## AQA

## Surname

Other Names
Centre Number
Candidate Number
Candidate Signature
GCSE
MATHEMATICS


Higher Tier Paper 3 Calculator 8300/3H

Monday 12 November 2018 Morning
Time allowed: 1 hour 30 minutes
At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]

For this paper you must have:

- a calculator
- mathematical instruments.

INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## ADVICE

In all calculations, show clearly how you work out your answer.

## DO NOT TURN OVER UNTIL TOLD TO DO SO

## Answer ALL questions in the spaces provided.

1 A shape is translated by the vector $\binom{0}{4}$
In which direction does the shape move?

Circle your answer. [1 mark]
up
down
left
right

2 What is 1.75 kilometres as a fraction of 700 metres?

Circle your answer. [1 mark]
$\frac{5}{2}$
$\frac{1}{4}$
$\frac{4}{1}$
$\frac{2}{5}$

3 The first 4 terms of a linear sequence are

3


19
27
Circle the expression for the $\boldsymbol{n}$ th term. [1 mark]

$$
\begin{array}{ll}
8-5 n & n+8 \\
8 n+3 & 8 n-5
\end{array}
$$

[Turn over]

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4 Work out the lowest common multiple (LCM) of 20, 30 and 40

Circle your answer. [1 mark] 10 120

240
24000

5 The length of a table is 110 cm to the nearest cm

Complete the error interval. [2 marks]
cm $\leqslant$ length $<$
cm
[Turn over]
6

6 A music festival has taken place each year from 2011

The table shows the number of people who attended each year.

| Year | 2011 | 2012 | 2013 | 2014 |
| :--- | :--- | :--- | :--- | :--- |
| Number of <br> people | 350 | 583 | 906 | 1471 |


| Year | 2015 | 2016 | 2017 | 2018 |
| :--- | :--- | :--- | :--- | :--- |
| Number of <br> people | 2023 | 2612 | 3251 | 3780 |

The festival organisers draw a time series graph to represent the data.

The first four years have been plotted.

6 (a) Complete the graph on page 9. [2 marks]

## Number of people



## [Turn over]

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# 6 (b) Use the graph to estimate the number of people who will attend the festival in 2019 <br> [2 marks] 

## Answer

[Turn over]

## 12

$7 k=n^{2}+9 n+1$

Mo says,

" $k$ will be a prime number for all integer values of $\boldsymbol{n}$ from 1 to 9 "

Show that Mo is wrong.

You MUST show that your value of $k$ is NOT prime. [3 marks]
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## 8 Doug owes an amount of $£ 600$

He wants to pay off this amount in five months.

He says,
"Each month, I will pay back 20\% of the amount I still owe."

## Show working to check if his method is correct. [3 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## 15

[Turn over]


## 9 A motor racing circuit consists of

 two parallel straight sections, each of length 0.75 kma semicircle of diameter 0.9 km three equal, smaller semicircles. The diagram is not drawn accurately.


The length of a motor race must be greater than 305 km

## 17

## What is the lowest number of FULL laps needed at this circuit?

You MUST show your working. [5 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

## [Turn over]

10 Solve $8>3-\frac{1}{2} x \quad$ [2 marks]

## Answer

## 19

## BLANK PAGE

## [Turn over]

20

## 11 Use trigonometry to work out the

 size of angle $x$. [2 marks]The diagram is not drawn accurately.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

degrees

## [Turn over]



22


12 Lewis wants to draw the graph $y=x^{3}$ for values of $x$ from -2 to 2

The graph is on page 22.
Make ONE criticism of his graph. [1 mark]

## [Turn over]

13 The probability of Heads when a biased coin is thrown is $\mathbf{0 . 6}$

The coin is thrown 500 times.
Circle the expected number of Tails. [1 mark]

$$
\begin{array}{llll}
20 & 200 & 250 & 300
\end{array}
$$

14 The mean mass of a squad of 19 hockey players is $\mathbf{8 2} \mathbf{~ k g}$

A player of mass 93 kg joins the squad.

Work out the mean mass of the squad now. [3 marks]
$\qquad$
$\qquad$
$\qquad$

25

## Answer

## kg

## [Turn over]

5

## 15 A company makes two types of

 lampshade using fabric on wire frames.
## LAMPSHADE A

Fabric is used to make the curved surface of a cylinder.

