	Cambridge		dge Internation dge Internationa		nations Certificate of Secondary Educ	ation
	CANDIDATE NAME					
×=====	CENTRE NUMBER				CANDIDATE NUMBER	
σ	MATHEMATIC	CS				0580/42
ω	Paper 4 (Exter	nded)				May/June 2018
4						2 hours 30 minutes
n	Candidates an	nswer on th	ne Question Pape	er.		
0 4 2 8	Additional Mat	terials:	Electronic calcu Tracing paper (c		Geometrical instrume	ents
*						

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.

This document consists of 15 printed pages and 1 blank page.

1 (a) Here is a list of ingredients to make 20 biscuits.

260g of butter	
500g of sugar	
650g of flour	
425g of rice	

- (i) Find the mass of rice as a percentage of the mass of sugar.
 -%[1]
- (ii) Find the mass of butter needed to make 35 of these biscuits.

..... g [2]

(iii) Michel has 2 kg of each ingredient.

Work out the greatest number of these biscuits that he can make.

.....[3]

(b) A company makes these biscuits at a cost of \$1.35 per packet. These biscuits are sold for \$1.89 per packet.

(i) Calculate the percentage profit the company makes on each packet.

(ii) The selling price of \$1.89 has increased by 8% from last year.

Calculate the selling price last year.

(c) Over a period of 3 years, the company's sales of biscuits increased from 15.6 million packets to 20.8 million packets. The sales increased exponentially by the same percentage each year.

The sales increased exponentially by the same percentage each

Calculate the percentage increase each year.

(d) The people who work for the company are in the following age groups.

Group A	Group B	Group C
Under 30 years	30 to 50 years	Over 50 years

The ratio of the number in group A to the number in group B is 7:10. The ratio of the number in group B to the number in group C is 4:3.

(i) Find the ratio of the number in group A to the number in group C. Give your answer in its simplest form.

(ii) There are 45 people in group C.

Find the total number of people who work for the company.

.....[3]

4

2 The time taken for each of 120 students to complete a cooking challenge is shown in the table.

Time (<i>t</i> minutes)	$20 < t \le 25$	$25 < t \le 30$	$30 < t \le 35$	$35 < t \le 40$	$40 < t \le 45$
Frequency	44	32	28	12	4

(a) (i) Write down the modal time interval.

 $\dots \dots < t \leq \dots \dots [1]$

(ii) Write down the interval containing the median time.

 $\dots < t \leq \dots [1]$

(iii) Calculate an estimate of the mean time.

..... min [4]

(iv) A student is chosen at random.

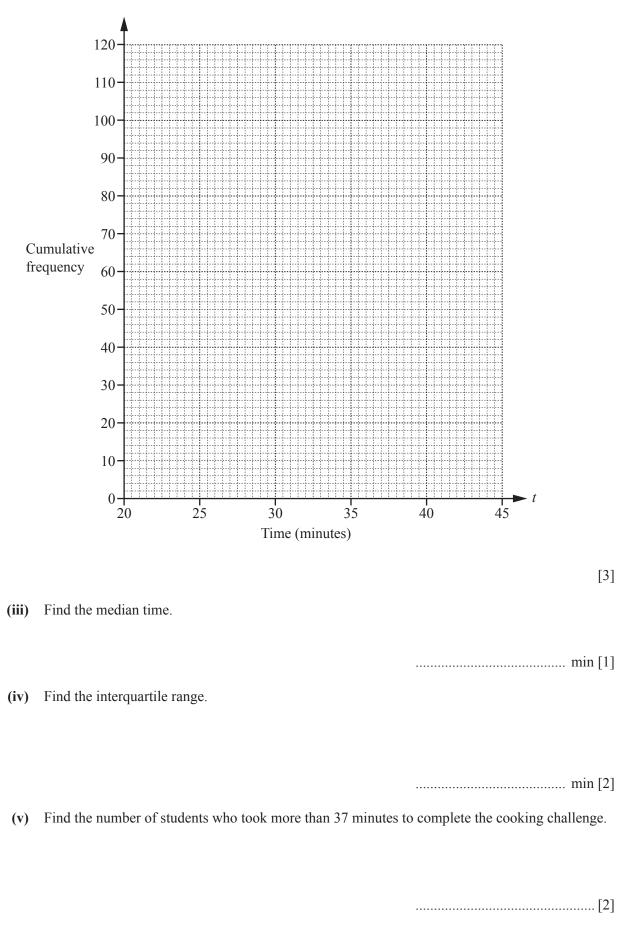
Find the probability that this student takes more than 40 minutes.

