

### Cambridge IGCSE™

MATHEMATICS (US)

Paper 4 (Extended)

MARK SCHEME

Maximum Mark: 130

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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#### **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

#### GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

#### GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

#### GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

#### GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

#### GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

#### GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Maths-Specific Marking Principles			
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.			
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.			
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.			
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).			
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.			
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.			

### **Abbreviations**

cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

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Question	Answer	Marks	Partial Marks
1(a)	Rotation 90° clockwise oe [centre] (5, 2)	3	B1 for each
1(b)(i)	Translation $\begin{pmatrix} -1 \\ 4 \end{pmatrix}$	2	B1 for each
1(b)(ii)	4.12 or 4.123	2	<b>M1</b> for $(their (-1))^2 + (their 4)^2$
2(a)	52°	3	M1 for $180 - 2 \times 38$ , implied by 104 M1 for their $AOB \div 2$
2(b)(i)	100°	1	
2(b)(ii)	50°	2	<b>M1</b> for angle $FEC$ or angle $FCE = 50$
3(a)(i)	105	2	<b>M1</b> for $\frac{3}{100} \times 500[\times 7]$
3(a)(ii)	115 or 114.9	3	M2 for $500 \times \left(1 + \frac{3}{100}\right)^7 [-500]$ or M1 for $500 \times \left(1 + \frac{3}{100}\right)^k$ , k integer $\ge 2$
3(b)	8600	3	M2 for $\frac{6269.4}{\left(1 - \frac{10}{100}\right)^3}$ oe or M1 for $C \times \left(1 - \frac{10}{100}\right)^3 = 6269.4$ oe
4(a)(i)	4.095	2	<b>B1</b> for figs 4095 or <b>M1</b> for $\frac{525 \times 7.8}{1000}$
4(a)(ii)	15	3	<b>B2</b> for 35 OR <b>M2</b> for $\frac{1}{2}(10+4)\times 5 \times L = 525$ oe <b>M1</b> for $\frac{1}{2}(10+4)\times 5$ oe

Question	Answer	Marks	Partial Marks
4(a)(iii)	455 or 454.9	6	M3 for their $[BD = ]\sqrt{3^2 + 5^2} \times (their \ 15)$ [× 2] or B2 for $\sqrt{34}$ or 5.83 or 5.830 to 5.831 or M1 for $5^2 + \left(\frac{1}{2}(10 - 4)\right)^2$ and M1 for their $35 \times 2$ M1 for (their $15$ ) × 10 and (their $15$ ) × 4
4(a)(iv)	4200	3	M2 for $525 - \left(\frac{10}{5}\right)^3$ oe or M1 for $\left(\frac{10}{5}\right)^3$ or $\left(\frac{5}{10}\right)^3$ oe
4(b)	2.13 or 2.132 to 2.133	3	M2 for $50000 \div 3500 \div \pi$ or M1 for $50000 \div 3500$
5(a)	Correctly equate one set of coefficients	M1	or for expressing one variable in terms of the other
	Correctly eliminate one variable	M1	or for correct substitution
	p = 3 $q = -1$	A2	A1 for each If M0, SC1 for 2 values satisfying one of original equations If 0 scored SC1 for correct answers with no working
5(b)	$1\frac{1}{11}$ or $\frac{12}{11}$ 1.09 or 1.090 to 1.091	2	<b>M1</b> for $\frac{3x}{12} + \frac{8x}{12} = 1$ or better
5(c)(i)	$-2 < x \le 3$	3	<b>B2</b> for $-2 < x$ or $x \le 3$ or <b>M1</b> for $-8 + 2 < 3x$ or $3x \le 7 + 2$
5(c)(ii)	-1, 0, 1, 2, 3	1	FT dep on –ve and +ve values in <i>their</i> (c)(i)
5(d)	4a(4-a) final answer	2	B1 for any correct partial factorisation
5(e)(i)	$\frac{2b}{3a}$ final answer	2	M1 for $\frac{1}{2a} \times \frac{4b}{3}$ or better
5(e)(ii)	$\frac{x-2}{x-1}$ final answer nfww	2	<b>B1</b> for $2(x-1)-x$ oe seen.

Question	Answer	Marks	Partial Marks
6(a)	9.33 or 9.334	3	M2 for $\frac{12\sin 50}{\sin 100}$ or M1 for $\frac{\sin 100}{12} = \frac{\sin 50}{AD}$ oe
6(b)	$[\cos =] \frac{11^2 + 12^2 - 8^2}{2 \times 11 \times 12}$	M2	M1 for $8^2 = 11^2 + 12^2 - 2 \times 11 \times 12 \cos(BAC)$
	40.415	A2	<b>A1</b> for 0.761 or $\frac{201}{264}$ or $\frac{67}{88}$
6(c)	70.8 or 70.77 to 70.79	3	M1 for $\frac{1}{2} \times 12 \times their$ (a) $\times \sin(180 - 100 - 50)$ M1 for $\frac{1}{2} \times 12 \times 11 \times \sin(40.42)$
6(d)	7.13 or 7.131 to 7.132	3	M2 for $\frac{\text{dist}}{11} = \sin(40.42)$ or M1 for recognition that shortest distance is perpendicular to $AC$
7(a)	87	3	<b>M2</b> for $3c + 4c = 587 + 22$ or better or <b>M1</b> for $3c + 2(2c - 11)$ [= 587 or 5.87]
7(b)	1.1[0]	3	M2 for $22w + 22 = 42w$ or better or M1 for $\frac{22}{w} = \frac{42}{w+1}$ oe OR B2 for number of bottles = 20 or M1 for $Nw = 22$ and $N(w+1) = 42$
8(a)(i)	$\frac{60}{360} \times 600$ oe	1	
8(a)(ii)	45	2	<b>M1</b> for $\frac{27}{360} \times 600$ oe
8(a)(iii)	Correct straight line on the pie chart	2	<b>B1</b> for 75
8(b)	Correct diagram  0.6 3.4 5.2 7.5 8.7	3	B1 for any three of 0.6, 3.4, 5.2, 7.5, 8.7 correctly placed B1 for 7.5 and 8.7 seen
8(c)(i)	5	1	

