

Α

Surname
Other Names
Centre Number
Candidate Number
Candidate Signature
GCSE
MATHEMATICS
Higher Tier Paper 3 Calculator
8300/3H
Monday 12 November 2018 Morning
Time allowed: 1 hour 30 minutes
At the top of the page, write your

surname and other names, your centre number, your candidate number and add your signature.



For this paper you must have:

- a calculator
- mathematical instruments.

INSTRUCTIONS

- Use black ink or black ball-point pen.
 Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.



INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

ADVICE

In all calculations, show clearly how you work out your answer.

DO NOT TUDN OVED UNTU TOLD

TO DO SO



Answer ALL questions in the spaces provided.

1 A shape is translated by the vector

4

In which direction does the shape move?

Circle your answer. [1 mark]

up down

 $\begin{pmatrix} 0 \\ 4 \end{pmatrix}$

left right



2 What is 1.75 kilometres as a fraction of 700 metres?

Circle your answer. [1 mark]

3 The first 4 terms of a linear sequence are

3 11 19 27 Circle the expression for the *n* th term. [1 mark]

8 – 5*n n* + 8

8*n* + 3 8*n* - 5



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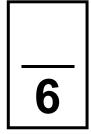


Work out the lowest common multiple (LCM) of 20, 30 and 40
Circle your answer. [1 mark]
10 120
240 24 000

5 The length of a table is 110 cm to the nearest cm

Complete the error interval. [2 marks]

_cm ≤ length < ____cm





6 A music festival has taken place each year from 2011

The table shows the number of people who attended each year.

			2013	2014
Number of people	350	583	906	1471

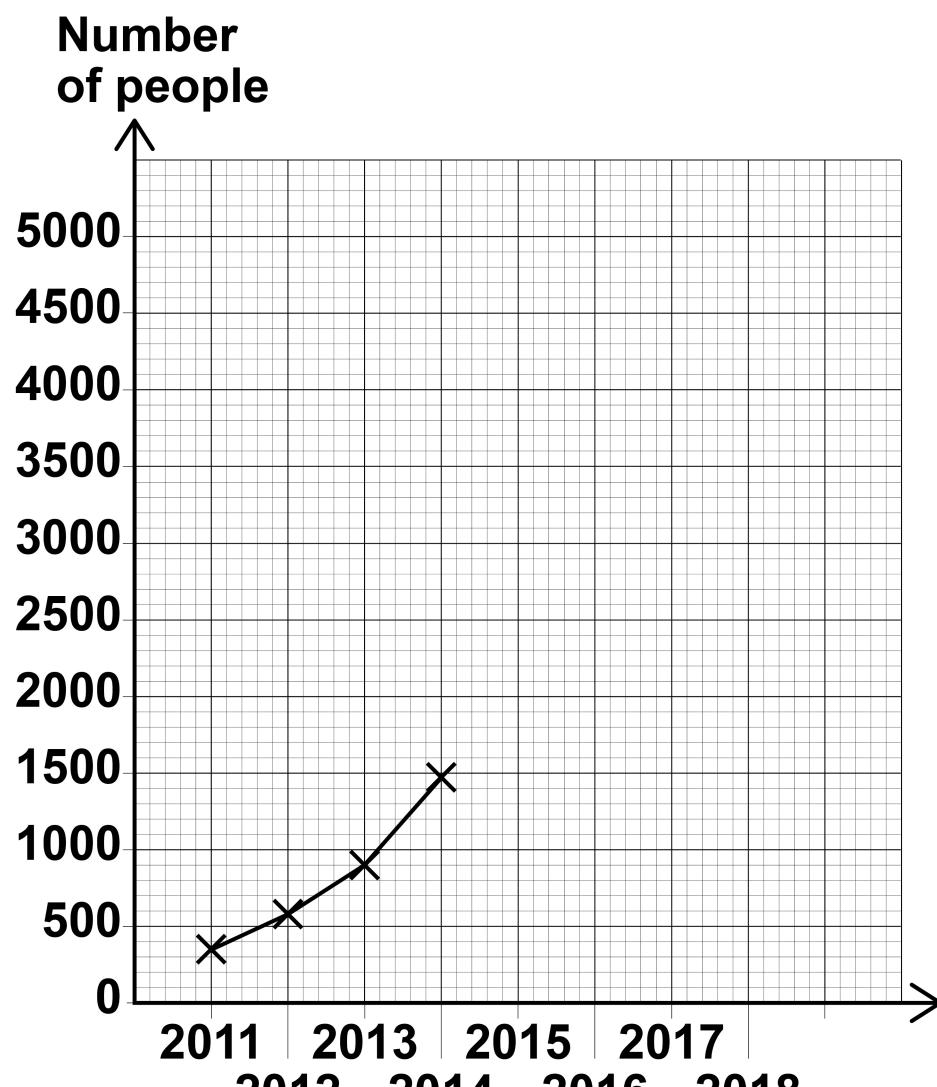
Year	2015	2016	2017	2018
Number of people	2023	2612	3251	3780

