

# GCSE MATHEMATICS 8300/3H

Higher Tier Paper 3 Calculator

Mark scheme

November 2018

Version: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| М               | Method marks are awarded for a correct method which could lead to a correct answer.  |
|-----------------|--|
| A               | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| В               | Marks awarded independent of method.   |
| ft              | Follow through marks. Marks awarded for correct working following a mistake in an earlier step.  |
| SC              | Special case. Marks awarded for a common misinterpretation which has some mathematical worth.  |
| M dep           | A method mark dependent on a previous method mark being awarded.   |
| B dep           | A mark that can only be awarded if a previous independent mark has been awarded.   |
| oe              | Or equivalent. Accept answers that are equivalent.   |
|                 | eg accept 0.5 as well as $\frac{1}{2}$   |
| [a, b]          | Accept values between a and b inclusive.   |
| [a, b)          | Accept values a ≤ value < b  |
| 3.14            | Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416   |
| Use of brackets | It is not necessary to see the bracketed work to award the marks.  |

Examiners should consistently apply the following principles

# **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

#### Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

#### Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

# Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### **Further work**

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

# Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

# Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

#### Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the student intended it to be a decimal point.

| Question              | Answer                        | Mark        | Comme                  | nts  |
|-----------------------|-------------------------------|-------------|------------------------|------|
|                       | up                            | B1          |                        |      |
| 1                     | Ac                            | Iditional G | uidance                |      |
|                       |                               |             |                        |      |
|                       | 5                             | D4          |                        |      |
| 2                     | <u>5</u><br>2                 | B1          |                        |      |
| 2                     | Ac                            | lditional G | uidance                |      |
|                       |                               |             |                        |      |
|                       | 8 <i>n</i> – 5                | B1          |                        |      |
| 3 Additional Guidance |                               |             | uidance                |      |
|                       |                               |             |                        |      |
|                       | 120                           | B1          |                        |      |
| 4                     | Ac                            | Iditional G | uidance                |      |
|                       |                               |             |                        |      |
|                       | 109.5 in the correct position | B1          | oe                     |      |
|                       | 110.5 in the correct position |             | oe                     |      |
|                       |                               | B1          | •<br>Allow 110.49      |      |
| 5                     |                               |             | answers reversed score | B0B1 |
|                       | Ac                            | lditional G | Buidance               |      |
|                       | 110.4999                      |             |                        | B1   |
|                       | 110.4999                      |             |                        | В0   |

| Question | Answer  | Mark       | Commer   | nts           |
|----------|---|------------|--|---------------|
|          | Plots at least 3 points correctly                 | M1         | Plots within the correct square                            | 2 mm vertical |
| 6(a)     | Fully correct with all points joined              | A1         |  |               |
|          | Ado   | ditional G | uidance  |               |
|          |   |            |  |               |
|          |   |            | B1   |               |
|          | [4200, 4500]                                      | B2         | Any indication the 2018 figure is being increased for 2019 |               |
|          |   |            | eg a point plotted for 2019 that is greater than 3780      |               |
| 24.      | Ado   | ditional G | uidance  |               |
| 6(b)     | Answer in range with or without worki             | ng         |  | B2            |
|          | 4300 – 4350 on answer line (both values in range) |            |  | B2            |
|          | 4400 – 4600 on answer line (one value in range)   |            | e)   | B1            |
|          | Answer outside of range but between 3780 and 4200 |            |  | B1            |
|          | Answer outside of range but greater t             | han 4500   |  | B1            |

