	i ampridae		dge International Exam dge International Genera	inations I Certificate of Secondary Educati	on
	CANDIDATE NAME				
	CENTRE NUMBER			CANDIDATE NUMBER	
4	MATHEMATICS	s			0580/41
0	Paper 4 (Exten	nded)			May/June 2015
n					2 hours 30 minutes
	Candidates ans				
	Additional Mate	erials:	Electronic calculator Tracing paper (optional).	Geometrical instruments	;

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.

This document consists of 20 printed pages.

- 1 12 000 vehicles drive through a road toll on one day. The ratio cars:trucks:motorcycles = 13:8:3.
  - (a) (i) Show that 6500 cars drive through the road toll on that day.

Answer(a)(i)

[1]

(ii) Calculate the number of trucks that drive through the road toll on that day.

(b) The toll charges in 2014 are shown in the table.

Vehicle	Charge
Cars	\$2
Trucks	\$5
Motorcycles	\$1

Show that the total amount paid in tolls on that day is \$34500.

Answer(b)

(c) This total amount is a decrease of 8% on the total amount paid on the same day in 2013.

Calculate the total amount paid on that day in 2013.

(d) 2750 of the 6500 car drivers pay their toll using a credit card.

Write down, in its simplest terms, the fraction of car drivers who pay using a credit card.

(e) To the nearest thousand, 90 000 cars drive through the road toll in one week.Write down the lower bound for this number of cars.

www.xtrapapers.com

[4]

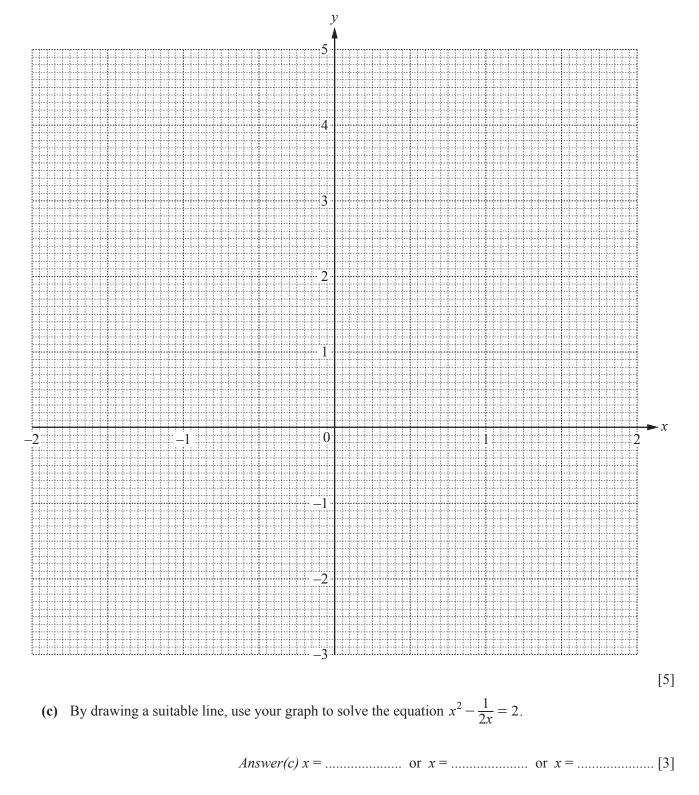
4

## 2 The table shows some values for $y = x^2 - \frac{1}{2x}, x \neq 0.$

x	-2	-1.5	-1	-0.5	-0.25	-0.2		0.2	0.25	0.5	1	1.5	2
У	4.25	2.58			2.06	2.54		-2.46	-1.94			1.92	3.75

(a) Complete the table of values.

(b) On the grid, draw the graph of 
$$y = x^2 - \frac{1}{2x}$$
 for  $-2 \le x \le -0.2$  and  $0.2 \le x \le 2$ .



