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	UNIVERSITY OF CAMBRIDGE INT International General Certificate of S	ERNATIONAL EXAMINATIONS secondary Education
CANDIDATE NAME		
CENTER NUMBER		CANDIDATE NUMBER
ADDITIONAL	MATHEMATICS (US)	0459
Paper 1		May/June 2
		2 ho
Candidates and	swer on the Question Paper	
Additional Mate	erials: Electronic calculator	

READ THESE INSTRUCTIONS FIRST

Write your Center number, candidate number, and name on the work you hand in.

List of formulas and statistical tables (MF25)

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together. The number of points is given in parentheses [] at the end of each question or part question. The total number of points for this paper is 80.



[Turn over



1 A circle is given by the equation

$$x^2 + y^2 - 8x + 6y + 8 = 0$$

Find the radius and the coordinates of the center of the circle.

2 Show that 
$$un \theta \left( \frac{1}{1 - \cos \theta} - \frac{1}{1 + \cos \theta} \right)$$
 can be written as  $\frac{k}{\sin \theta}$  and find the values of the transfer of t



3 A sequence of terms is defined recursively by

$$f(0) = 3$$
,  $f(1) = 5$ ,  $f(n+1) = kf(n) - f(n-1)$  for  $n \ge 1$ .

Given that f(3) = 9, find the possible values of *k*.

4 (i) Show that 
$$\left(\frac{x^{\frac{1}{4}}-x^{-\frac{1}{4}}}{x^{\frac{1}{4}}}\right)^2 = 1 - 2x^{-\frac{1}{2}} + x^{-1}.$$

(ii) Hence solve 
$$(1 - 2x^{-\frac{1}{2}} + x^{-1})^{\frac{1}{2}}x^{\frac{1}{2}} = 5.$$

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[3]

- 9i + 9j is a positi The position vectors of the points A and B, relative to an origin O, are  $5\mathbf{i} + 7\mathbf{j}$  and  $9\mathbf{i} + 9\mathbf{j}$  respectively. The position vector of the point C, relative to O, is  $k\mathbf{i} + 19\mathbf{j}$ , where k is a positi 5 constant.
  - (i) Find the value of k for which the length of AC is 20 units.

(ii) Find the value of k for which ABC is a straight line.

- timates spectively. e following From a random sample of the heights of 100 female college students, unbiased estimates 6 the population mean and standard deviation were found to be 172 cm and 6 cm respectively. a normal distribution, showing the estimated population percentages in each of the following classes.
  - Height, *h* cm  $h \leq 160$  $160 < h \le 165$  $165 < h \le 170$  $170 < h \le 175$  $175 < h \le 180$  $180 \le h \le 185$ 185 < *h*

[6]



The diagram shows a semicircle of radius 4 cm with center O. The radius OC is perpendicular to the diameter AB. An arc of a circle is drawn with center B and radius BC. The arc meets AB at D.

(i) Show that  $BD = 4\sqrt{2}$  cm and find the length of the arc *CD*.

(ii) Find the area of the shaded region.

[4]

[4]

7



The diagram shows a triangle *ABC* together with equilateral triangles *ADB* and *AEC*. The lines *BE* and *CD* intersect at *F*. Prove that

(i) triangles *ADC* and *ABE* are congruent,

(ii) angle  $BFC = 120^{\circ}$ .

8

[3]

[4]

- 9 Given the points A(2, 3), B(4, 0) and C(6, 3.5),
  - (i) find the equation of the perpendicular bisector of AB,

(ii) verify that *C* lies on the perpendicular bisector of *AB*.

[1]

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of AB, Given also that the point D is such that the mid-point of CD is also the mid-point of AB,

(iii) find the coordinates of D,

(iv) explain why the quadrilateral *ACBD* is a rhombus.

[1]



Given that  $\mathbf{A} = \begin{pmatrix} 3 & 2 \\ -1 & 1 \end{pmatrix}$ , use the inverse matrix of **A** to

(i) solve the system of equations

10

$$2y + 3x - 4 = 0, y - x - 7 = 0,$$



13

- s divide The polynomial  $f(x) = 2x^3 + ax^2 + bx + 15$  has x + 3 as a factor. When f(x) is divide x - 3 the remainder is -60. 11
  - (i) Show that a = -5 and find the value of b.

(ii) Solve f(x) = 0.

[4]



Question 12 is printed on the next page.

- www.papacambridge.com Two events, A and B, are such that P(A) = 0.6, P(B) = 0.3 and P(B|A) = 0.4. Calculate 12 probability that
  - (i) either A or B occurs, but not both,

(ii) neither A nor B occurs.

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[2]