm{b}$
3.14... Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416

Use of brackets It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

## Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

## Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

## Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

| Question | Mnswer | Comments |
| :--- | :---: | :---: | :---: |


| $\mathbf{1}$ | $5^{8}$ | B1 |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{2}$ | $200 \pi$ | B1 |  |


| 3 | $22 a$ | B1 |  |
| :---: | :---: | :---: | :---: |
| 4 | $\frac{\sqrt{3}}{2}$ | B1 |  |


| Question | Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |



The Additional Guidance for question 5 is on the next page

| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| $\begin{gathered} 5 \\ \text { cont } \end{gathered}$ | Additional Guidance |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Working with decimals |  |  |  | 0,3 or 4 |
|  | Ignore incorrect attempt to simplify a mixed number eg $3 \frac{3}{16}=3 \frac{1}{8}$ |  |  |  | M1M1A1B1 |
|  | $3 \frac{3}{16}$ seen, then $\frac{51}{16}$ on answer line |  |  |  | M1M1A1B0 |
|  | $\frac{9}{2}$ and $\frac{8}{3}, \quad \frac{27}{6} \div \frac{16}{6}, \quad \frac{27}{16}, \quad 1 \frac{11}{16}$ |  |  |  | M1M1A0B1ft |
|  | $\frac{9}{2}$ and $\frac{8}{3}, \quad \frac{27}{6} \div \frac{16}{6}, \quad 1 \frac{11}{16}$ |  |  |  | M1M1A0B1ft |
|  | $\frac{9}{2}$ and $\frac{4}{3}, \quad \frac{27}{6} \div \frac{8}{6}, \quad 3 \frac{3}{8}$ |  |  |  | M0M1A0B1ft |


| Question | Answer | Mark | Comments |
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| 6 | Alternative method 1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Correct reading of at least one <br> value  <br> at 0 hours $[46,50]$ <br> at 1 hour $[63,67]$ <br> at 2 hours $[80,84]$ <br> at 3 hours $[96,100]$ <br> at 4 hours $[114,118]$ | M1 | may be seen on graph |  |
|  | subtraction of two values correct number of hours | M1 | division by 1 may be implied |  |
|  | 17 | A1 | SC1 29 |  |
|  | Alternative method 2 |  |  |  |
|  | A difference in the range  <br> for 1 hour $[15,19]$ <br> for 2 hours $[32,36]$ <br> for 3 hours $[49,53]$ <br> for 4 hours $[66,70]$ | M1 | may be seen on graph |  |
|  | difference correct number of hours | M1 | division by 1 may be implied |  |
|  | 17 | A1 | SC1 29 |  |
|  | Additional Guidance |  |  |  |
|  | $(119-42) \div 4=19.25$ |  |  | M0M1A0 |
|  | for 2nd M1 in Alt 1, subtraction must be in the correct order unless recovered |  |  |  |
|  | 17 does not imply three marks, so working must be checked eg $(110-42) \div 4=17$ |  |  | M0M1A0 |


| Question | Answer | Mark | Comments |
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The Additional Guidance for question 7 is on the next page

| Question | Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| $*$ <br> 7 <br> cont | If comparing $72^{\circ}$ to $90^{\circ}$, they must state that they are referring to the <br> exterior angles |  |
| :---: | :--- | :--- |
|  | If 'Yes' is ticked, M1 can still be scored |  |
|  | If neither box is ticked, 'No' must be implied by the explanation for <br> $M 1 A 1$ |  |



| Question | Answer | Mark | Comments |
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| Question | Answer | Mark | Comments |
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| 8(c) | Ticks 'Her prediction could be too low or too high' <br> and <br> explains that fewer landings in winter would make it too low, but fewer landings at night would make it too high <br> or states that the actual numbers are not given | B2 | oe reason <br> B1 <br> ticks 'Her prediction c too high' | too low or |
| :---: | :---: | :---: | :---: | :---: |
|  | Additional Guidance |  |  |  |
|  | Ticks 'Her prediction could be too low or too high' and states that there is not enough data |  |  | B1 only |


| Question | Answer | Mark | Comments |
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| Question | Answer | Mark | Comments |
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| 10 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | 280-80 or 200 | M1 |  |
|  | $\begin{aligned} & \text { their } 200 \div 80(\times 100) \\ & \text { or } 2.5(\times 100) \end{aligned}$ | M1dep | oe |
|  | 250 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $280 \div 80$ or 3.5 | M1 | oe |
|  | $\begin{aligned} & 280 \div 80 \times 100(-100) \\ & \text { or their } 3.5 \times 100(-100) \\ & \text { or } 350(-100) \\ & \text { or (their } 3.5-1)(\times 100) \\ & \text { or } 2.5(\times 100) \end{aligned}$ | M1dep | oe |
|  | 250 | A1 |  |