| Question | Answer  | Mark     | Comme                   | nts           |
|----------|---|----------|-------------------------|---------------|
|          | Any correct value   | M1       | 11, 23, 37, 53, 71, 91, | 113, 137, 163 |
|          | Selects 91 as the only incorrect value with no errors in values given   | A1       | oe<br>eg stops at 91    |               |
|          | 91 and 13 (is a factor) or 91 and 7 (is a factor) or 91 and 13 × 7  | A1       | oe<br>eg 91 ÷ 7 = 13    |               |
| 7        | Additional Guidance   |          |                         |               |
|          | Ignore incorrect evaluations for first m  | ark      |                         |               |
|          | Ignore all values for $n$ greater than 9  |          |                         |               |
|          | Do not allow 11 within a list of prime n  | umbers e | g 2, 3, 5, 7, 11        |               |
|          | Error in list eg 12, 23, 37, 53, 71, 91, selected as not prime (not valid as inc  | M1A0A0   |                         |               |
|          | Error in list eg 12, 23, 37, 53, 71, 91, 113, 137, 163 with only 91 selected as not prime (not valid as incorrect conclusion from their list) |          |                         | M1A0A0        |
|          | $9^2 + 9 + 1 = 91$ is incorrect working   |          |                         | M0A0A0        |

| Question | Answer   | Mark  | Comments                                 |  |  |
|----------|--|-------|--|--|--|
|          | Alternative method 1   |       |  |  |  |
|          | (600 ×) 0.8 or 480   | M1    | oe                                       |  |  |
|          | $600 \times 0.8^2$ or $384$<br>or $600 \times 0.8^3$ or $307.2(0)$<br>or $600 \times 0.8^4$ or $245.76$<br>or $600 \times 0.8^5$ or $[196, 197]$                               | M1dep |  |  |  |
|          | [196, 197] and incorrect   | A1    | oe eg 196.61 and no<br>196.61 still owed |  |  |
|          | Alternative method 2   |       |  |  |  |
|          | 600 × 0.2 or 120   | M1    | oe                                       |  |  |
| 8        | 120 × 0.8 or 96<br>or 96 × 0.8 or 76.8(0)<br>or 76.8(0) × 0.8 or 61.44<br>or 61.44 × 0.8 or [49.15, 49.16]   | M1dep | oe eg (600 – 120) × 0.2<br>or 480 × 0.2  |  |  |
|          | [403, 404] and incorrect   | A1    | oe eg paid off 403.39(2)                 |  |  |
|          | Alternative method 3   |       |  |  |  |
|          | 0.8  | M1    |  |  |  |
|          | 0.8 <sup>5</sup> or 0.327 68 or 0.3277<br>or 0.328 or 0.33   | M1dep |  |  |  |
|          | 0.327 68 (or 0.3277 or 0.328 or 0.33) and incorrect  | A1    | oe                                       |  |  |
|          | Additional Guidance  |       |  |  |  |
|          | Ignore units   |       |  |  |  |
|          | Full marks can be awarded for a correct explanation eg 120 and 96 calculated with a comment 'as soon as the payment is below 120 a month it cannot be paid off in five months' |       |  |  |  |

| Question | Answer  | Mark        | Comme   | nts  |
|----------|---|-------------|---|------|
|          | $0.9 \times \pi \div 2 \text{ or } 0.9\pi \div 2 \text{ or } 0.45\pi$<br>or $0.9 \times [3.14, 3.142] \div 2$<br>or $[2.82, 2.83] \div 2$ or $2.8 \div 2$<br>or $1.4$ | M1          | Large semicircle  |      |
|          | $0.9 \div 3 \times \pi \div 2 \text{ or } 0.3\pi \div 2$<br>or $0.15\pi$<br>or $0.9 \div 3 \times [3.14, 3.142] \div 2$<br>or $0.94 \div 2$<br>or $0.47$              | M1          | Small semicircle  May be implied from usi small semicircles in next |      |
| 9        | their 1.4 + 3 × their 0.47 + 2 × 0.75  or $0.9\pi + 2 \times 0.75$ or 2 × their 1.4 + 2 × 0.75  | M1dep       | oe<br>dep on both marks   |      |
|          | or 4.3 305 ÷ their 4.3 or [70.4, 70.94] 71 with working   | M1dep       | dep on previous mark  |      |
|          | Ac  | lditional G | Guidance  |      |
|          | $0.9\pi$ or $2.8$ with no evidence of in  | ncorrect me | ethod   | M1M1 |
|          | 0.45π ÷ 2   |             |   | MO   |