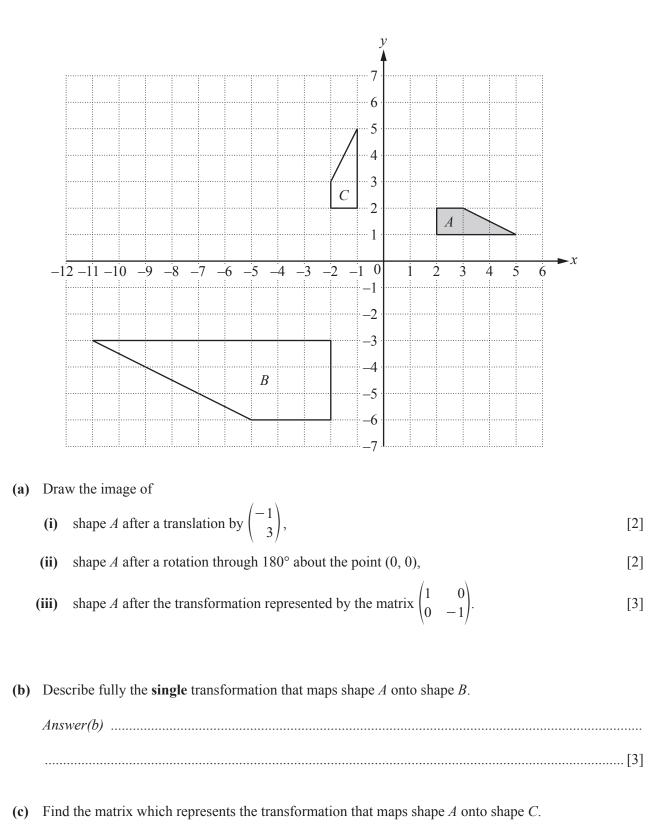
(d) The equation  $x^2 - \frac{1}{2x} = k$  has only one solution.

Write down the range of values of k for which this is possible.

*Answer(d)* [2]

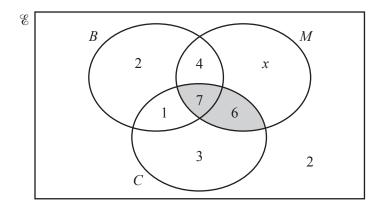
(e) By drawing a suitable tangent, find an estimate of the gradient of the curve at the point where x = -1.





Answer(c) [2]

4 30 students were asked if they had a bicycle (*B*), a mobile phone (*M*) and a computer (*C*). The results are shown in the Venn diagram.



(a) Work out the value of x.

Answer(a)  $x = \dots$ [1]

(b) Use set notation to describe the shaded region in the Venn diagram.

(c) Find  $n(C \cap (M \cup B)')$ .

(d) A student is chosen at random.

(i) Write down the probability that the student is a member of the set M'.

(ii) Write down the probability that the student has a bicycle.

(e) Two students are chosen at random from the students who have computers.Find the probability that each of these students has a mobile phone but no bicycle.

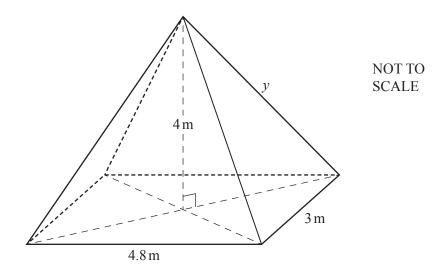
- 5 (a) Andrei stands on level horizontal ground, 294 m from the foot of a vertical tower which is 55 m high.
  - (i) Calculate the angle of elevation of the top of the tower.

(ii) Andrei walks a distance x metres directly towards the tower. The angle of elevation of the top of the tower is now 24.8°.

Calculate the value of *x*.

 $Answer(a)(ii) x = \dots [4]$ 

(b) The diagram shows a pyramid with a horizontal rectangular base.



The rectangular base has length 4.8 m and width 3 m and the height of the pyramid is 4 m.

Calculate

(i) *y*, the length of a sloping edge of the pyramid,

*Answer(b)*(i) *y* = ..... m [4]

(ii) the angle between a sloping edge and the rectangular base of the pyramid.

- Time taken<br/>(t mins) $0 < t \le 10$  $10 < t \le 24$  $24 < t \le 30$  $30 < t \le 40$  $40 < t \le 60$  $60 < t \le 70$ Frequency1090135857010
- 6 The table shows the time, *t* minutes, that 400 people take to complete a test.

(a) (i) Write down the modal time interval.

