

Cambridge International Examinations Cambridge International General Certificate of Secondary Education

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/42 May/June 2016

Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

Published

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

Question	Answer	Mark	Part Marks
1 (a)	Image at (5, 5), (7, 5), (6, 6), (5, 6)	2	If 0 scored SC1 for translation $\begin{pmatrix} 3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
(b)	Image at (-1, -2), (-1, -4), (-2, -3), (-2, -2)	2	If 0 scored SC1 for reflection in line $y = x$
(c)	Image at (-2, 5), (-2, 7), (-3, 5), (-3, 6)	3	If 0 scored SC2 for 90° clockwise about (-2, 1) or SC1 for 90° anticlockwise about other centre
(d) (i)	Enlargement [scale factor] 3 [centre] (2, 4)	B1 B1 B1	If combined transformations, all three marks lost
(ii)	Stretch [factor] 2 y-axis oe invariant	B1 B1 B1	If combined transformations, all three marks lost
2 (a)	$\frac{630}{9} \times 5$ and $\frac{630}{9} \times 4$ oe	M2	M1 for $630 \div 9$ [=70] or $\frac{5 \times 630 \text{ or } 3150}{9}$ or $\frac{4 \times 630 \text{ or } 2520}{9}$
(b) (i)	120	3	M2 for 98.4[0] ÷ [0].82 oe or M1 for recognising 98.4[0] is 82%
(ii)	69.5 or 69.51	3	M2 for $\frac{98.4[0] - 30}{98.4[0]} \times 100$ oe or M1 for $\frac{98.4[0] - 30}{98.4[0]}$ oe or $\frac{30}{98.4[0]} \times 100$
(iii)	211.6[0] cao final answer	1	If 0 scored, SC1 for answer 75%
(d) (i) (ii) 2 (a) (b) (i) (ii) (iii)	Enlargement [scale factor] 3 [centre] (2, 4) Stretch [factor] 2 <i>y</i> -axis oe invariant $\frac{630}{9} \times 5 \text{ and } \frac{630}{9} \times 4 \text{ oe}$ 120 69.5 or 69.51	B1 B1 B1 B1 B1 M2 3 3	or SC1 for 90° anticlockwise about of centre If combined transformations, all three marks lost If combined transformations, all three marks lost M1 for $630 \div 9$ [=70] or $\frac{5 \times 630 \text{ or } 3150}{9}$ or $\frac{4 \times 630 \text{ or } 252}{9}$ M2 for 98.4[0] \div [0].82 oe or M1 for recognising 98.4[0] is 82% M2 for $\frac{98.4[0] - 30}{98.4[0]} \times 100$ oe or M1 for $\frac{98.4[0] - 30}{98.4[0]}$ oe or $\frac{30}{98.4[0]} \times 1$ If 0 scored, SC1 for answer 75%

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Q	uestion	Answer	Mark	Part Marks
	(iv)	183	4	B3 for answers 182.8 or 182.84 to 182.85 or M2 for $150(1.02)^{10}$ seen oe or M1 for $150(1.02)^n$ seen oe where $n > 1$
	(c)	September or October 2035 nfww	5	B4 for 2035 or 19 years and 9 or 10 or 9.96 or 9.961 to 9.962 months nfww or B3 for 19.8 or 19.83 seen or M2 for $\frac{\log(\frac{500}{350})}{\log(1.0015)}$ oe or 350×1.0015 ⁿ = 500 and at least two valid trials or sketch of appropriate graph or M1 for 350×1.0015 ⁿ [= 500] or $350 \times (1 + \frac{0.15}{100})^n$ [= 500] If 0 scored SC2 for 24[.0] or 23.95 to 23.98 or 2.55 or 2.552 to 2.554 seen
3	(a) (i)	60	1	
5	(ii)	8	2	B1 for $[la =]$ 56 or $[la =]$ 64
	(iii)	12	2	M1 for 188 seen
	(h)	68.6 or 68.57	3	M2 for 50 $\times \frac{2.4}{1.75}$ oe or M1 for <i>their</i> distance \div 1.75 or B1 for distance = 120 or for 2.4 and 1.75 or 144 and 105 or 8640 and 6300 seen If 0 scored, SC1 for 77.2 or 77.24
4	(a)	24	3	M2 for $6w + 5(w + 30) = 414$ oe or better
	(b)	$2x^2 + 4x - 7 = 0$ oe	B2	i.e. a correct simplified quadratic equation M1 for $x^2 + (x+1)(x+3)$ [=10] oe
		Sketch of appropriate graph or correct use of formula or completing square	M1 dep	Dep on a quadratic from addition of two areas. Must see some valid method
		4.48 or 4.49	B2	B1 for 4.484 to 4.485 or $6\sqrt{2} - 4$ or 1.12 or 1.121 or $1.5\sqrt{2} - 1$