.....[1]

(b) (i) Complete the cumulative frequency table.

Time (<i>t</i> minutes)	<i>t</i> ≤ 20	<i>t</i> ≤ 25	<i>t</i> ≤ 30	<i>t</i> ≤ 35	<i>t</i> ≤ 40	<i>t</i> ≤ 45
Cumulative frequency	0	44				

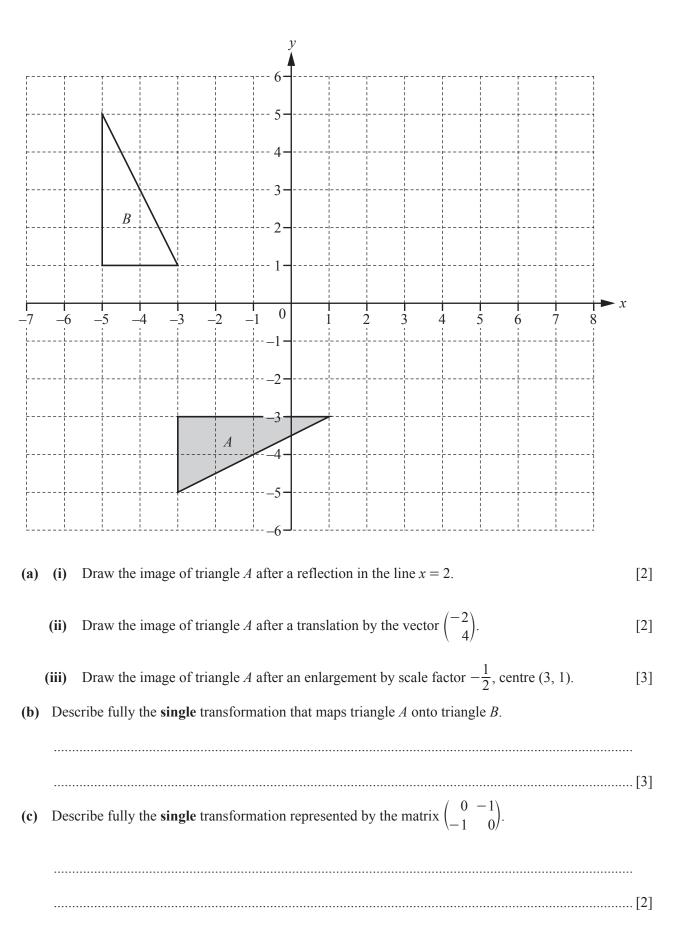
[2]



(ii) On the grid, draw a cumulative frequency diagram to show this information.

5





4 (a) Simplify.

(i) $(3p^2)^5$

.....[2]

(ii)
$$18x^2y^6 \div 2xy^2$$

.....[2]

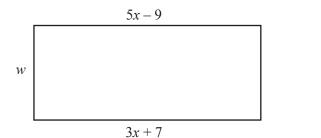


.....[1]

NOT TO

SCALE

(b) In this part, all measurements are in metres.

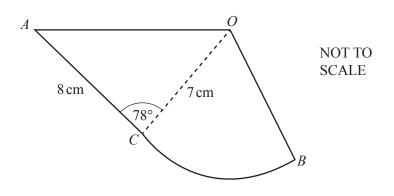


The diagram shows a rectangle. The area of the rectangle is 310 m^2 .

Work out the value of *w*.

 $w = \dots [4]$

[4]



The diagram shows a design made from a triangle *AOC* joined to a sector *OCB*. AC = 8 cm, OB = OC = 7 cm and angle $ACO = 78^{\circ}$.

(a) Use the cosine rule to show that OA = 9.47 cm, correct to 2 decimal places.

(b) Calculate angle *OAC*.

(c) The perimeter of the design is 29.5 cm.

Show that angle $COB = 41.2^\circ$, correct to 1 decimal place.

