

## **Cambridge International Examinations**

Cambridge International General Certificate of Secondary Education

MATHEMATICS (US) 0444/43

Paper 4 (Extended)

October/November 2016

MARK SCHEME

Maximum Mark: 130

## **Published**

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## **Abbreviations**

correct answer only cao

dep

dependent
follow through after error
ignore subsequent working
or equivalent FTisw

oe SC

Special Case not from wrong working nfww

seen or implied soi

	Question	Answer	Mark	Part marks
1	(a)	Triangle drawn at (-4, 3), (-1, 3), (-1, 4)	2	SC1 for correct reflection in $x = k$ or $y = 1$
	(b)	Triangle drawn at (1, 7), (1, 6), (4, 6)	2	<b>SC1</b> for translation by $\binom{-2}{k}$ or $\binom{k}{3}$
	(c)	Triangle drawn at (2, 3), (2, 1), (8, 1)	2	
	(d)	Rotation	1	
		90° clockwise oe	1	Accept –90°
		(7, 4)	1	

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	Question	Answer	Mark	Part marks
2	(a) (i)	1050	2	M1 for 924 ÷ 22 oe or 924 ÷ 0.88 oe If zero scored, SC1 for 126 seen
	(ii)	12	1	
	(iii)	$5\frac{1}{4}$ hrs or 5.25 hrs	2	M1 for $9 \div (7+5)$ or $540 \div (7+5)$ If zero scored, SC1 for answer 3.75h or 3h 45 mins
	(b)	24.6[0]	3	<b>M2</b> for 15.99 ÷ $\left(1 - \frac{35}{100}\right)$ oe or <b>M1</b> for 65% associated with 15.99
	(c)	63	3	<b>M2</b> for $35 \times \sqrt{\frac{2835}{875}}$ oe
				or <b>M1</b> for $\sqrt{\frac{2835}{875}}$ or $\sqrt{\frac{875}{2835}}$ or better
				or $\frac{\sqrt{2835}}{?} = \frac{\sqrt{875}}{35}$ oe
				OR
				<b>M2</b> for $\sqrt{2835 \times \frac{35}{their(875 \div 35)}}$ oe
				or
				<b>M1</b> for $\frac{35}{their(875 \div 35)}$ or $\frac{their(875 \div 35)}{35}$
	(d) (i)	0.661[0]	1	
	(ii)	48	3	<b>M2</b> for $\frac{18.50 - 12.50}{12.50} \times 100$
				or <b>M1</b> for $\frac{18.50 - 12.50}{12.50}$ or $\frac{18.50}{12.50} \times 100$

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	Question	Answer	Mark	Part marks
3	(a)	-4.5 and 10.5	2	B1 for each value
	(b)	Correct curve	5	B4 for correct curve with branches joined OR B3 FT for 9 or 10 points or B2 FT for 7 or 8 points or B1 FT for 5 or 6 points and B1 independent for one branch on each side of the y-axis and not touching or crossing the y-axis
	(c)	5	1	
	(d) (i)	Line $y = 15 - 3x$ ruled and -0.4 to $-0.310.35$ to $0.452.2$ to $2.3$	4	B3 for correct line and 2 correct values or B2 for correct line or M1 for ruled line with gradient –3 or through (0, 15) or SC2 for no/wrong line and three correct values or SC1 for no/wrong line and two correct values or for correct freehand line
	(ii)	[a =] 6 [b =] -14 [c =] 0	3	<b>B2</b> for $6x^3 - 14x^2 + 2 = 0$ oe or <b>M1</b> for correct removal of denominator or collection of terms on one side
4	(a)	1/64	2	<b>M1</b> for $\frac{1}{8} \times \frac{1}{8}$
	(b)	$\frac{63}{64}$	1FT	<b>FT</b> 1 – their (a)
	(c)	$\frac{30}{64}$ oe	2	M1 for $[2 \times] \frac{3}{8} \times \frac{5}{8}$ oe
	(d)	<del>7</del> <del>64</del>	3	<b>M2</b> for $\frac{1}{8} \times \frac{1}{8} + \frac{1}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{1}{8}$ oe
	(e)	$\frac{24}{64}$ oe	3	or <b>M1</b> for identifying combinations required, (8, 8) and (8, 6) and (8, 5) or identifying 6 out of the 7 possible outcomes <b>M2</b> for $\frac{1}{8} \times \frac{7}{8} + \frac{3}{8} \times \frac{4}{8} + \frac{2}{8} \times \frac{2}{8} + \frac{1}{8} \times \frac{1}{8}$ oe or $\frac{7}{8} \times \frac{1}{8} + \frac{6}{8} \times \frac{1}{8} + \frac{4}{8} \times \frac{2}{8} + \frac{1}{8} \times \frac{3}{8}$ oe or
				M1 for the sum of any two correct products from above oe isw