The festival organisers draw a time series graph to represent the data.

The first four years have been plotted.

6 (a) Complete the graph on page 9. [2 marks]





9

2012 2014 2016 2018 Year



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6 (b) Use the graph to estimate the number of people who will attend the festival in 2019 [2 marks]

Answer

[Turn over]

4



7
$$k = n^2 + 9n + 1$$

Mo says,

"*k* will be a prime number for all integer values of *n* from 1 to 9"

Show that Mo is wrong.

You MUST show that your value of *k* is NOT prime. [3 marks]



13



8 Doug owes an amount of £600

He wants to pay off this amount in five months.

He says,

"Each month, I will pay back 20% of the amount I still owe."

Show working to check if his method is correct. [3 marks]







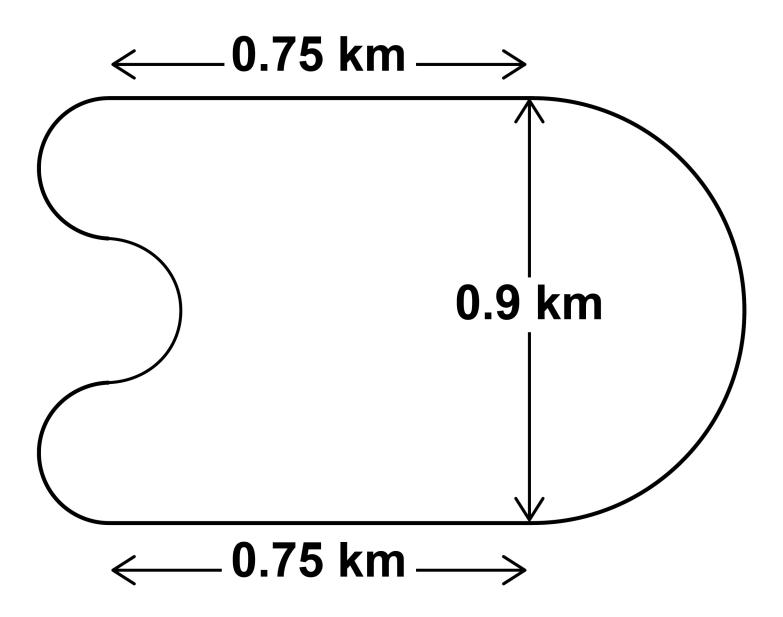
9 A motor racing circuit consists of

two parallel straight sections, each of length 0.75 km

a semicircle of diameter 0.9 km

three equal, smaller semicircles.

The diagram is not drawn accurately.



The length of a motor race must be greater than 305 km



What is the lowest number of FULL laps needed at this circuit?

