

Cambridge International Examinations Cambridge International General Certificate of Secondary Education

#### CAMBRIDGE INTERNATIONAL MATHEMATICS

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Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

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### MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

### **Types of mark**

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

### Abbreviations

answers which round to awrt correct answer only cao dep dependent follow through after error FT ignore subsequent working isw not from wrong working nfww or equivalent oe rounded or truncated rot Special Case SC seen or implied soi

Question	Answer	Marks	Part Marks
1(a)	Image at (0, 5), (3, 5), (3, 3)	2	<b>SC1</b> for translation $\begin{pmatrix} -2\\ k \end{pmatrix}$ or $\begin{pmatrix} k\\ 7 \end{pmatrix}$
1(b)(i)	Image at (2, 2), (5, 2), (5, 4)	1	
1(b)(ii)	Image at $(-4, -2)$ , $(-7, -2)$ , $(-7, -4)$	1	
1(b)(iii)	Rotation 180 [centre] (-1, 0)	3	B1 for each
1(c)	Stretch [factor]2 <i>x</i> -axis oe invariant	3	B1 for each
2(a)(i)	44	2	<b>M1</b> for [angle <i>BAC</i> or <i>DEC</i> =] $180 - 2 \times 68$ , so iby angle <i>CDE</i> = 44 or <b>M1</b> for angle <i>BAC</i> = <i>their</i> angle <i>CDE</i>
2(a)(ii)	isosceles	1	
2(b)	162	3	M2 for $180 - \frac{360}{20}$ or $\frac{180 \times (20 - 2)}{20}$ or M1 for $\frac{360}{20}$ or $180 \times (20 - 2)$
2(c)(i)	Angle sum of triangle oe	1	
2(c)(ii)(a)	similar	1	
2(c)(ii)(b)	5.4	2	M1 for $\frac{5}{3} = \frac{9}{QR}$ oe
3(a)(i)	6.5	1	
3(a)(ii)	4.5	1	
3(a)(iii)	3	1	
3(b)(i)	Positive	1	
3(b)(ii)	13	1	
3(b)(iii)	15.5	1	
3(b)(iv)	7.32 <i>t</i> – 55.3	2	(7.322  to  7.323)t - (55.25) <b>B1</b> for $7.32t + k$ or $kt - 55.3$ or <b>SC1</b> for $7.3t - 55$
3(b)(v)	Correct line (positive gradient and not below the <i>x</i> -axis)	2	<b>B1</b> for positive gradient

Question	Answer	Marks	Part Marks
4(a)(i)	5:4	2	B1 for any other correct ratio
4(a)(ii)	41.68	2	<b>M1</b> for 0.16 × 260.5[0] oe
4(a)(iii)	12.5[0]	3	<b>M2</b> for 11.25 ÷ 0.9 oe or <b>M1</b> for recognising 11.25 as 90%
4(a)(iv)	300 nfww	3	M2 for $\frac{200 \times 2 \times 25}{100} + 200$ oe or M1 for $\frac{200 \times 2 \times 25}{100}$ oe (implied by 100 nfww)
4(a)(v)	311.72	3	<b>M2</b> for $190 \times 1.02^{25}$ oe or <b>M1</b> for $190 \times 1.02^{n}$ oe where $n > 1$
4(b)	17	3	<b>B2</b> for 16.5 or 16.52 to 16.53 or <b>M2</b> for $\frac{\log(\frac{300}{120})}{\log 1.057}$ or appropriate sketch or 120 × 1.057 <sup>n</sup> = 300 <b>and</b> at least 2 trials which reach from 250 to 350 or <b>M1</b> for 120 × 1.057 <sup>n</sup> [= 300]
5(a)	804 or 804.2 to 804.4	3	M1 for $\frac{1}{3}\pi \times 8^2 \times 16$ M1 for $\frac{4}{3}\pi \times 4^3$
5(b)	450 or 449.5 to 449.6	3	<b>M2</b> for $\pi \times 8 \times \sqrt{8^2 + 16^2}$ or <b>M1</b> for $\sqrt{8^2 + 16^2}$ or $\pi \times 8 \times their l$

Question	Answer	Marks	Part Marks
5(c)	8.94 or 8.944	4	P is point of contact between slant edge and circle. B2 for $PV = 8$ nfww or M1 for $\frac{8}{4} = \frac{16}{PV}$ oe M1 for $OV^2 = 4^2 + PV^2$ OR B2 for $l = \sqrt{320}$ oe or M1 for $l^2 = 8^2 + 16^2$ M1 for $\frac{8}{4} = \frac{l}{OV}$ soi OR x is semi-vertical angle of cone M1 for $\tan x = \frac{8}{16}$ oe M2 for $\frac{4}{\sin x}$ or M1 for $\frac{4}{OV} = \sin x$
6(a)	Correct sketch	2	<b>B1</b> for correct shape
6(b)	(2.17, 0.488) or (2.171, 0.4877)	2	B1 for each
6(c)	$0.488 \le f(x) \le 1.51$ or $0.4877 \le f(x) \le 1.505$	2	<b>FT</b> <i>their</i> 0.488 <b>B1</b> for $0.488 \le f(x)$ oe or $f(x) \le 1.51$ oe
6(d)	0.502 or 0.5015 5.83 or 5.827	2	B1 for each
6(e)	0.502 < <i>x</i> < 5.83 or 0.5015 < <i>x</i> < 5.827	1	FT their (d)
6(f)(i)	15.[0] or 15.00 25.[0] or 25.00 35. [0] or 35.00	1	
6(f)(ii)	[an] asymptote oe	1	