| Question | Answer  | Mark             | Commen     | S    |
|----------|---|------------------|------------|------|
|          | Alternative method 1  |                  |            |      |
|          | $\frac{1}{2}x > 3 - 8$ or $\frac{1}{2}x > -5$ or $8 - 3 > -\frac{1}{2}x$ or $5 > -\frac{1}{2}x$ or $8 + \frac{1}{2}x > 3$ | M1               | oe         |      |
| 10       | x > -10   | A1               | oe -10 < x |      |
|          | Alternative method 2  |                  |            |      |
|          | 16 > 6 - x<br>or $16 - 6 > -x$<br>or $10 > -x$<br>or $x > 6 - 16$<br>or $16 + x > 6$                                      | M1               | oe         |      |
|          | x > -10   | A1               | oe -10 < x |      |
|          | Ad  | ditional G       | uidance    |      |
|          | Answer using incorrect sign eg $x < -x$   | 10 or <i>x</i> = | -10        | M1A0 |

| Question | Answer   | Mark       | Commer  | nts  |
|----------|--|------------|---|------|
|          | $\cos x = \frac{9}{10}$                            | M1         | oe<br>eg<br>$\sin x = \frac{\sqrt{10^2 - 9^2}}{10}$<br>$\tan x = \frac{\sqrt{10^2 - 9^2}}{9}$ |      |
| 11       | 25.8 or 26   | A1         |   |      |
|          | Add  | ditional G | uidance   |      |
|          | $\cos = \frac{9}{10} x = 25.8 \text{ (recovered)}$ |            |   | M1A1 |
|          | $\cos = \frac{9}{10}$                              |            |   | M0A0 |
| 12       | Graph should be a curve                            | B1         | oe eg Should not be straight lir Not a curve Not smooth Too straight Need more points plotte  |      |
|          | Additional Guidance                                |            |   |      |
|          |  |            |   |      |
|          | 200  | B1         |   |      |
| 13       |  | ditional G | Guidance  |      |
|          |  |            |   |      |

| Question | Ans   | wer   | Mark       | Comn  | nents                              |
|----------|---|---|------------|---|------------------------------------|
|          | 19 × 82 or 1558   |   | M1         |   |                                    |
|          | $\frac{\text{their } 1558 + 93}{20}  \text{or}  \frac{1651}{20}$                              |   | M1dep      | oe  |                                    |
| 14       | 82.55 or 82.6   |   | A1         |   |                                    |
|          |   | Ad  | ditional G | Guidance  |                                    |
|          |   |   |            |   |                                    |
|          | $2 \times \pi \times 8 \times 22$ or [1105, 1106]   | r 352π  | M1         | Area of lampshade A oe $2 \times \pi \times 0.08 \times 0.22$ or [0.1105, 0.1106] | or $0.0352\pi$                     |
|          | $4 \times \frac{1}{2} \times 15 \times 24$ or 720   |   | M1         | Area of lampshade B oe $4 \times \frac{1}{2} \times 0.15 \times 0.24$             | or 0.072                           |
| 15       | their $352\pi \div 100^2 \times 400$<br>or $14.08\pi$<br>or $[44.2, 44.24]$                   | their 720 ÷ 100 <sup>2</sup> × 400 or 28.8(0) | M1dep      | their $0.0352\pi \times 400$ or $14.08\pi$ or $[44.2, 44.24]$                     | their 0.072 × 400<br>or<br>28.8(0) |
|          |   |   |            | dep on 1st M1   | dep on 2nd M1                      |
|          | their $14.08\pi + 3.50$<br>or $[47.7, 47.74]$<br>and<br>their $28.8(0) + 7.5(0)$ or $36.3(0)$ |   | M1dep      | dep on M3 and metho<br>both lampshades corr                                       |                                    |
|          | 1.3(1):1 or 1   | 1.32 : 1                                      | A1         |   |                                    |
|          |   | Ad  | ditional G | Guidance  |                                    |
|          | 1 : 1.3(1) or   | 1 : 1.32                                      |            |   | M4A0                               |