| 11 | A and D | B1 |  |
| :--- | :--- | :--- | :--- |


| Question | Answer | Mark | Comments |
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| Question | Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 13 | Alternative method 1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $2 \times 5: 3 \times 5$ or $10: 15$ and $5 \times 3: 4 \times 3$ or $15: 12$ | M1 | oe common value for $f$ eg $10: 15: 12$ or $\frac{2}{3}: 1: \frac{4}{5}$ |  |
|  | 10: 12 | M1dep | oe unsimplified ratio condone fractions or decimals |  |
|  | 5: 6 | A1 |  |  |
|  | Alternative method 2 |  |  |  |
|  | $3 e=2 f$ and $4 f=5 g$ | M1 | oe equations |  |
|  | $6 e=5 g$ | M1dep | oe equation |  |
|  | $5: 6$ | A1 |  |  |
|  | Additional Guidance |  |  |  |
|  | Variables in an otherwise correct answer: <br> the same variable scores 2 marks, eg $5 f: 6 f$ different variables do not score, unless earlier marks can be awarded, eg $5 e: 6 g$ with no working worth M1 or M1M1 |  |  | M1M1A0 <br> MOMOAO |


| 14 | $1-0.3-0.15-0.35$ or $1-0.8$ or 0.2 <br> or $0.15+0.35(+0.2)$ or $0.5(+0.2)$ or 1-0.3 <br> or <br> $A^{\prime} \cup B$ clearly shaded on diagram | M1 | oe |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 0.7 | A1 | oe fraction, decimal or percentage |  |
|  | Additional Guidance |  |  |  |
|  | Do not award M1 for $0.15+0.35$ or calculation $\text { eg } 0.15+0.35=0.5,0.5+0.3=0$ |  | n used in an incorrect <br> working) | MO |


| Question | Answer | Mark | Comments |
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| 15(a) | C and 'lowest median' | B2 | oe B1 C |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Additional Guidance |  |  |  |
|  | If the value of the median is given it must be 4 for B2 |  |  |  |
|  | Accept midpoint oe for median |  |  |  |
|  | Do not accept mean for median |  |  |  |
|  | Only accept average for median if the value of 4 is also given |  |  |  |
|  | Accept mention of the lowest lower quartile with correct mention of the median for B2, but do not accept mention of any extra statistical measure as part of their justification |  |  |  |


| 15(b) | B and 'lowest interquartile range' or <br> $B$ and 'lowest range' | B2 | oe <br> B1 B |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Additional Guidance |  |  |  |
|  | If the value of the interquartile range is given it must be 2 for B 2 <br> If the value of the range is given it must be 5 for B 2 |  |  |  |
|  | For B2, do not accept non-statistical reasons, eg 'the narrowest box' |  |  |  |
|  | For B2, do not accept mention of any extra statistical measure as part of their justification |  |  |  |


| Question | Answer | Mark | Comments |
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| 16 | 27000 | B 1 |  |
| :--- | :--- | :---: | :--- |



| Question | Answer | Mark | Comments |
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| Question | Answer | Mark | Comments |
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| 19(a) | $2(x+5)=y+8$ <br> or $2 x+10=y+8$ | M1 | oe eg $\frac{x+5}{y+8}=\frac{1}{2}$ or $\frac{y+8}{x+5}=2$ |
| :---: | :--- | :---: | :---: |
|  | $2 x+10=y+8$ <br> and $y=2 x+2$ | A1 |  |