The cylinder has radius 8 cm and height 22 cm


## LAMPSHADE B

## Fabric is used to make the four triangular faces of a pyramid.



## [Turn over]

28

## Each triangular face has base 15 cm and perpendicular height 24 cm

The diagram is not drawn accurately


| Cost of fabric | $£ 400$ per square <br> metre |
| :--- | :--- |
| Other costs for A | $£ 3.50$ per <br> lampshade |
| Other costs for B | $£ 7.50$ per <br> lampshade |

## Work out the ratio

 cost of one lampshade A : cost of one lampshade BGive your answer in the form $n: 1$ [5 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

16 In a running club there are 50 females and 80 males.

If a female is chosen at random, the probability she has blue eyes is 0.38

If a male is chosen at random, the probability he has blue eyes is 0.6

One person is chosen at random.
Show that the probability the person has blue eyes is MORE THAN 0.5 [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$17 w=\frac{3}{5 \sqrt{x}}$

## Circle the expression for $w^{2}$ [1 mark]

6
$\overline{10 x^{2}}$
$\frac{6}{10 x}$
$\frac{9}{25 x}$

## [Turn over]

18 Here is some information about the ages of people at a concert.

| Age, $x$ (years) | Frequency |
| :--- | :--- |
| $10 \leqslant x<15$ | 8 |
| $15 \leqslant x<25$ | 24 |
| $25 \leqslant x<40$ | 30 |
| $40 \leqslant x<70$ | 39 |

Draw a histogram, on page 33, to represent the information.
[3 marks]

## Ages of people at a concert


[Turn over]

34
19 The length of a roll of ribbon is 30 metres, correct to the nearest half-metre.

A piece of length 5.8 metres, correct to the nearest 10 centimetres, is cut from the roll.

Work out the maximum possible length of ribbon left on the roll. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer <br> metres

## [Turn over]

36
20 Curve P has equation

$$
y=2(x-1)^{2}-5
$$

Curve $Q$ is a reflection in the $y$-axis of curve $P$.

Work out the equation of curve $\mathbf{Q}$.
Give your answer in the form $y=a x^{2}+b x+c \quad$ where $a, b$ and $c$ are integers. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## [Turn over]

6

38
21 Priya and Joe travel the same 16.8 km route.

Priya starts at 9.00 am and walks at a constant speed of $6 \mathrm{~km} / \mathrm{h}$

Joe starts at 9.30 am and runs at a constant speed.

Joe overtakes Priya at 10.20 am

## At what time does Joe finish the route? [5 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## [Turn over]

## 40

22 An approximate solution to an equation is found using the iterative formula

$$
x_{n+1}=\frac{\left(x_{n}\right)^{3}-2}{10} \text { with } x_{1}=-1
$$

22 (a) Work out the values of $x_{2}$ and $x_{3}$ [2 marks]

$$
\begin{aligned}
& x_{2}= \\
& x_{3}=
\end{aligned}
$$

$\qquad$

## 22 (b) Work out the solution to 5 decimal places. [1 mark]

$$
x=
$$

## [Turn over]

8

42
23 The diagram shows the side view of a step ladder with a horizontal strut of length 48 cm
The strut is one third of the way up the ladder.

The symmetrical cross section of the ladder shows two similar triangles.
The diagram is not drawn accurately.


# Work out the vertical height, $h \mathbf{c m}$, of the ladder. [5 marks] 

$\qquad$
$\qquad$
$\qquad$
$\qquad$

## 44

24 Volume of a sphere $=\frac{4}{3} \pi r^{3}$ where $r$ is the radius
Volume of a cone $=\frac{1}{3} \pi r^{2} h$ where $r$ is the radius and $h$ is the perpendicular height

A sphere has radius $2 x \mathrm{~cm}$

## A cone has

radius $3 x$ cm
perpendicular height $\boldsymbol{h} \mathbf{c m}$
The sphere and the cone have the same volume.

Work out radius of cone : perpendicular height of cone

Give your answer in the form $a: b$ where $a$ and $b$ are integers. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

## $\square$

## [Turn over]

$25 A B C D$ is a quadrilateral.
The diagram is not drawn accurately.


The quadrilateral is reflected in the line $x=4$

## 47

# Which vertices are invariant? 

# Circle your answer. [1 mark] 

$A$ and $D$

$C$ and $D$

## $B$ and $C$

$B$ and $D$

## [Turn over]

## BLANK PAGE

$26 f(x)=\frac{2 x+3}{x-4}$
Work out $\mathrm{f}^{-1}(x)$ [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

## [Turn over]

27 The line $y=3 x+p$ and the circle $x^{2}+y^{2}=53$ intersect at points $A$ and $B$.
$p$ is a positive integer.
27 (a) Show that the $x$-coordinates of points $A$ and $B$ satisfy the equation $10 x^{2}+6 p x+p^{2}-53=0 \quad$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

27 (b) The coordinates of $A$ are $(2,7)$ Work out the coordinates of $B$. You must show your working. [5 marks]
[Continue your answer on page 53]

## BLANK PAGE

53

## Answer (

## [Turn over]

54
28 Here is a sketch of a quadratic curve.

## The turning point is $(3,-2)$

The diagram is not drawn accurately.


## 55

# Circle the correct statement about the gradient of the curve for $x<3$ <br> [1 mark] 

gradient is positive
gradient is negative
gradient is zero
gradient could be any value

## END OF QUESTIONS

## 56

## There are no questions printed on this page

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
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| $12-15$ |  |
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