| Question | Answer  | Mark  | Comments |  |  |
|----------|---|-------|----------|--|--|
|          | Alternative method 1  |       |          |  |  |
|          | 0.38 × 50 or 19   | M1    | oe       |  |  |
|          | 0.6 × 80 or 48  | M1    | oe       |  |  |
|          | their 19 + their 48 $50 + 80$ or $\frac{67}{130}$   | M1dep | oe       |  |  |
|          | 0.51(5) or 0.52<br>or $\frac{67}{130}$ and $(67 \times 2 =) 134$<br>or $\frac{67}{130}$ and $(130 \div 2 =) 65$ | A1    | oe       |  |  |
|          | Alternative method 2  |       |          |  |  |
| 16       | 0.38 × 50 or 19   | M1    | oe       |  |  |
|          | 0.6 × 80 or 48  | M1    | oe       |  |  |
|          | 0.5 × (50 + 80) or 65   | M1dep | oe       |  |  |
|          | 65 and 67   | A1    |          |  |  |
|          | Alternative method 3  |       |          |  |  |
|          | 0.38 × 50 or 19   | M1    | oe       |  |  |
|          | 0.5 × (50 + 80) or 65   | M1    | oe       |  |  |
|          | $\frac{\text{their } 65 - \text{their } 19}{80}$ or $\frac{46}{80}$   | M1dep | oe       |  |  |
|          | 0.575   | A1    |          |  |  |

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| Question | Answer  | Mark       | Comments |  |
|----------|---|------------|----------|--|
|          | Alternative method 4  |            |          |  |
|          | 0.6 × 80 or 48  | M1         | oe       |  |
|          | 0.5 × (50 + 80) or 65   | M1         | oe       |  |
|          | $\frac{\text{their } 65 - \text{their } 48}{50}$ or $\frac{17}{50}$ | M1dep      | oe       |  |
|          | 0.34  | A1         |          |  |
|          | Alternative method 5  |            |          |  |
| 16 cont  | $\frac{50}{130}$ × 0.38 or 0.14 or 0.15                             | M1         | oe       |  |
|          | $\frac{80}{130}$ × 0.6 or 0.36 or 0.37                              | M1         | oe       |  |
|          | their 0.14 + their 0.36   | M1dep      | oe       |  |
|          | 0.51(5) or 0.52   | A1         |          |  |
|          | Ad  | ditional G | Guidance |  |
|          |   |            |          |  |
|          | ۵   |            |          |  |
|          | $\frac{9}{25x}$   | B1         |          |  |
| 17       | Additional Guidance   |            |          |  |
|          |   |            |          |  |

| Question | Answer   | Mark     | Comments                           |  |
|----------|--|----------|------------------------------------|--|
|          | Any one of<br>8 ÷ 5 or 1.6<br>or<br>24 ÷ 10 or 2.4<br>or<br>30 ÷ 15 or 2<br>or<br>39 ÷ 30 or 1.3 | M1       | Implied by a correct bar           |  |
|          | At least three of<br>1.6 and 2.4 and 2 and 1.3   | M1dep    | Implied by three correct bars      |  |
|          | Fully correct histogram  | A1       | Tolerance $\pm \frac{1}{2}$ square |  |
| 18       | ignore frequency polygon if drawn  Additional Guidance   |          |                                    |  |
|          | 2.5  2.0  Frequency density  1.5  0.0  0 10 15 20 25 30 35 40 Age, x (y                          | 45 50 55 | 3 marks                            |  |