You MUST show your working. [5 marks]

Answer



18

10 Solve
$$8 > 3 - \frac{1}{2}x$$
 [2 marks]

Answer

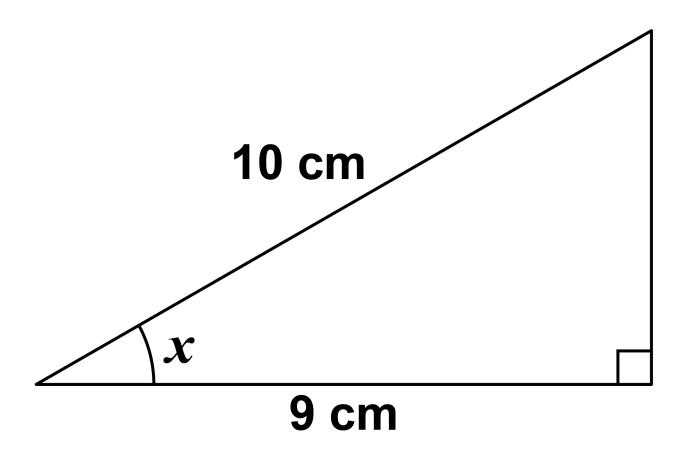


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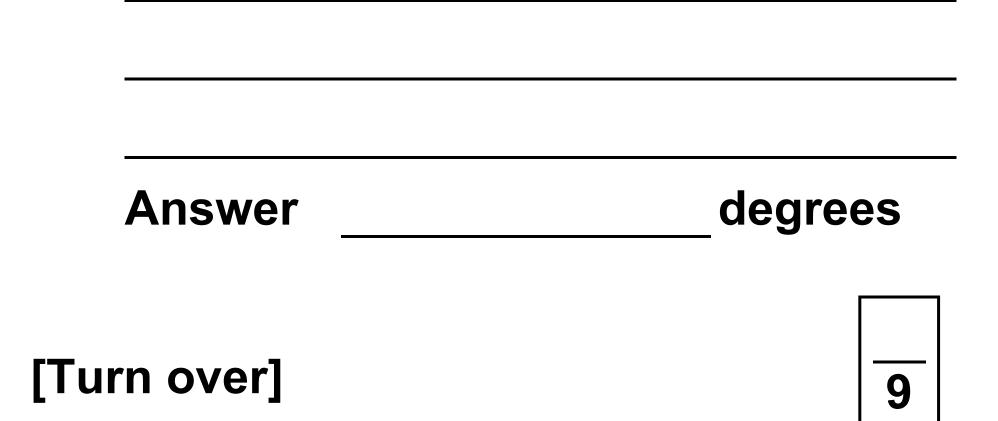
11 Use trigonometry to work out the size of angle *x*. [2 marks]

The diagram is not drawn accurately.