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	Question	Answer	Mark	Part marks
5	(a)	$[\cos ABL =] \frac{40^2 + 61.1^2 - 92.1^2}{2 \times 40 \times 61.1}$	M2	M1 for correct implicit version
		130.11	<b>A2</b>	<b>A1</b> for $[\cos ABL =] -0.644$ or $-\frac{7873}{12220}$
				or $-\frac{3149.2}{4888}$
	(b)	[0]59.5 or 59.50 to 59.511	4	<b>M2</b> for $\frac{40\sin 130.1}{92.1}$ or $\frac{61.1\sin 130.1}{92.1}$
				or $\mathbf{M1}$ for $\frac{\sin A}{40} = \frac{\sin 130.1}{92.1}$ or $\frac{\sin L}{61.1} = \frac{\sin 130.1}{92.1}$
				and A1 for 19.39 to 19.4 or 30.48 to 30.49
	(c)	1h 50min	5	<b>M2</b> for $[BC = ]2 \times 40 \times \cos(180 - 130.1)$ oe
				or <b>M1</b> for $\frac{x}{40} = \cos(180 - 130.1)$ oe
				OR <b>M2</b> for [ <i>BC</i> =] $\sqrt{40^2 + 40^2 - 2 \times 40 \times 40 \cos(their \ 80.2)}$ or <b>M1</b> for correct implicit version
				OR <b>M2</b> for $[BC =]$ $\frac{40\sin(their\ 80.2)}{\sin 49.9}$
				or M1 for correct implicit version
				and
				M1 for $\frac{\text{their }BC}{28}$
				<b>A1</b> for 1.84[0] to 1.841

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	Que	stion	l	Answer	Mark	Part marks
6	(a)	(i)		6000 [7600] 10 200 4200	2	<b>B1</b> for 6000 or 10200 If <b>B0</b> then <b>B1FT</b> for <i>their</i> (UQ – LQ)
		(ii)	(a)	True, median price is lower	1	No inclusion of other statistic
			<b>(b)</b>	False, A's UQ < 13 600 oe	1FT	FT their UQ in (a)(i)
	(b)			11025	4	Listed values are in thousands M1 for 3, 7, 9, 11, 13, 18 soi
						<b>M1</b> for $\Sigma fm$ [1323]
						<b>M1</b> (dep on second <b>M1</b> ) for <i>their</i> $\Sigma fm \div 120$
	(c)			323.25 nfww	3	<b>M2</b> for $9948 - 0.25 \times 8760$
						or M1 for 0.25 × 8760
7	(a)			Attempt to use $18 - r$ in Pythagoras'	M1	
				$\begin{vmatrix} 144 = r^2 - 324 + 18r + 18r - r^2 \text{ oe} \\ 468 = 36r \text{ oe} \end{vmatrix}$	B2 A1	or <b>B1</b> for $324 - 18r - 18r + r^2$ Correct simplification with no errors
	(b)			$[2 \times] \sin^{-1}\left(\frac{12}{13}\right)$ oe	M1	or $\cos = \left(\frac{13^2 + 13^2 - 24^2}{2 \times 13 \times 13}\right)$ or better
						or $[180 - ] 2 \times \sin^{-1}\left(\frac{5}{13}\right)$
				134.76	<b>A1</b>	not 67.4 × 2
	(c)	(i)		332 or 332.1 to 332.2	3	<b>M2</b> for $\frac{(360-134.8)}{360} \times \pi \times 13^2$
						or <b>M1</b> for $\frac{134.8}{360} \times \pi \times 13^2$
		(ii)		392 or 392.0 to 392.2	3	<b>M2</b> for $\frac{1}{2} \times 24 \times 5 + their (c)(i)$
						or $\frac{1}{2} \times 13^2 \times \sin 134.8 + their$ (c)(i)
						or <b>M1</b> for $\frac{1}{2} \times 24 \times 5$ or $\frac{1}{2} \times 13^2 \times \sin 134.8$
		(iii)		15700 or 15670 to 15690	1FT	<b>FT</b> for answer to $40 \times their$ (c)(ii)
	(d)			29.5 or 29.6 or 29.51 to 29.57	2FT	<b>M1</b> for $\pi \times 13^2 \times h = their$ (c)(iii) or better