| Question | Answer                                  | Mark         | Commer  | nts    |
|----------|---|--------------|---|--------|
|          | 30.25<br>or 29.75<br>or 5.85<br>or 5.75 | B1           |   |        |
| 19       | their 30.25 – their 5.75                | M1           | Must be their max roll – their max must be (30, 3 their min must be [5.5, 5 | 0.5]   |
|          | 24.5                                    | A1           |   |        |
|          |   | Additional G | uidance   |        |
|          | 30.5 – 5.75 = 24.75                     |              |   | B1M1A0 |

|    | Alternative method 1   |       |                            |           |  |
|----|--|-------|----------------------------|-----------|--|
|    | $2(-x-1)^2-5$  | M1    | oe                         |           |  |
|    |  |       | Replacing x with –x        |           |  |
|    | $2(x^2 + x + x + 1) - 5$   |       | oe expansion               |           |  |
|    | or $2x^2 + 4x + 2 - 5$   | M1dep |                            |           |  |
|    | or $2x^2 + 4x - 3$   |       |                            |           |  |
|    | $y = 2x^2 + 4x - 3$  | A1    |                            |           |  |
| 00 | Alternative method 2   |       |                            |           |  |
| 20 | $2(x^2 - x - x + 1) - 5$   |       | oe expansion               |           |  |
|    | or $2x^2 - 4x + 2 - 5$   | M1    | Multiplying out original e | xpression |  |
|    | or $2x^2 - 4x - 3$   |       |                            |           |  |
|    | $2(-x)^2 - 4(-x) - 3$  |       | oe                         |           |  |
|    | or $2x^2 + 4x - 3$   | M1dep | Replacing $x$ with $-x$    |           |  |
|    | $y = 2x^2 + 4x - 3$  | A1    |                            |           |  |
|    | Additional Guidance  |       |                            |           |  |
|    | Using symmetry in y axis, $y = 2(x + 1)^2 - 5 \rightarrow y = 2x^2 + 4x - 3$ |       |                            | M1M1A1    |  |

| Question | Answer   | Mark        | Commer                         | nts              |
|----------|--|-------------|--------------------------------|------------------|
|          | 1(h) 20 (min) and 50 (min) or $1\frac{20}{60}$ (h) or $1\frac{1}{3}$ (h) or 1.33(h) or $\frac{50}{60}$ (h) or $\frac{5}{6}$ (h) or 0.83(h)                     | B1          | oe<br>Journey time(s) at 10.20 | am               |
|          | $6 \times \text{their } 1\frac{1}{3} \text{ or } 8$  | M1          | oe Priya's distance at 10      | ).20 am          |
|          | their 8 ÷ their $\frac{50}{60}$ or 9.6   | M1dep       | oe Joe's speed in km/h         |                  |
|          | or 16.8 ÷ 8 or 2.1   |             | Multiplier for distance co     | mparison         |
|          | 16.8 ÷ their 9.6 or 1.75(h)  |             | oe                             |                  |
|          | or 1(h) 45 (min) or 105 (min)  |             | Joe's total journey time       |                  |
| 21       | or $16.8 \div 8 \times 50 \ (\div 60)$ or $\frac{16.8 - \text{their } 8}{\text{their } 9.6}  \text{or}  \frac{8.8}{\text{their } 9.6}$                         | M1dep       | Joe's journey time after       | overtaking Priya |
|          | or 0.91(6)(h) or 0.917(h)<br>or 0.92(h) or 55(min)   |             |                                |                  |
|          | 11.15 (am)   | A1          | oe eg quarter past 11 (i       | n the morning)   |
|          | Ac   | Iditional ( | Guidance                       |                  |
|          | If 11.15 comes from correct method but with premature rounding eg 8 ÷ 0.83 = 9.64 16.8 ÷ 9.64 = 1.743 h 1.743 × 60 = 104.58 minutes ie 11 : 14 : 58 so 11 : 15 |             |                                | B1M3A0           |
|          | 8 km implies   |             | B1M1                           |                  |
|          | 16.8 ÷ 6 or 2.8 with no further valid working  |             |                                | ВОМО             |