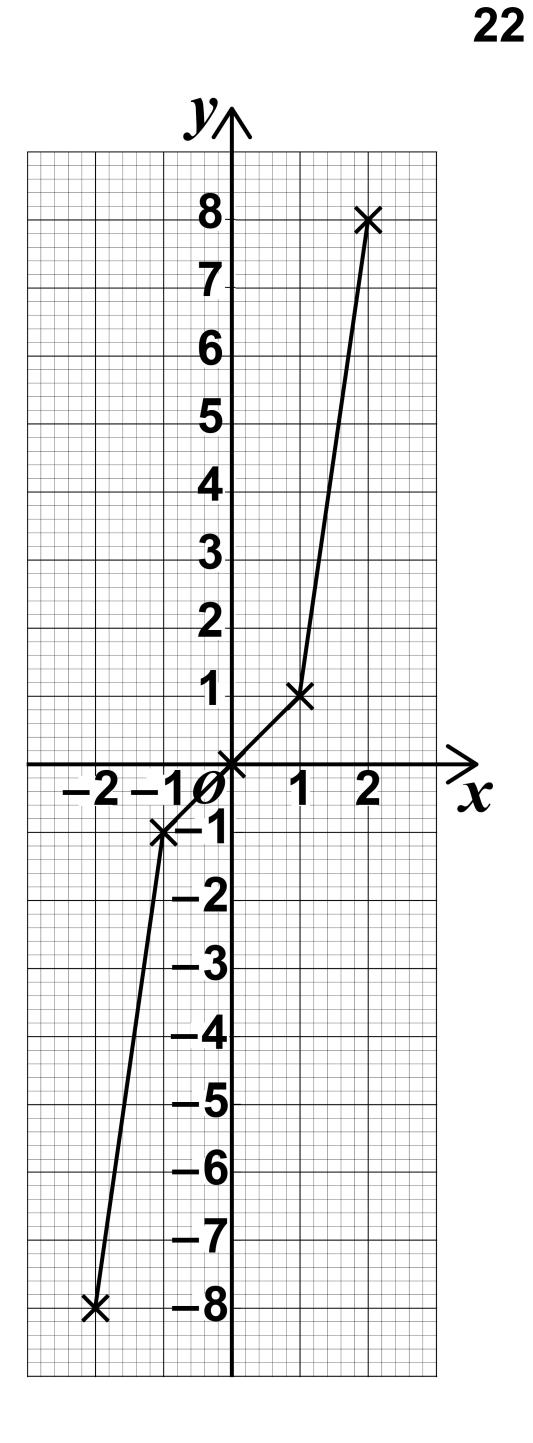




21









12 Lewis wants to draw the graph $y = x^3$ for values of x from -2 to 2

The graph is on page 22.

Make ONE criticism of his graph. [1 mark]



13 The probability of Heads when a biased coin is thrown is 0.6

The coin is thrown 500 times.

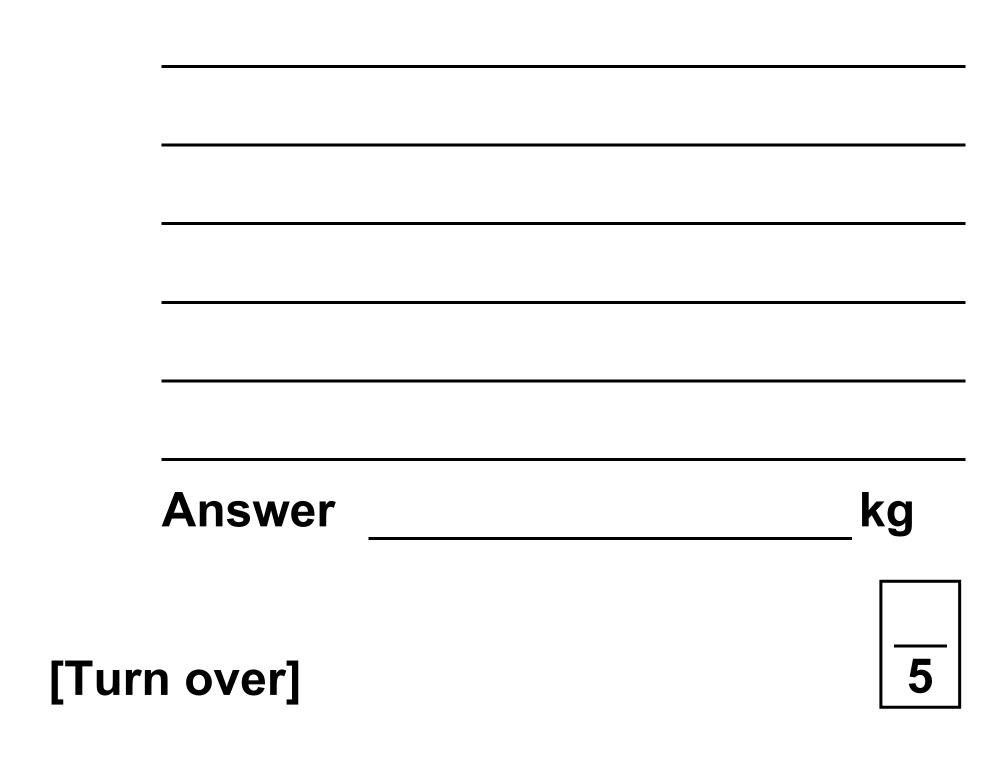
Circle the expected number of Tails. [1 mark]

- 20 200 250 300
- 14 The mean mass of a squad of 19 hockey players is 82 kg

A player of mass 93 kg joins the squad.