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	Question		Answer	Mark	Part marks
8	(a) (i)		$\begin{pmatrix} 12 \\ -5 \end{pmatrix}$	2	<b>M1</b> for $\begin{pmatrix} 12 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$
	(ii)		13 nfww	2FT	<b>M1FT</b> for $\sqrt{their 12^2 + their (-5)^2}$
					<b>FT</b> dep on <i>their</i> (a) being $\begin{pmatrix} a \\ b \end{pmatrix}$ where $a, b$ are
					both non-zero
	(b) (i)	(a)	$\mathbf{b} - \mathbf{a}$	1	
		(b)	$\frac{3}{5}$ ( <b>b</b> - <b>a</b> ) or $\frac{3}{5}$ <b>b</b> - $\frac{3}{5}$ <b>a</b> final answer	1FT	FT $\frac{3}{5}$ their vector, in terms of <b>a</b> and <b>b</b> , in (b)(i)(a)
		(c)	$\frac{1}{5}(2\mathbf{a} + 3\mathbf{b}) \text{ or } \frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{b}$ final answer	2	M1 for a + their vector in (b)(i)(b) or any correct route
	(ii)		$\frac{3}{2}$ oe	1	
9	(a)		2.25 oe	2	<b>M1</b> for $8x + 4x = 22 + 5$ or better
	<b>(b)</b>		$x \ge 3.5$ final answer	2	M1 for $6x - 2x \ge 14$ or better
	(c)		(x-7)(x+3) final answer	2	M1 for $x(x + 3) - 7(x + 3)$ or $x(x - 7) + 3(x - 7)$
					or for $(x + a)(x + b)$ where $ab = -21$ or $a + b = -4$
	(d)		$12x^2 + xy - 6y^2$ final answer	3	M2 for $12x^2 + 9xy - 8xy - 6y^2$ or M1 for any two of the four terms correct

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Question	Answer		Mark	Part marks
10 (a)	A: 14	3 <i>n</i> − 1 oe	3	<b>B1</b> for 14 <b>B2</b> for $3n - 1$ oe or <b>M1</b> for $3n + k$ , for any $k$ oe
	B: -4	26 – 6 <i>n</i> oe	3	<b>B1</b> for $-4$ <b>B2</b> for $26 - 6n$ oe or <b>M1</b> for $k - 6n$ , for any $k$ oe
	C: 25	$n^2$ oe	2	<b>B1</b> for 25 <b>B1</b> for <i>n</i> <sup>2</sup>
	D: 20	$n^2 - n$ oe	2	<b>B1</b> for 20 <b>B1</b> for $n^2 - n$ oe
(b) (i)	$\frac{n(3n+1)}{2}=155$		M1	accept $\frac{3n^2 + n}{2} = 155$
	$3n^2 + n = 310$			Intermediate step must include elimination of fraction, e.g. $n(3n + 1) = 310$
	$3n^2 + n - 310 = 0$	)	A1	with no errors or omissions
(ii)	$10, -\frac{31}{3}$ oe		3	M2 for $(3n + 31)(n - 10)$ [= 0] or M1 for $3n(n - 10) + 31(n - 10)$ or $n(3n + 31) - 10(3n + 31)$ or $(3n + a)(n + b)$ where $ab = -310$ or $a + 3b = 1$
(iii)	10		1FT	FT their (b)(ii) if only one positive integer solution

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Question	Answer	Mark	Part marks
11	$5 \text{ and} - \frac{27}{2} \text{ oe}$	7	M2 for $12 \times 2(2x - 1) + (x + 3)(2x - 1) =$ $12 \times 3(x + 3)$ oe or M1 for a common denominator with 2 or more of the terms  and B2 for $2x^2 + 17x - 135$ [= 0] oe or B1 for $48x - 24$ or $2x^2 - x + 6x - 3$ or $36x + 108$ or $2x^2 - x + 54x - 27$ or $132 - 12x$ or $37x + 111 - 2x^2 - 6x$ and M2 for $(2x + 27)(x - 5)$ or their correct factors or formula or M1 for $2x(x - 5) + 27(x - 5)$ or $x(2x + 27) - 5(2x + 27)$ or $(2x + a)(x + b)$ where $ab = -135$
			or $a + 2b = 17$