

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/41

Paper 4 (Extended)

May/June 2016

MARK SCHEME

Maximum Mark: 120

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2016 series for most Cambridge IGCSE[®], Cambridge International A and AS Level components and some Cambridge O Level components.

® IGCSE is the registered trademark of Cambridge International Examinations.



| Page 2 | Mark Scheme | Syllabus | Paper |
|--------|---------------------------------|----------|-------|
| | Cambridge IGCSE – May/June 2016 | 0607 | 41 |

Abbreviations

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

| | Question | Answer | Mark | Part Marks |
|---|----------|---|--------|--|
| 1 | (a) (i) | 16 000 | 3 | M2 for 13600 ÷ 0.85 oe or M1 for 13600 = 85% |
| | (ii) | 9590 or 9587 to 9588 | 3 | M2 for 13600×0.89^3 oe or M1 for 13600×0.89^k , $k > 1$ oe |
| | (b) | 9 years nfww | 3 | M2 for $\frac{\log\left(\frac{11500}{23000}\right)}{\log 0.92}$ |
| | | | | or 23 $000 \times 0.92^n = 11500$ and appropriate sketch or at least 2 valid trials |
| | | | | or M1 for $23\ 000 \times 0.92^n$ [= 11500] |
| | | 300 | | If 0 scored SC2 for 8 nfww or 8.3(1295) nfww |
| 2 | (a) | $\frac{300}{L}$ oe | 3 | M1 for $f = \frac{k}{L}$ soi oe |
| | | | | M1 (Dep on 1 st M1) for substituting $f = 93.7$ and $L = 3.2$ soi by 299.8 or 299.84 |
| | (b) | 107 or 107.0 to 107.1 | 1FT | FT $\frac{their k}{L}$ oe only |
| | (c) | 857 or 856.5 to 857.1 | 2FT | $\mathbf{FT} \ \frac{\text{their } k}{L} \text{ oe only}$ |
| | | | | M1 for $0.35 = \frac{their k}{L}$ |
| 3 | (a) (i) | Quadrilateral drawn at $(-1, -1), (-1, -2), (-3, -1), (-3, -3)$ | 3 | M2 for 3 pts correct or M1 for correct reflection of A in y-axis |
| | (ii) | Reflection $y = -x$ oe | 1 1 | |
| | (b) (i) | Quadrilateral drawn at (3, 1), (6, 1), (3, 3), (9, 3) | 2 | B1 for any stretch with <i>y</i> -axis invariant or with stretch factor 3 |
| | (ii) | Stretch, y-axis oe invariant (stretch factor) $\frac{1}{y}$ | 2 | B1 for any 2 correct |
| | | (stretch factor) $\frac{1}{3}$ | | |

| Page 3 | Mark Scheme | Syllabus | Paper |
|--------|---------------------------------|----------|-------|
| | Cambridge IGCSE – May/June 2016 | 0607 | 41 |

| | Question | Answer | Mark | Part Marks |
|---|------------|--|------|---|
| 4 | (a) | 66 000 or 65 970 to 65 982 | 4 | M1 for $\frac{4}{3} \times \pi \times 15^3$ |
| | | | | M1 for $\pi \times 15^2 \times 40$ M1 for $\pi \times 25^2 \times 12$ |
| | (b) (i) | 16.4 | 1 | |
| | (ii) | 120 | 3 | M2 for $15000 \div 5^3$ oe or M1 for 5^3 or $(\frac{1}{5})^3$ seen |
| 5 | (a) | 4 points plotted correctly | 2 | B1 for 2 or 3 correct |
| | (b) | Positive | 1 | Ignore comments on strength |
| | (c) (i) | 75 | 1 | |
| | (ii) | 16.6 | 1 | |
| | (d) (i) | 0.168t + 3.96 | 2 | or $m = 0.1684$ to 0.1685 , $c = 3.963$ to 3.964 B1 for $n = mt + c$ with either m or c correct or SC1 for $0.17t + 4[.0]$ |
| | (ii) | 18 | 1FT | FT from <i>their</i> equation with $t = 85$, answer rounded or truncated to nearest whole number |
| 6 | (a) | 3n + 2 oe final answer | 2 | B1 for $3n + k$ or $kn + 2$ oe |
| | (b) | -3, 4, 15, 30 | 2 | B1 for 2 or 3 correct in correct place or –6, –3, 4, 15 |
| | (c) | 2n-3 oe final answer | 3 | M2 for $(2n-3)(n+2)$ or SC1 for $(2n+a)(n+b)$ where $ab = -6$ or $a+2b=1$ |
| | | | | OR |
| | | | | B1 for -1 , 1, 3, 5 B1 for answer $2n + k$ or $kn - 3$ |
| | (d) | No and e.g. 502 not a multiple of 5 oe nfww | 2 | Dep on $5n - 1$ M1dep for <i>their</i> $(3n + 2) + their (2n - 3) = 501$ oe Dependent on (a) and (c) linear |
| 7 | (a) | 19.9 or 19.89 to 19.90 | 3 | M2 for $36^2 - 30^2$ soi by 396 or M1 for $AD^2 + 30^2 = 36^2$ oe |
| | (b) | 30 ÷ tan 68 oe | M2 | M1 for $\tan 68 = \frac{30}{AC}$ oe |
| | | 12.12 | A1 | |
| | (c) | 301 or 301.3 to 301.4 or 239 or 238.6 to 238.7 | 3 | B2 for 31.3 or 31.30 to 31.35 or M1 for tan = $12.1 \div their$ (a) oe |

| Page 4 | Mark Scheme | | Paper |
|--------|---------------------------------|------|-------|
| | Cambridge IGCSE – May/June 2016 | 0607 | 41 |