| Answer   | Mark  | Comments  |   |  |  |  |
|--|---|---|---|--|--|--|
|  |   |   |   |  |  |  |
| $-0.3 \text{ or } -\frac{3}{10}$                               | B1  |   |   |  |  |  |
| $-0.2027$ or $-\frac{2027}{10000}$                             | B1ft  | ft their –0.3   |   |  |  |  |
| Additional Guidance  |   |   |   |  |  |  |
| ft answer must be to at least 4 decimal places                 |   |   |   |  |  |  |
| Note: if their –0.3 is –0.2027, then ft answer is –0.200 832 8 |   |   |   |  |  |  |
|  | $-0.3 \text{ or } -\frac{3}{10}$ $-0.2027 \text{ or } -\frac{2027}{10000}$ Add  ft answer must be to at least 4 decim | $-0.3 \text{ or } -\frac{3}{10}$ $-0.2027 \text{ or } -\frac{2027}{10000}$ B1ft  Additional G  ft answer must be to at least 4 decimal places | $-0.3 \text{ or } -\frac{3}{10}$ $-0.2027 \text{ or } -\frac{2027}{10000}$ $B1 \text{ ft their } -0.3$ $Additional Guidance$ $ft answer must be to at least 4 decimal places$ |  |  |  |

|       | -0.20081                            | B1 |  |  |
|-------|-------------------------------------|----|--|--|
| 22/6) | Additional Guidance                 |    |  |  |
| 22(b) | Answer must be to exactly 5 decimal |    |  |  |
|       | -0.20083                            |    |  |  |

|    | Alternative method 1   |       |  |  |
|----|--|-------|--|--|
|    | 48 ÷ 2 × 3 or 72   | M1    | oe   |  |
|    | their 72 ÷ 2 or 36   | M1dep | $\cos^{-1}\left(\frac{36}{141}\right)$ or 75.2   |  |
| 23 | 141 <sup>2</sup> – their 36 <sup>2</sup> or 18 585           | M1dep | ft their base ÷ 2<br>sin (their 75.2) = $\frac{h}{141}$<br>or tan (their 75.2) = $\frac{h}{\text{their 36}}$ |  |
|    | $\sqrt{141^2 - \text{their } 36^2} \text{ or } \sqrt{18585}$ | M1dep | 141 × sin (their 75.2)<br>or their 36 × tan (their 75.2)   |  |
|    | [136.2, 136.4] or 136  | A1    |  |  |

# **Continues on next page**

| Question | Answer   | Mark        | Comments   |  |  |
|----------|--|-------------|--|--|--|
|          | Alternative method 2   |             |  |  |  |
|          | 141 ÷ 3 or 47  | M1          | oe   |  |  |
|          | 24 and their 47 × 2<br>or 24 and 94<br>or 12 and their 47  | M1dep       | $\cos^{-1}\left(\frac{24}{94}\right)$ or 75.2  |  |  |
| 23 cont  | their $94^2 - 24^2$ or 8260<br>or $\sqrt{8260}$<br>or 90.88<br>or their $47^2 - 12^2$ or 2065<br>or $\sqrt{2065}$<br>or 45.44  | M1dep       | $\sin (\text{their } 75.2) = \frac{h}{\text{their } 94}$ or $\tan (\text{their } 75.2) = \frac{h}{24}$ |  |  |
|          | $\sqrt{\text{their } 94^2 - 24^2} \times 3 \div 2$ or $\sqrt{8260} \times 3 \div 2$ or 90.88 × 3 ÷ 2 or $\sqrt{\text{their } 47^2 - 12^2} \times 3$ or $\sqrt{2065} \times 3$ or 45.44 × 3 | M1dep       | their 94 × sin (their 75.2) × 3 ÷ 2<br>or 24 × tan (their 75.2) × 3 ÷ 2                                |  |  |
|          | [136.2, 136.35] or 136   | A1          |  |  |  |
|          | Ac   | Iditional C | Guidance   |  |  |
|          | Values may be seen on diagram in correct positions   |             |  |  |  |