Work out the mean mass of the squad now. [3 marks]





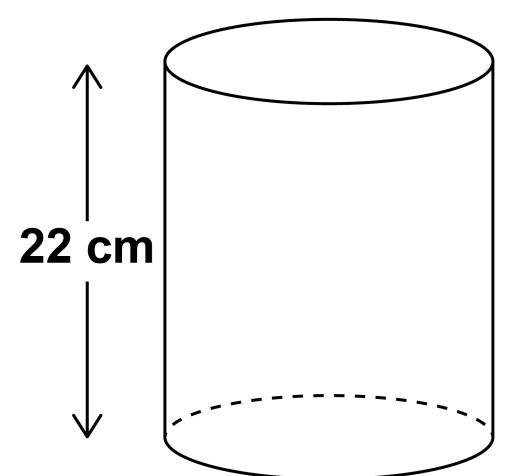


15 A company makes two types of lampshade using fabric on wire frames.

LAMPSHADE A

Fabric is used to make the curved surface of a cylinder.

The cylinder has radius 8 cm and height 22 cm

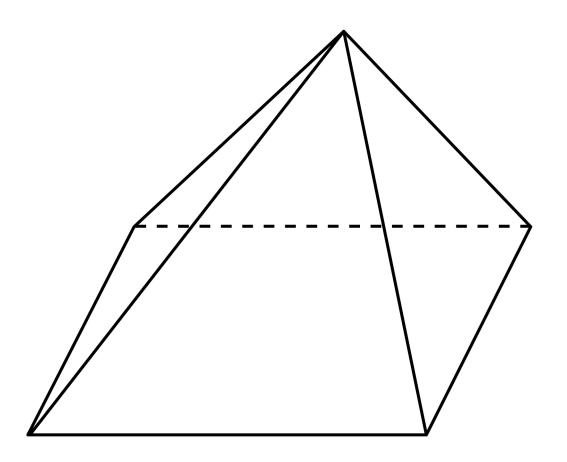






LAMPSHADE B

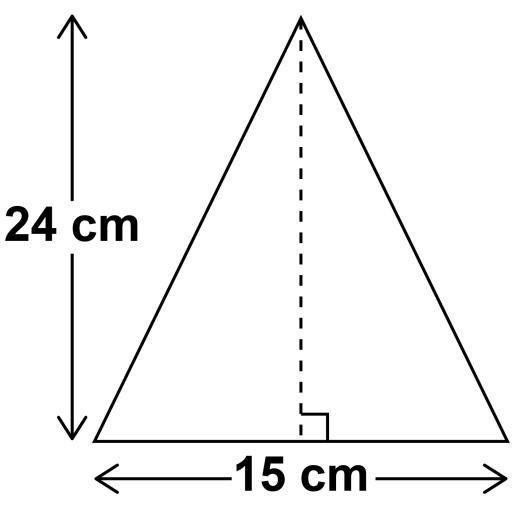
Fabric is used to make the four triangular faces of a pyramid.





Each triangular face has base 15 cm and perpendicular height 24 cm

The diagram is not drawn accurately



Cost of fabric	£400 per square metre
Other costs for A	£3.50 per lampshade
Other costs for B	£7.50 per lampshade



Work out the ratio

cost of one lampshade A : cost of one lampshade B

Give your answer in the form *n* : 1 [5 marks]

Answer

[Turn over]



5

16 In a running club there are 50 females and 80 males.

If a female is chosen at random, the probability she has blue eyes is 0.38

If a male is chosen at random, the probability he has blue eyes is 0.6

One person is chosen at random.

Show that the probability the person has blue eyes is MORE THAN 0.5 [4 marks]



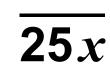
$$17 \quad w = \frac{3}{5\sqrt{x}}$$

Circle the expression for w^2 [1 mark]