Question	Answer	Marks	Partial Marks
8(c)(ii)	2	1	
8(c)(iii)	3	1	
8(d)	39.2	4	M1 for mid-values soi
			M1 for $\Sigma fx$ with $x$ in correct interval including boundaries $\Sigma fx$
			<b>M1 dep</b> for $\frac{\Sigma fx}{50}$ dep on second M1
9(a)(i)	(0,0),(1,0),(2,0)	2	B1 for any two correct
			If 0 scored, SC1 for all three <i>x</i> values clearly identified
9(a)(ii)	С	1	
9(b)	$[g(x) =] \frac{5}{x}$	2	<b>M1</b> for $y = \frac{k}{x}$
9(c)(i)	-2 2	1	
9(c)(ii)	$[a=] 2$ $[b=] \frac{1}{2}$	2	B1 for each
9(d)(i)	Translation $\begin{pmatrix} 5 \\ 0 \end{pmatrix}$	2	B1 for each
9(d)(ii)	Stretch [factor] 5 x-axis oe invariant	3	B1 for each
10(a)(i)	1	1	
10(a)(ii)	$\frac{1}{4}$ oe <b>nfww</b>	2	M1 for $\frac{2}{4} \times \frac{2}{4}$ oe
10(a)(iii)	7	2	M1 for trials with $\left(\frac{3}{4}\right)^k \times \frac{1}{4}$ soi
10(b)(i)	0.72 oe	2	<b>M1</b> for $0.9 \times 0.8$
10(b)(ii)	0.26 oe	3	<b>M2</b> for $0.9 \times 0.2 + 0.1 \times 0.8$ or $1 - their$ (b)(i) $-0.1 \times 0.2$
			or <b>M1</b> for $0.9 \times 0.2$ or $0.1 \times 0.8$ or $1 - their$ (b)(i) or $1 - 0.1 \times 0.2$

Question	Answer	Marks	Partial Marks
11(a)(i)	64	1	
11(a)(ii)	127	1	<b>FT</b> 2 × their <b>(a)(i)</b> – 1
11(b)	$\pm \frac{1}{2}$ oe nfww	4	M1 for $(2x-1)^2 + 2(2x-1)$ B1 for $4x^2 - 2x - 2x + 1$ or $(2x-1)(2x-1+2)$ B1 for $4x^2 - 1$ [= 0] or $(2x-1)(2x+1)$ [= 0] OR M1 for $x(x+2) = 0$ (solving $g(x) = 0$ ) A1 for $x = 0$ or $-2$ B1 for $2x - 1 = 0$ or $2x - 1 = -2$
11(c)	$\frac{x+1}{2}$ oe final answer	2	M1 for $y+1=2x$ or $\frac{y}{2} = x - \frac{1}{2}$ or $x = 2y - 1$
11(d)	$-\frac{1}{6}$ oe nfww	3	<b>B2</b> for $3x = -\frac{1}{2}$ oe OR <b>M1</b> for $2^{2x} \times 2^x$ oe or $4^{\frac{1}{2}x} \times 4^x$ oe or $8^x$ oe M1 for $2^{-\frac{1}{2}}$ or $4^{-\frac{1}{4}}$ or $8^{-\frac{1}{6}}$ soi
12(a)	$\frac{9}{x} + \frac{5}{2x+1} = 2.5 \text{ oe}$ $9(2x+1) + 5x = 2.5x(2x+1) \text{ oe}$	M2	M1 for $\frac{9}{x}$ or $\frac{5}{2x+1}$ Correctly clearing fractions, or correctly collecting into a single fraction FT <i>their</i> expression dep on two fractions
	or $\frac{9(2x+1)+5x}{x(2x+1)}$ [= 2.5 oe]  All brackets expanded leading to $10x^2 - 41x - 18 = 0$ with no errors or omissions	A1	both with algebraic denominators

Question	Answer	Marks	Partial Marks
12(b)	$ \begin{array}{c} (2x-9)(5x+2) \\ \text{or } \frac{-(-41) \pm \sqrt{(-41)^2 - 4(10)(-18)}}{2(10)} \end{array} $	M2	or <b>B1</b> for $(ax+b)(cx+d)$ with $ac = 10$ and $bd = -18$ or $ad + bc = -41$ or $\sqrt{(-41)^2 - 4(10)(-18)}$ or correct $\frac{-(-41)}{2(10)}$ if formula in correct form
	10	A2	A1 for $[x =] \frac{9}{2}$ oe or M1 for $2 \times their$ positive root + 1