| 19(b) | $x+10=y+1$ | M1 | oe |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Eliminates $x$ or $y$ from their $(x+10)=y+1$ and $y=2 x+2$ | M1 | their $(x+10)=$ in $x$ and $y$ eg $x+10=y-1$ <br> followed by $x+11=2 x+2$ | an equation <br> 2) |
|  | $x=7$ and $y=16$ | A1 |  |  |
|  | Additional Guidance |  |  |  |
|  | $x=7$ or $y=16$ with no value or an incorrect value for the other unknown and no working worth M marks |  |  | MOMOAO |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 20 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | angle $Q P R=27$ | M1 | may be seen on diagram |
|  | $\text { angle } X P S=\frac{180-50}{2} \text { or } 65$ | M1 | may be seen on diagram |
|  | ```angle QPR = 27 and angle XPS = 65 and angle QPS = 92 and angle in a semicircle is a right angle``` | A1 | oe accept $92 \neq 90$ |
|  | all reasons for angle facts: angles in same segment (are equal) <br> and angle sum of triangle (is 180) and base angles of isosceles triangle (are equal) | A1 | oe <br> oe <br> oe |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 20 cont | Alternative method 2 |  |  |
| :---: | :---: | :---: | :---: |
|  | ```angle SXR=180-50 or 130 and angle XRS = 180-their 130-27 and angle PQS = their 23``` | M1 | may be seen on diagram <br> angle $X R S=23$ |
|  | angle $X S P=\frac{180-50}{2}$ or 65 | M1 | may be seen on diagram |
|  | ```angle SXR = 130 and angle XRS = 23 and angle PQS = 23 and XSP = 65 and angle QPS = 92 and angle in a semicircle is a right angle``` | A1 | oe accept $92 \neq 90$ |
|  | all reasons for angle facts: angles on a straight line (add up to 180) <br> and angle sum of triangle (is 180) and angles in same segment (are equal) <br> and base angles of isosceles triangle (are equal) | A1 | oe <br> oe <br> oe <br> oe |


| Question | Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |



| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 22 | Any two of $x(x-2)$ and $7(x+4)$ and $(x-2)(x+4)$ | M1 | oe <br> $x(x-2)$ and $7(x+4)$ cannot be denominators |
| :---: | :---: | :---: | :---: |
|  | correct equation including $x(x-2)$ and $7(x+4)$ and $(x-2)(x+4)$ | M1dep |  |
|  | $x^{2}-2 x+7 x+28=x^{2}+4 x-2 x-8$ | M1dep | oe all brackets must be expanded |
|  | -12 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\frac{x(x-2)}{x+4}+7=x-2$ | M1 |  |
|  | $\frac{x(x-2)}{x+4}=x-9$ <br> or $x(x-2)=(x-9)(x+4)$ | M1dep |  |
|  | $x^{2}-2 x=x^{2}-9 x+4 x-36$ | M1dep | oe all brackets must be expanded |
|  | -12 | A1 |  |
|  | Alternative method 3 |  |  |
|  | $x+\frac{7(x+4)}{x-2}=x+4$ | M1 |  |
|  | $\frac{7(x+4)}{x-2}=4$ <br> or $7(x+4)=4(x-2)$ | M1dep |  |
|  | $7 x+28=4 x-8$ | M1dep | oe all brackets must be expanded |
|  | -12 | A1 |  |
|  | Additional Guidance |  |  |
|  | In Alt 1, do not allow $x \times x-2$ or $7 \times x+4$ unless recovered |  |  |