$$\frac{6}{10x^2} \qquad \frac{9}{25x^2}$$

10*x*

6



9



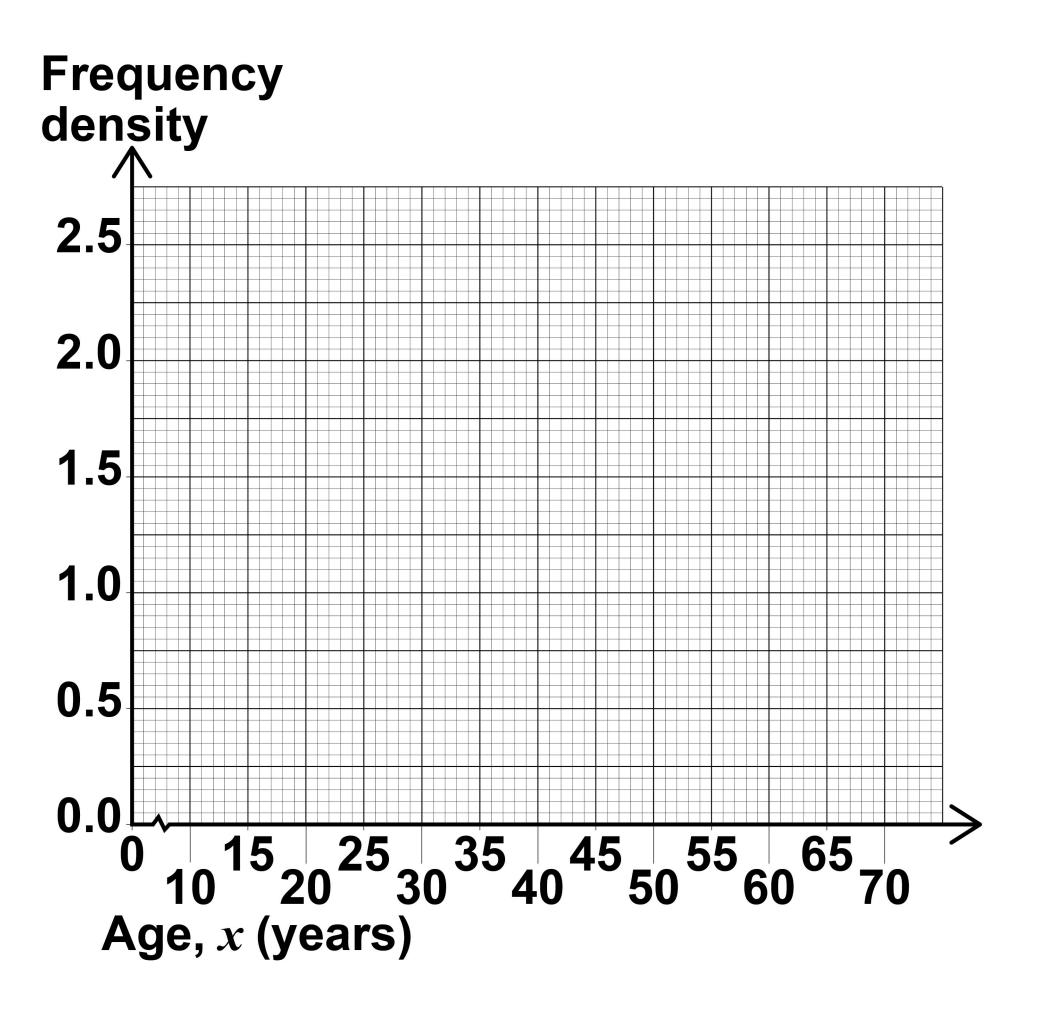
18 Here is some information about the ages of people at a concert.

Age, x (years)	Frequency
10 <i>≤ x <</i> 15	8
15 ≼ <i>x</i> < 25	24
25 <i>≤ x</i> < 40	30
40 ≤ <i>x</i> < 70	39

Draw a histogram, on page 33, to represent the information. [3 marks]



Ages of people at a concert







19 The length of a roll of ribbon is 30 metres, correct to the nearest half-metre.

A piece of length 5.8 metres, correct to the nearest 10 centimetres, is cut from the roll.

Work out the maximum possible length of ribbon left on the roll. [3 marks]



35

Answer metres



20 Curve P has equation $y = 2(x - 1)^2 - 5$

Curve Q is a reflection in the *y*-axis of curve P.

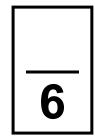
Work out the equation of curve Q.

Give your answer in the form $y = ax^2 + bx + c$ where *a*, *b* and *c* are integers. [3 marks]



Answer

[Turn over]





21 Priya and Joe travel the same 16.8 km route.

Priya starts at 9.00 am and walks at a constant speed of 6 km/h

Joe starts at 9.30 am and runs at a constant speed.