Question	Answer	Marks	Part Marks
7(a)	9.77 or 9.766	3	M2 for $\frac{8}{\cos 35}$ oe or M1 for $\cos 35 = \frac{8}{4B}$ oe
			AB
7(b)	60.6 or 60.61	3	<b>M2</b> for $\frac{6^2 + 9^2 - 8^2}{2 \times 6 \times 9}$
			or <b>M1</b> for $8^2 = 6^2 + 9^2 - 2 \times 6 \times 9 \cos C$
8(a)	10	1	
8(b)	4	2	<b>M1</b> for $[h(1) = ]\frac{1}{2}$ or for
			$[gh(x) = ] 3 + 2\left(\frac{1}{x+1}\right)$
8(c)	$5x^2 + 12x + 11$	3	<b>M1</b> for $(3+2x)^2 + 1 + x^2 + 1$
			<b>B1</b> for $9+6x+6x+4x^2$ or better for $(3+2x)^2$
8(d)	$\frac{1}{x} - 1$ or $\frac{1 - x}{x}$ oe final answer	3	M1 correct first step M1 correct second step
8(e)(i)	- 1	2	<b>M1</b> for $3 + 2x = 1$
8(e)(ii)	5	1	
9(a)	15, 7, 12 correctly placed	2	<b>B1</b> for two correctly placed or <b>M1</b> for $41 - (40 - 6)$ seen oe or correct equation
9(b)(i)	7	1	FT their Venn diagram
9(b)(ii)	28	1	FT their Venn diagram
9(c)	15	1	FT their Venn diagram
9(d)	$\frac{462}{1560}$ oe	2	<b>M1</b> for $\frac{22}{40} \times \frac{21}{39}$
9(e)(i)	$\frac{7}{19}$	1	FT their Venn diagram
9(e)(ii)	$\frac{168}{342} \text{ oe}$	3	<b>M2</b> for $\frac{their7}{19} \times \frac{their12}{18} + \frac{their12}{19} \times \frac{their7}{18}$ oe or <b>M1</b> for one of these products
9(f)	8	3	M2 for $\frac{their 7 + n}{40 + n} = \frac{5}{16}$ oe or M1 for at least two trials

Question	Answer	Marks	Part Marks
9(g)		1	
10(a)(i)	3.0875	2	<b>M1</b> for 2.75, 3.125, 3.5 soi
10(a)(ii)	Correct histogram	3	B1 correct widths B1 for two correct heights
10(b)(i)	$\frac{200}{x} - \frac{200}{x+10} = \frac{20}{60} \text{ oe}$	B2	<b>B1</b> for $\frac{200}{x}$ or $\frac{200}{x+10}$
	$60 \times 200(x+10) - 60 \times 200x = 20x(x+10)$ oe	M1	i.e. correctly clearing fractions or all over common denominator
	$x^2 + 10x - 6000 = 0$	A1	completion with at least one interim line and without any errors or omissions
10(b)(ii)	2 h 45 min	4	<b>B2</b> for 72.6 or 72.62 or <b>M1</b> for correct use of formula or correct sketch <b>M1</b> for 200 $\div$ <i>their</i> positive <i>x</i> , implied by 2.75
11(a)(i)	$-\mathbf{a} + \mathbf{b}$ oe	1	
11(a)(ii)	$-\frac{1}{4}\mathbf{a} + \frac{1}{4}\mathbf{b} \text{ oe}$	1	FT their (i)
11(a)(iii)	$\frac{3}{4}\mathbf{a} + \frac{1}{4}\mathbf{b} \text{ oe}$	2	<b>B1</b> for correct unsimplified answer or a correct route
11(b)	(6.5, 1.5)	3	FT their (a)(iii)
			<b>B2</b> for $\begin{pmatrix} 6.5\\ 1.5 \end{pmatrix}$
			or M1 for $\frac{3}{4} \times \begin{pmatrix} 8 \\ 0 \end{pmatrix} + \frac{1}{4} \times \begin{pmatrix} 2 \\ 6 \end{pmatrix}$
			OR
			<b>B2</b> for (5, 3) at <i>M</i> or $[\overrightarrow{OM} = ] \begin{pmatrix} 5\\ 3 \end{pmatrix}$ or <b>B1</b> for ( <i>k</i> , 3) or (5, <i>k</i> ) at <i>M</i>
			or $[\overline{OM} = ] \begin{pmatrix} k \\ 3 \end{pmatrix}$ or $\begin{pmatrix} 5 \\ k \end{pmatrix}$