| Question | Answer   | Mark          | Commen                       | ts         |
|----------|--|---------------|------------------------------|------------|
|          | $\frac{4}{3}\pi(2x)^3$ or $\frac{1}{3}\pi(3x)^2h$  | M1            | oe                           |            |
|          | $\frac{4}{3}\pi(2x)^3 = \frac{1}{3}\pi(3x)^2h$ or $\frac{4}{3}\pi 8x^3 = \frac{1}{3}\pi 9x^2h$   | M1dep         | oe<br>Sets up equation       |            |
| 24       | $32x = 9h$ or $x = \frac{9}{32}h$<br>or $h = \frac{32}{9}x$<br>or $\frac{32}{3}r = 9h$ or $r = \frac{27}{32}h$<br>or $h = \frac{32}{27}r$ or $27h = 32r$ | M1dep         | oe linear equation or ration | 0          |
|          | or $\frac{27}{32}h:h$ or $3x:\frac{32}{9}x$ or $\frac{27}{32}:1$ or $3:\frac{32}{9}$ or $0.84:1$ or $3:3.55$   |               |                              |            |
|          | 27 : 32  | A1 ditional G | uidanee                      |            |
|          | 32 : 27  | unional G     | uluance                      | M1M1M1A0   |
|          | Note $\frac{4}{3}\pi(2)^3 = [33.49, 33.52]$ $\frac{1}{3}\pi(3)^2h = [9.42h, 9.43h]$  |               |                              | WIWIIWITAO |

| Answer   | Mark   | Commer  | nts   |  |
|--|--|---|---|--|
| B and C  | B1   |   |   |  |
| Ad   | ditional G   | uidance   |   |  |
| y(x-4) = 2x + 3  | M1   | x(y-4) = 2y + 3   |   |  |
| yx - 4y = 2x + 3   | M1dep  | xy - 4x = 2y + 3  |   |  |
| yx - 2x = 4y + 3<br>or $x(y - 2) = 4y + 3$<br>or $x = \frac{4y + 3}{y - 2}$  | M1dep  | xy - 2y = 4x + 3<br>or $y(x - 2) = 4x + 3$  |   |  |
| $\frac{4x+3}{x-2}$   | A1   | oe Must be in terms of $x$  |   |  |
| Additional Guidance  |  |   |   |  |
| Ignore any attempt to give the domain  | of f <sup>-1</sup>   |   |   |  |
| $x^2 + (3x + p)^2 = 53$  | M1   | oe  |   |  |
| $9x^2 + 3xp + 3xp + p^2$<br>or $9x^2 + 6xp + p^2$  | M1   | Expands $(3x + p)^2$ correct  | ctly  |  |
| $x^{2} + (3x + p)^{2} = 53$<br>and $x^{2} + 9x^{2} + 3xp + 3xp + p^{2} = 53$<br>and $10x^{2} + 6px + p^{2} - 53 = 0$<br>or<br>$x^{2} + (3x + p)^{2} = 53$<br>and $x^{2} + 9x^{2} + 6xp + p^{2} = 53$<br>and $10x^{2} + 6px + p^{2} - 53 = 0$ | A1   |   |   |  |
| Additional Guidance  |  |   |   |  |
|  |  |   |   |  |
|  | Ad<br>$y(x-4) = 2x + 3$ $yx - 4y = 2x + 3$ $yx - 2x = 4y + 3$ or $x(y-2) = 4y + 3$ or $x = \frac{4y+3}{y-2}$ Ad<br>Ignore any attempt to give the domain $x^2 + (3x + p)^2 = 53$ $9x^2 + 3xp + 3xp + p^2$ or $9x^2 + 6xp + p^2$ $x^2 + (3x + p)^2 = 53$ and $x^2 + 9x^2 + 3xp + 3xp + p^2 = 53$ and $10x^2 + 6px + p^2 - 53 = 0$ or $x^2 + (3x + p)^2 = 53$ and $10x^2 + 6px + p^2 - 53 = 0$ or $x^2 + (3x + p)^2 = 53$ and $10x^2 + 6px + p^2 - 53 = 0$ | Additional G $y(x-4) = 2x + 3$ $yx - 4y = 2x + 3$ $yx - 2x = 4y + 3$ or $x(y-2) = 4y + 3$ or $x = \frac{4y + 3}{y - 2}$ Algore any attempt to give the domain of $f^{-1}$ $x^2 + (3x + p)^2 = 53$ $2x^2 + (3x + p)^2 = 53$ and $x^2 + 9x^2 + 3xp + 3xp + p^2$ or $y^2 + 6xp + p^2$ $x^2 + (3x + p)^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp + 3xp + 3xp + 3xp + p^2 = 53$ and $y^2 + 3xp +$ | Additional Guidance $y(x-4) = 2x + 3$ $yx - 4y = 2x + 3$ $yx - 2x = 4y + 3$ $or x(y-2) = 4y + 3$ $or x = \frac{4y + 3}{y - 2}$ $\frac{4x + 3}{x - 2}$ All oe Must be in terms of $x$ Additional Guidance  Ignore any attempt to give the domain of $f^{-1}$ $x^2 + (3x + p)^2 = 53$ $and x^2 + 9x^2 + 3xp + 3xp + p^2 = 53$ $and 10x^2 + 6px + p^2 = 53$ and $10x^2 + 6px + p^2 = 53$ |  |