Joe overtakes Priya at 10.20 am

At what time does Joe finish the route? [5 marks]



	39		
Answer _			

[Turn over]



22 An approximate solution to an equation is found using the iterative formula

$$x_{n+1} = \frac{(x_n)^3 - 2}{10}$$
 with $x_1 = -1$

22 (a) Work out the values of x_2 and x_3 [2 marks]

*x*₂ *x*₃ =



22 (b) Work out the solution to 5 decimal places. [1 mark]

<i>x</i> =			
over]			8



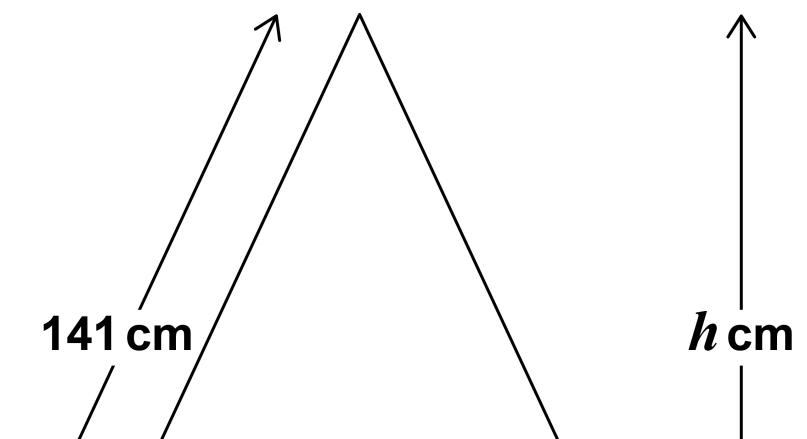
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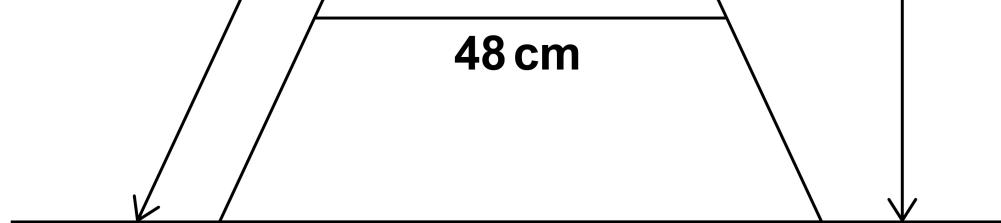
23 The diagram shows the side view of a step ladder with a horizontal strut of length 48 cm

The strut is one third of the way up the ladder.

The symmetrical cross section of the ladder shows two similar triangles.

The diagram is not drawn accurately.







Work out the vertical height, *h* cm, of the ladder. [5 marks]

Answer

cm



44

24

Volume of a sphere = $\frac{4}{3}\pi r^3$ where *r* is the radius Volume of a cone = $\frac{1}{3}\pi r^2 h$ where *r* is the radius and *h* is the perpendicular height

- A sphere has radius 2x cm
- A cone has
- radius 3*x* cm
- perpendicular height h cm
- The sphere and the cone have the same volume.
- Work out radius of cone : perpendicular height of cone

Give your answer in the form *a* : *b* where *a* and *b* are integers. [4 marks]