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Question		Answer	Mark	Part Marks
5	(a)	Any 2 of the following		
		Angle ADX = Angle BCX and same segment oe Angle DAX = Angle CBX and same segment oe Angle AXD = Angle BXC and vertically opp oe	2	B1 for one of the three pairs or for at least two pairs of angles without reasons or with incorrect reasons
	(b)	7.5 oe	2	M1 for $\frac{2}{3} = \frac{5}{BX}$ oe
	(c)	67.2 or 67.20 to 67.21 nfww	3	M2 for [cos =] $\frac{2^2 + 5^2 - 4.61^2}{2 \times 2 \times 5}$
				or M1 for $4.61^2 = 2^2 + 5^2 - 2 \times 2 \times 5 \cos(AXD)$
6	(a)	Correct sketch		
			2	M1 for shape i.e. starting at origin then one maximum then one minimum A1 for two zeros to right of $x = 10$ and to the left of $x = 20$
	(b)	13.4 or 13.41 to 13.42 19[.0] or 18.97	1 1	
	(c)	(9.49, 1) or (9.486 to 9.487, 1)	B1 B1	
	(d)	(16.4, -1) or (16.43, -1)	B1 B1	
	(e)	$-1 \leq f(x) \leq 1$	1	
	(f)	Correct sketch of parabola shape from	B 1	
		approximately $y = -1$ 5.48 or 5.477	B1	
7	(a) (i)	576 or 575.8 to 576.0	3	M1 for $\frac{2}{3}\pi \times 5^3$ (262 or 261.7 to 261.8)
				M1 for $\frac{1}{3}\pi \times 5^2 \times 12$ (314 or 314.1 to 314.2)
	(ii)	0.547 or 0.5470 to 0.5472	2FT	FT <i>their</i> (a)(i) M1 for <i>their</i> (a)(i) × 0.95 ÷ 1000
	(iii)	1827 or 1828	2FT	FT with consistent units usual accuracy and truncatedM1 for 1000 ÷ <i>their</i> (a)(ii)

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Q	Question	Answer	Mark	Part Marks
	(iv)	361 or 361.2 to 361.3	4	M1 for $2\pi \times 5^2$ (157 or 157.0 to 157.1)
				M2 for $\pi \times 5 \times \sqrt{5^2 + 12^2}$ (204 or
				$\sqrt{5^2 + 12^2}$ (13)
	(b)	5.37 or 5.369	5	M4 for $\sqrt{\frac{377}{\pi(1+\sqrt{10})}}$
				or M3 for $\frac{377}{\pi(1+\sqrt{10})}$
				or M2 for $\pi r^2 + \pi r \left(\sqrt{(3r)^2 + r^2} \right) = 377$
				or M1 for $r^2 + (3r)^2$ oe
8	(a)	[a, b, c =] -2, 1, 2	1, 1, 1	In any order
		[d=] 0	1	
	(b)	- 1	1	
	(c)	- 1	1	
	(d)	Parabola vertex downwards and vertex below <i>x</i> -axis	M1	
		Cuts given graph in 5 places	A1	
9	(a)	11	1	
	(b)	$\frac{7}{2}$ or	1	
		23 00		
	(c)	110	3	M2 for $\frac{their(a)}{d(a)} \times \frac{their(a)-1}{d(a)}$
		$\overline{182}$ oe		their(a) + 3 their(a) + 2 or M1 for a single product of two
				fractions with first fraction <u>their (a)</u>
				their(a)+3
	(d)		1	

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Question		Answer	Mark	Part Marks
10	(a)	31	2	B1 for $[f(7) =]$ 12 or M1 for $2(x^2 - x - 30) + 7$
	(b)	$\frac{x-7}{2}$ oe	2	M1 for $y - 7 = 2x$ or $x = 2y + 7$ or $\frac{y}{2} = x + \frac{7}{2}$
	(c)	(2x+13)(2x+1) final answer	3	B2 for $(2x+7+6)(2x+7-6)$ or for $4x^2 + 28x + 13$ or M1 for $(2x+7)^2 - 36$
	(d)	$\frac{x+5}{x+6}$ final answer nfww	4	B2 for $(x-6)(x+5)$ or SC1 for $(x+a)(x+b)$ where ab = -30 or $a+b = -1$
				and B1 for $(x + 6)(x - 6)$
11	(a)	5.4[0] or 5.396	2	M1 for $\tan 34 = \frac{AB}{8}$ oe or better
	(b)	20.4 or 20.38 nfww	5	B1 for angle $D = 146$
				M2 for $[\sin C =] \frac{8\sin(theirD)}{19}$ or M1 for $\frac{8}{\sin C} = \frac{19}{\sin(theirD)}$ oe A1 for $[\text{angle } C =]$ 13.6 or 13.61 to 13.63 OR B1 for angle $A = 56$ M2 for $[\sin C =] \frac{their AB \times \sin(theirA)}{19}$ or M1 for $\frac{their AB}{\sin C} = \frac{19}{\sin(theirA)}$ oe A1 for $[\text{angle } C =]$ 13.6 or 13.61 to 13.63
	(c)	48[.0] or 48.1 or 48.04 to 48.12 cao	2	M1 for $0.5 \times their(a) \times 19 \times sin(90 + their(b))$ oe
12	(a)	n ³ cao	1	
	(b) (i)	392	2	B1 for second differences 14, 20, 26 and 32
	(ii)	$n^3 + n^2$ oe	2	M1 for cubic expression but not n^3 or kn^3 only