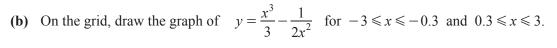
[5]

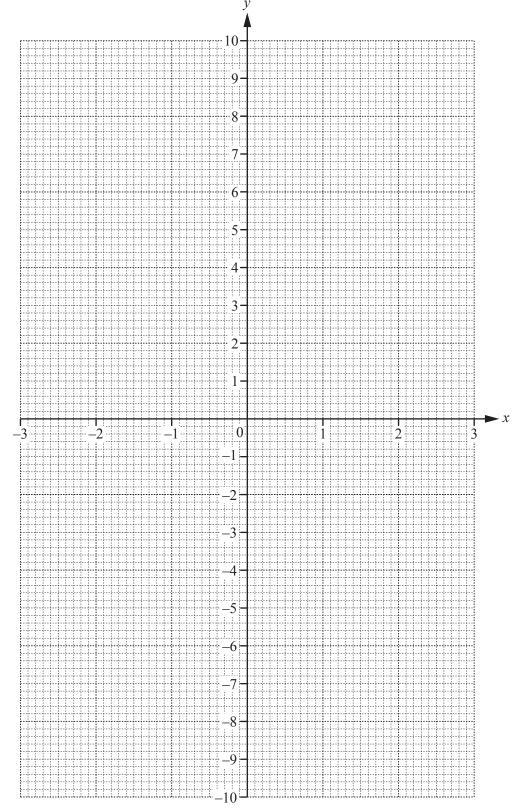
(d) Calculate the total area of the design.

..... cm² [4]

6 (a) Complete the table of values for $y = \frac{x^3}{3} - \frac{1}{2x^2}$, $x \neq 0$.

x	-3	-2	-1	-0.5	-0.3	0.3	0.5	1	2	3	
у	-9.1	-2.8	-0.8		-5.6	-5.5	-2.0			8.9	[3]





11

(c) (i) By drawing a suitable tangent, find an estimate of the gradient of the curve at x = -2.

(ii) Write down the equation of the tangent to the curve at x = -2. Give your answer in the form y = mx + c.

(d) Use your graph to solve the equations.

(i)
$$\frac{x^3}{3} - \frac{1}{2x^2} = 0$$

(ii) $\frac{x^3}{3} - \frac{1}{2x^2} + 4 = 0$
[1]

 $x = \dots$ or $x = \dots$ [3]

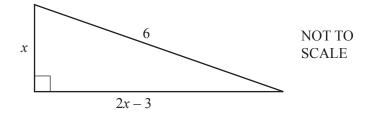
(e) The equation $\frac{x^3}{3} - \frac{1}{2x^2} + 4 = 0$ can be written in the form $ax^n + bx^{n-3} - 3 = 0$.

Find the value of *a*, the value of *b* and the value of *n*.

<i>a</i> =	 	 	
<i>b</i> =	 	 	
n =	 	 	[3]

[3]

7 In this question, all measurements are in metres.



The diagram shows a right-angled triangle.

(a) Show that $5x^2 - 12x - 27 = 0$.

(b) Solve $5x^2 - 12x - 27 = 0$. Show all your working and give your answers correct to 2 decimal places.

 $x = \dots$ [4]

(c) Calculate the perimeter of the triangle.

..... m [2]

(d) Calculate the smallest angle of the triangle.

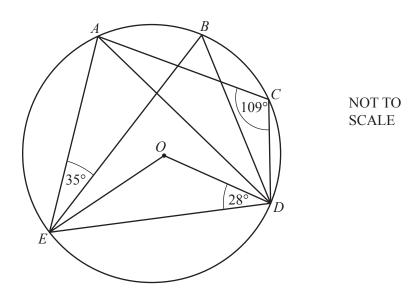
.....[2]

8 (a)	f(x) = 8 - 3x Find	$g(x) = \frac{10}{x+1}, x \neq -1$	$h(x) = 2^x$
	(i) $hf\left(\frac{8}{3}\right)$,		
	(ii) gh(-2),		[2]
	(iii) $g^{-1}(x)$,		[2]
	(iv) $f^{-1}f(5)$.		$g^{-1}(x) = \dots [3]$
(b)	Write $f(x) + g(x)$ as a	single fraction in its simplest form	[1]

.....[3]

14

9 (a)



A, *B*, *C*, *D* and *E* lie on the circle, centre *O*. Angle $AEB = 35^\circ$, angle $ODE = 28^\circ$ and angle $ACD = 109^\circ$.

(i) Work out the following angles, giving reasons for your answers.

(a)	Angle <i>EBD</i> = because
	[3]
(b)	Angle <i>EAD</i> = because
	[2]

(ii) Work out angle *BEO*.

Angle *BEO* =[3]

- (b) In a regular polygon, the interior angle is 11 times the exterior angle.
 - (i) Work out the number of sides of this polygon.

.....[3]

(ii) Find the sum of the interior angles of this polygon.

.....[2]

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