| | Question | Answer | Mark | Part Marks |
|---|----------|--|--------|---|
| 8 | (a) (i) | Correct sketch y f(x)=log(1+2x+x*2) 2- 4- | 2 | B1 RH branch through (0, 0) ,with asymptote x = a (-ve a) B1 for LH branch symmetrical, with asymptote x = a (-ve a) |
| | (ii) | -2 0 | 1 1 | |
| | (iii) | x = -1 | 1 | |
| | (b) (i) | Correct sketch | 2 | B1 for correct shape |
| | (ii) | Same right hand branch | 1 | |
| | (iii) | e.g. $log(1 + 2x + x^2) = 2 log(1 + x)$ No log of a negative number | 1 1 | Independent |
| 9 | (a) | 1 hour 20 minutes cao | 3 | M1 for 65 ÷ 48.75 M1 for correctly converting <i>their</i> time in hours to hours and mins |
| | (b) | 140 or 140.4 to 140.5 | 5 | M1 for 632 + 65 [km] soi by 697 M1 for <i>their</i> 697 ÷ 119.5 soi by 5.83 M1 for subtracting <i>their</i> 1.33(from (a)) M1 for 632 ÷ (<i>their</i> 4.4993) |
| | (c) | 27.9 | 3 | M2 for $\frac{800 + 130}{120 \times \frac{1000}{60 \times 60}}$ oe or M1 for distance ÷ speed |

| Page 5 | Mark Scheme | Syllabus | Paper |
|--------|---------------------------------|----------|-------|
| | Cambridge IGCSE – May/June 2016 | 0607 | 41 |

| (| Question | Answer | Mark | Part Marks |
|----|----------|---|----------------------------|--|
| 10 | (a) | 8.94 or 8.944 or $4\sqrt{5}$ | 3 | M2 for 8 ² + 4 ² M1 for 8 and 4 seen |
| | (b) | Gradient of $AB = \frac{1}{2}$ oe Gradient of perpendicular = -2 oe y = (their-2)x + c | 1 1FT M1 | |
| | | midpoint $(2, 1)$ Substitute $(2, 1)$ to reach $c = 5$ OR | B1 A1 | May be on diagram |
| | | $(x+2)^2 + (y+1)^2$ oe $(x-6)^2 + (y-3)^2$ oe equating above two expressions 3 correct expansions correct completion with no errors or omissions | B1 B1 M1 B1 A1 | |
| | (c) | $\left(\frac{5}{3}, \frac{5}{3}\right)$ oe | 2 | M1 for $x + 2x = 5$ oe |
| 11 | (a) | $9^{2} = (3x - 1)^{2} + (2x)^{2}$ $-2(2x)(3x - 1)\cos 60 \text{ oe}$ | M1 | |
| | | $81 = 9x^2 - 6x + 1 + 4x^2 - 6x^2 + 2x \text{ oe}$ | A2 | or B1 for $9x^2 - 3x - 3x + 1$ |
| | | $7x^2 - 4x - 80 = 0$ | A1 | Completion with no errors or omissions |
| | (b) (i) | $\frac{-(-4)\pm\sqrt{(-4)^2-4\times7\times(-80)}}{2\times7}$ oe | M1 | or sketch of quadratic graph (any relevant one) with 1 positive root and 1 negative root |
| | | x = 3.68 or 3.678 or -3.11 or -3.107 to -3.106 | B2 | B1 for either |
| | (ii) | [AB =] 7.36 or 7.356 to 7.357 [BC =] 10[.0] or 10.03 to 10.04 | 1FT 1FT | FT 2 × a positive root FT 3 × a positive root – 1 |
| | (c) | 31.9 or 32[.0] or 31.85 to 32[.00] | 2FT | M1 for $\frac{1}{2} \times their AB \times their BC \sin 60$ oe |

| Page 6 | 6 Mark Scheme | | Paper |
|--------|---------------------------------|------|-------|
| | Cambridge IGCSE – May/June 2016 | 0607 | 41 |

| | Question | Answer | Mark | Part Marks |
|----|----------|------------------------------------|------|---|
| 12 | (a) | 63.6 | 2 | M1 for midpoints (47.5, 52.5, 57.5, 62.5, 67.5, 72.5, 77.5) soi |
| | (b) | Correct Curve | 5 | B4 for 5 points correct and joined or for 6 points correct or B3 for at least 3 correct points or B2 for all correct cfs 5, 24, 58, 116, 162, 191, 200 seen or B1 for at least 3 correct cfs or for increasing curve with 6 points plotted at upper bounds If 0 or 1 or 2 scored, SC3 for all points correct but consistently translated to mid-interval or lower bound. |
| | (c) (i) | 63 to 64 | 1 | Dependent on increasing curve |
| | (ii) | 8.5 to 10.5 | 2 | B1 for[l.qtile. =] 58.5 to 59.5 or [u.qtile. =] 68 to 69 Dependent on increasing curve |
| | (d) (i) | $\frac{12 \text{ to } 16}{200}$ oe | 1FT | FT (their 'read off' at 53)/200 dep on increasing cfs |
| | (ii) | $\frac{72}{39800}$ oe | 2 | M1 for $\frac{k}{200} \times \frac{k-1}{199}$ where $k = 8, 9 \text{ or } 10$ |
| 13 | (a) (i) | 2.25 oe | 2 | M1 for $1 = 2(5 - 2x)$ or $5 - 2x = \frac{1}{2}$ oe |
| | (ii) | -5 + 4x final answer | 2 | B1 for $5 - 2(5 - 2x)$ |
| | (iii) | 5-x oe final answer | 2 | M1 for $2x = 5 - y$ or $x = 5 - 2y$ or $\frac{y}{2} = \frac{5}{2} - x$ |
| | | 2 3 | 1 | |