*Answer(a)*(i) ..... min [1]

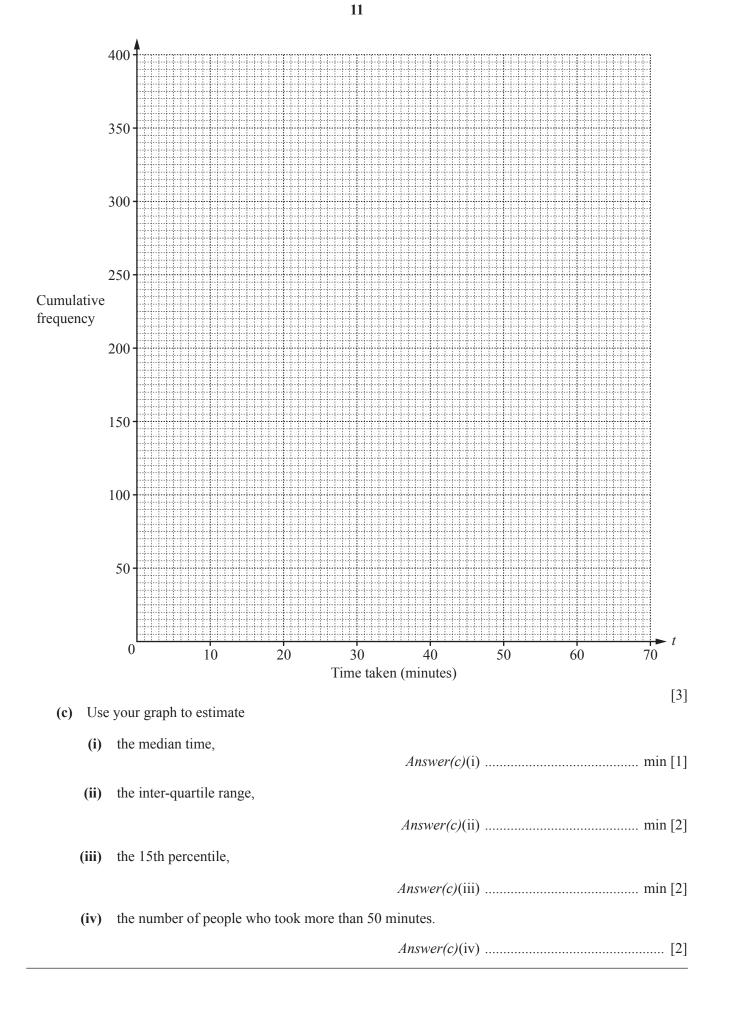
(ii) Calculate an estimate of the mean time taken to complete the test.

*Answer(a)*(ii) ..... min [4]

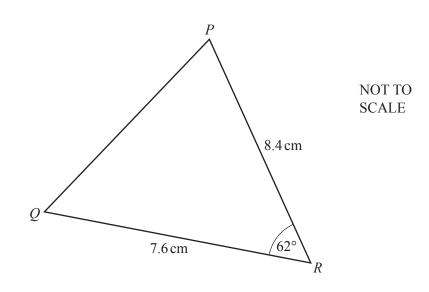
(b) (i) Complete the table of cumulative frequencies.

Time taken ( <i>t</i> mins)	<i>t</i> ≤ 10	<i>t</i> ≤ 24	<i>t</i> ≤ 30	<i>t</i> ≤ 40	$t \le 60$	$t \leq 70$	
Cumulative frequency	10	100				400	
							[2

(ii) On the grid opposite, draw a cumulative frequency diagram to show this information.



7 (a)



In the triangle *PQR*, QR = 7.6 cm and PR = 8.4 cm. Angle  $QRP = 62^{\circ}$ .

Calculate

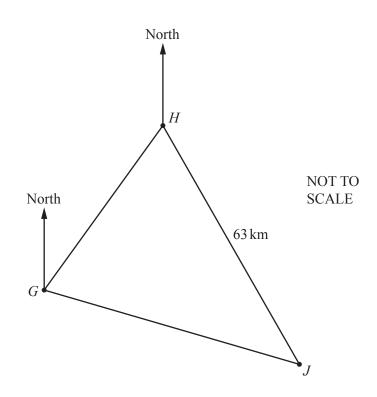
(i) *PQ*,

*Answer(a)*(i) *PQ* = ..... cm [4]

(ii) the area of triangle PQR.