| Question | Answer | Mark | Comments |
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| 23 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\sqrt{4}: \sqrt{9}$ or $2: 3$ | M1 | length $A$ : length $B$ |
|  | $30 \div$ their $3 \times$ their 2 or 20 | M1dep | length $A$ |
|  | $480 \div$ their 20 or 24 | M1dep | area cross section A |
|  | their $24 \div 4 \times 9$ | M1dep |  |
|  | 54 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\sqrt{4}: \sqrt{9}$ or $2: 3$ | M1 | length $A$ : length B |
|  | $(\sqrt{4})^{3}:(\sqrt{9})^{3}$ or $8: 27$ | M1dep | volume A : volume B |
|  | $480 \div$ their $8 \times$ their 27 or 1620 | M1dep | volume B |
|  | their $1620 \div 30$ | M1dep |  |
|  | 54 | A1 |  |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 24 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \frac{2 \sqrt{6}}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} \\ & \text { or } \frac{\sqrt{3}}{\sqrt{10}} \times \frac{\sqrt{10}}{\sqrt{10}} \end{aligned}$ | M1 |  |
|  | $\begin{aligned} & \frac{2 \sqrt{30}}{5} \text { or } \frac{4 \sqrt{30}}{10} \\ & \text { or } \frac{\sqrt{30}}{10} \end{aligned}$ | M1dep |  |
|  | $\frac{3 \sqrt{30}}{10}$ | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\begin{aligned} & \frac{2 \sqrt{6} \sqrt{2}}{\sqrt{10}}-\frac{\sqrt{3}}{\sqrt{10}} \\ & \text { or } \frac{2 \sqrt{12}}{\sqrt{10}}-\frac{\sqrt{3}}{\sqrt{10}} \end{aligned}$ | M1 | oe common denominator eg $\frac{2 \sqrt{60}}{\sqrt{50}}-\frac{\sqrt{15}}{\sqrt{50}}$ |
|  | $\frac{4 \sqrt{3}}{\sqrt{10}}-\frac{\sqrt{3}}{\sqrt{10}}$ or $\frac{3 \sqrt{3}}{\sqrt{10}}$ | M1dep | oe common denominator and common surd in numerator $\frac{4 \sqrt{15}}{\sqrt{50}}-\frac{\sqrt{15}}{\sqrt{50}} \text { or } \frac{3 \sqrt{15}}{\sqrt{50}}$ |
|  | $\frac{3 \sqrt{30}}{10}$ | A1 |  |
|  |  | itional | uidance |
|  | Ignore an attempt at fur | on after | $\frac{\sqrt{30}}{10}$ M1M1A1 |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 25 | Alternative method 1 |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & a(-3)^{2}+b(-3)+c=0 \\ & \text { or } a(3)^{2}+b(3)+c=0 \end{aligned}$ | M1 | oe |  |
|  | any two of $(-) 6 b=0, c=18 \text { and } 9 a+18=0$ | M1dep | oe |  |
|  | $y=18-2 x^{2}$ | A1 | oe equation |  |
|  | Alternative method 2 |  |  |  |
|  | $y=18-2 x^{2}$ | B3 | oe equation <br> B2 correct equation missing $y=$ <br> eg $18-2 x^{2}$ <br> B1 <br> equation of a quadratic curve that passes through $(-3,0)$ or $(3,0)$ or $(0,18)$ <br> condone missing $y=$ <br> eg $(y=) 18-x^{2}$ or $(y=)(3+x)(3-x)$ <br> or $(y=) x^{2}-2 x-3$ <br> or $(y=)(x+3)(x-3)$ |  |
|  | Additional Guidance |  |  |  |
|  | Correct equations include$\begin{aligned} & y=2(3+x)(3-x) \\ & y=-2(x+3)(x-3) \\ & y=(6+2 x)(3-x) \\ & y=(3+x)(6-2 x) \end{aligned}$ |  |  |  |
|  | For B3, B2 or B1 ignore incorrect expansion after correct equation or expression seen |  |  |  |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 26 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $0.5 \times 20 \times x \times \sin 60$ <br> or $10 x \sin 60$ or $5 \sqrt{3} x$ | M1 | oe |
|  | $\begin{aligned} & 0.5 \times 20 \times x \times \sin 60=25 \sqrt{3} \\ & \text { or } x=5 \end{aligned}$ | M1dep | oe equation |
|  | $\begin{aligned} & \text { (their } 5)^{2}+20^{2} \\ & -2 \times \text { their } 5 \times 20 \times \cos 60 \\ & \text { or } 25+400-200 \cos 60 \\ & \text { or } 325 \end{aligned}$ | M1 | oe their 5 must be their value of $x$ |
|  | $\sqrt{\text { their 325 }}$ | M1dep | dep on 3rd M1 <br> their 325 can be unsimplified |
|  | $5 \sqrt{13}$ | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\begin{aligned} & 0.5 \times 20 \times h=25 \sqrt{3} \\ & \text { or } h=\frac{5 \sqrt{3}}{2} \end{aligned}$ | M1 | oe any letter <br> $h$ is perpendicular height for 20 cm base |
|  | $\begin{aligned} & \sin 60=\frac{\text { their } \frac{5 \sqrt{3}}{2}}{x} \\ & \text { or } x=5 \end{aligned}$ | M1dep | oe |
|  | $\begin{aligned} & \text { (their } 5)^{2}+20^{2} \\ & -2 \times \text { their } 5 \times 20 \times \cos 60 \\ & \text { or } 25+400-200 \cos 60 \\ & \text { or } 325 \end{aligned}$ | M1 | oe their 5 must be their value of $x$ |
|  | $\sqrt{\text { their 325 }}$ | M1dep | dep on 3rd M1 <br> their 325 can be unsimplified |
|  | $5 \sqrt{13}$ | A1 |  |


| Question | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |



| 27(a) | $-k$ | B 1 |  |
| :--- | :--- | :--- | :--- |


| 27(b) | $k$ | B 1 |  |
| :--- | :--- | :--- | :--- |