| Question | Answer   | Mark      | Commer  | nts               |
|----------|--|-----------|---|-------------------|
|          | $7 = 3 \times 2 + p$ or $7 = 6 + p$ or $p = 1$   | M1        | oe<br>Substitutes $x = 2$ into give<br>$10(2)^2 + 6p(2) + p^2 - 53$<br>or $p^2 + 12p - 13 = 0$<br>or $(p-1)(p+13)$<br>or $p = 1$ (and $p = -13$ ) |                   |
|          | $10x^{2} + 6x + 1 - 53 = 0$<br>or $10x^{2} + 6x - 52 = 0$<br>or $5x^{2} + 3x - 26 = 0$   | M1dep     | oe equation Substitutes their $p$ into $g$  | iven equation     |
|          | $(5x + 13)(x - 2)$ or $\frac{-3 \pm \sqrt{3^2 - 4 \times 5 \times -26}}{2 \times 5}$ or $-\frac{3}{10} \pm \sqrt{\frac{529}{100}}$     | M1        | oe Correct factorisation of t quadratic or correct substitution in 3-term quadratic or correct completion of expression for $x$                   | formula for their |
| 27(b)    | (x =) -2.6   | A1        | oe  |                   |
|          | (-2.6, -6.8)   | A1        | oe  |                   |
|          | Additional Guidance  |           |   |                   |
|          | After scoring first M1, they substitute $(p-1)(p+13)$ or $p=1$ (and $p=-13$ )  | e p = -13 |   | M1                |
|          | $10x^{2} - 78x + 169 - 53 = 0$ or $10x^{2} - 78x + 116 = 0$ or $5x^{2} - 39x + 58 = 0$   |           |   | M1dep             |
|          | $(5x - 29)(x - 2)$ or $\frac{-39 \pm \sqrt{(-39)^2 - 4 \times 5 \times 58}}{2 \times 5}$ or $\frac{39}{10} \pm \sqrt{\frac{361}{100}}$ |           |   | M1dep<br>A0 A0    |

| Question | Answer               | Mark       | Comments |
|----------|----------------------|------------|----------|
|          | gradient is negative | B1         |          |
| 28       | Ad                   | ditional G | uidance  |
|          |                      |            |          |