*Answer(a)*(ii) ..... cm<sup>2</sup> [2]

**(b)** 



The diagram shows the positions of three small islands G, H and J. The bearing of H from G is 045°. The bearing of J from G is 126°. The bearing of J from H is 164°. The distance HJ is 63 km.

Calculate the distance GJ.

Answer(b)  $GJ = \dots$  km [5]

8 (a) Jamil, Kiera and Luther collect badges. Jamil has x badges. Kiera has 12 badges more than Jamil. Luther has 3 times as many badges as Kiera. Altogether they have 123 badges.

Form an equation and solve it to find the value of *x*.

 $Answer(a) x = \dots [3]$ 

(b) Find the integer values of t which satisfy the inequalities.

$$4t + 7 < 39 \le 7t + 2$$

(c) Solve the following equations.

(i) 
$$\frac{21-x}{x+3} = 4$$

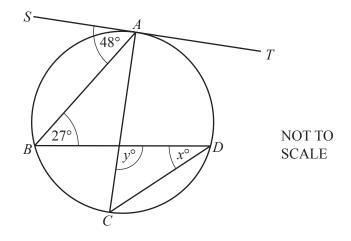
 $Answer(c)(i) x = \dots [3]$ 

(ii)  $3x^2 + 7x - 5 = 0$ 

Show all your working and give your answers correct to 2 decimal places.

15

9 (a) The points A, B, C and D lie on a circle. AC is a diameter of the circle. ST is the tangent to the circle at A.

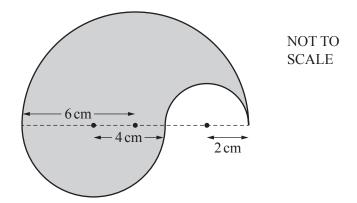


## Find the value of

(i) *x*,

**(ii)** *y*.

 $Answer(a)(ii) y = \dots [2]$ 



(i) Calculate the perimeter of the shaded shape.

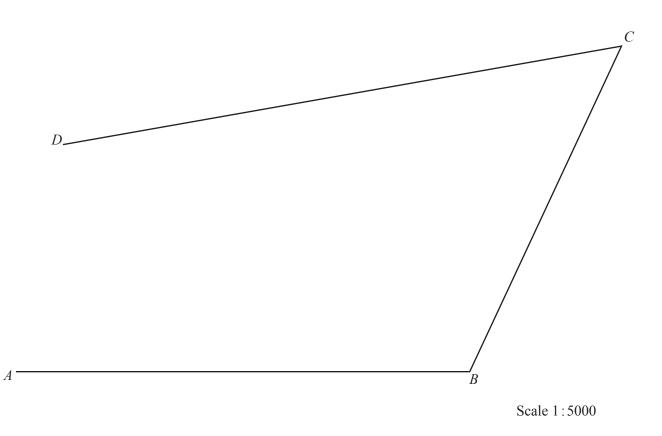
*Answer(b)*(i) ..... cm [2]

(ii) The shaded shape is made from metal 1.6 mm thick.

Calculate the volume of metal used to make this shape. Give your answer in cubic millimetres.

*Answer(b)*(ii) ..... mm<sup>3</sup> [5]

**10** The diagram is a scale drawing of three straight roads, *AB*, *BC* and *CD*. The scale is 1:5000.



18

(a) Find the actual length of the road *BC*. Give your answer in metres.

*Answer(a)* ..... m [2]

(b) Another straight road starts at *M*, the midpoint of *AB*. This road is perpendicular to *AB* and it meets the road *CD* at *X*.

Using a straight edge and compasses only, construct MX.

© UCLES 2015

[2]

(c) There is a park in the area enclosed by the four roads.

The park is

• less than 290 m from *B* 

and

• nearer to *CD* than to *CB*.

Using a ruler and compasses only, construct the boundaries of the park.

Leave in all your construction arcs and label the park *P*.

[5]

Question 11 is printed on the next page.

11 (a) Make *x* the subject of the formula.

$$A - x = \frac{xr}{t}$$

 $Answer(a) x = \dots [4]$ 

(b) Find the value of a and the value of b when  $x^2 - 16x + a = (x + b)^2$ .

 $Answer(b) a = \dots [3]$ 

(c) Write as a single fraction in its simplest form.

$$\frac{6}{x-4} - \frac{5}{3x-2}$$

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge International Examinations Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cie.org.uk after the live examination series.