Answer

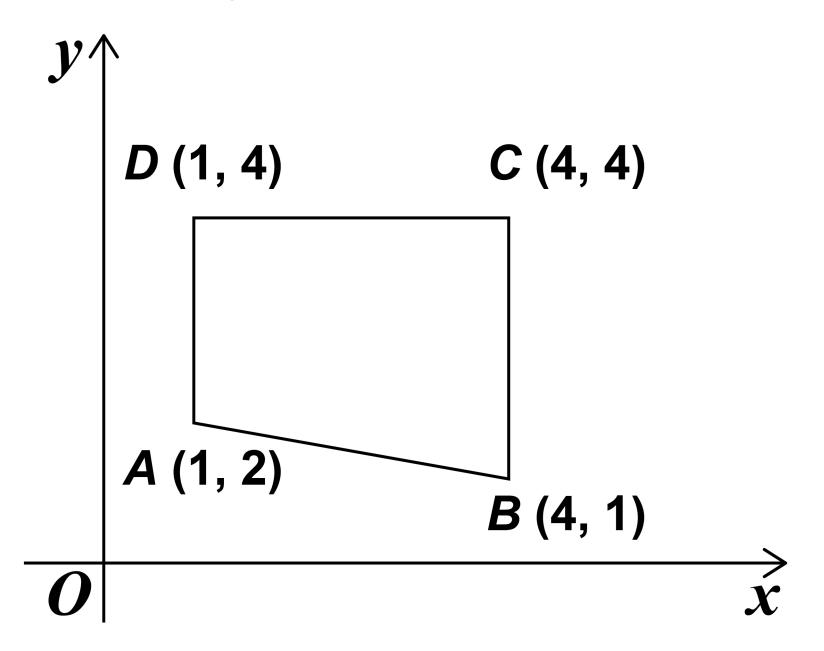
[Turn over]

9



25 *ABCD* is a quadrilateral.

The diagram is not drawn accurately.



The quadrilateral is reflected in the line x = 4



Which vertices are invariant?Circle your answer. [1 mark]A and DC and D

B and CB and D

[Turn over]



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49

26
$$f(x) = \frac{2x+3}{x-4}$$

Work out $f^{-1}(x)$ [4 marks]

Answer

[Turn over]



The line y = 3x + p and the circle $x^2 + y^2 = 53$ intersect at points *A* and *B*.

p is a positive integer.

27 (a) Show that the *x*-coordinates of points *A* and *B* satisfy the equation

 $10x^2 + 6px + p^2 - 53 = 0$ [3 marks]



27 (b) The coordinates of A are (2, 7)

Work out the coordinates of *B*.

You must show your working. [5 marks]



[Continue your answer on page 53]

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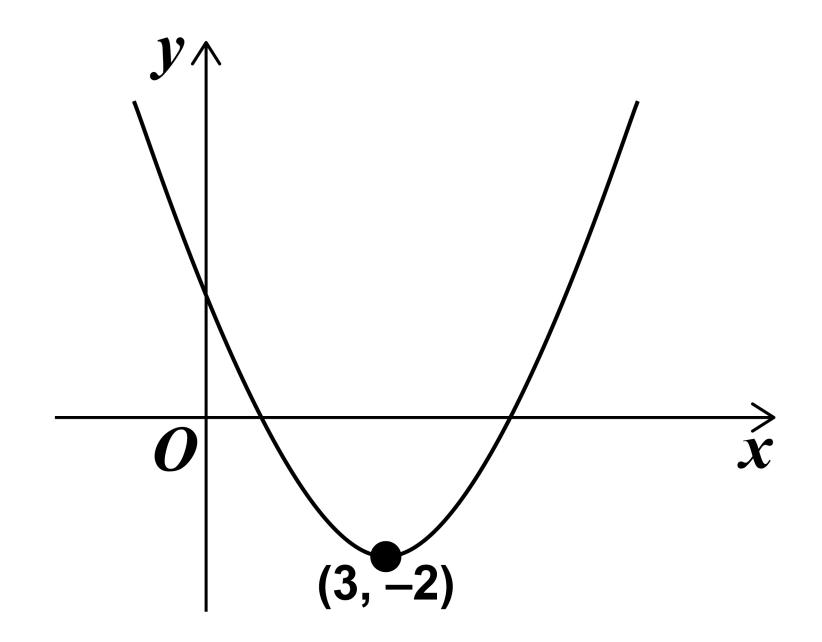
		53		
	Answer(_		,)
[Turn c	over]			8



28 Here is a sketch of a quadratic curve.

The turning point is (3, -2)

The diagram is not drawn accurately.





Circle the correct statement about the gradient of the curve for x < 3 [1 mark]

gradient is positive

gradient is negative

gradient is zero

gradient could be any value

END OF QUESTIONS



There are no questions printed on this page

For Examiner's Use		
Pages	Mark	
4–7		
8–11		
12–15		
16–21		
22–25		
26–29		
30–33		
34–37		
38–41		
42–45		
46–49		
50–53		
54–55		
TOTAL		

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