## Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

## CANDIDATE NAME



CENTRE NUMBER


## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/51
Paper 5 (Core)
October/November 2018
1 hour
Candidates answer on the Question Paper.
Additional Materials: Graphics Calculator

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
Do not use staples, paper clips, glue or correction fluid.
You may use an HB pencil for any diagrams or graphs.
DO NOT WRITE IN ANY BARCODES.
Answer all the questions.
You must show all relevant working to gain full marks for correct methods, including sketches.
In this paper you will also be assessed on your ability to provide full reasons and to communicate your mathematics clearly and precisely.
At the end of the examination, fasten all your work securely together.
The total number of marks for this paper is 24 .

Answer all the questions.

## INVESTIGATION

## DOTS IN RECTANGLES

This investigation looks at the number of dots inside rectangles drawn on square dotty paper.

1 Rectangles with a height of 1 unit have no dots inside.

height 1 width 1 height 1 width 2

. . .

> height 1
> width 3
height 1 width 4
(a) (i) These rectangles all have a height of 2 units.

height 2 width 1

height 2 width 2

height 2
width 3

height 2 width 4

Complete the table.

| Height of rectangle <br> $(h)$ | Width of rectangle <br> $(w)$ | Number of dots inside rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 2 | 1 |  |
| 2 | 2 |  |
| 2 | 3 |  |
| 2 | 4 |  |

(ii) Find an expression, in terms of $w$, for the number of dots, $d$, inside rectangles of height 2 .
(b) Complete the tables below.

You may use the square dotty paper on this page to help you.

| Height of rectangle <br> $(h)$ | Width of rectangle <br> $(w)$ | Number of dots inside rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 3 | 1 |  |
| 3 | 2 |  |
| 3 | 3 |  |
| 3 | 4 |  |
| 3 | $w$ | $2(w-1)$ |


| Height of rectangle <br> $(h)$ | Width of rectangle <br> $(w)$ | Number of dots inside rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 4 | 1 |  |
| 4 | 2 |  |
| 4 | 3 |  |
| 4 | 4 |  |
| 4 | $w$ |  |

(c) (i) Find a formula, in terms of $h$ and $w$, for the number of dots, $d$, inside a rectangle of height $h$ and width $w$.

$$
d=
$$

(ii) Use your formula in part (i) to show that there are 30 dots inside a rectangle of height 6 and width 7.
(iii) There are 33 dots inside a rectangle.

Find the height and the width of this rectangle.

2 (a) Squares are formed when $h=w$.
Change your formula in question $\mathbf{1 ( c ) ( i )}$ to find the number of dots, $d$, inside a square of side $s$.
(b) Find the number of dots inside a square of side 10 .

3 The rectangles below are drawn at an angle of $45^{\circ}$ to the horizontal.
They are called diagonal rectangles.
The diagonal lines between the dots give the height and the width of the diagonal rectangles.

(a) Complete the tables below.

| Height of diagonal <br> rectangle <br> $(h)$ | Width of diagonal <br> rectangle <br> $(w)$ | Number of dots inside <br> diagonal rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 1 | 1 | 1 |
| 1 | 2 | 2 |
| 1 | 3 | 3 |
| 1 | 4 |  |


| Height of diagonal <br> rectangle <br> $(h)$ | Width of diagonal <br> rectangle <br> $(w)$ | Number of dots inside <br> diagonal rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 2 | 1 | 2 |
| 2 | 2 |  |
| 2 | 3 |  |
| 2 | 4 |  |
| 2 | $w$ | $3 w-1$ |


| Height of diagonal <br> rectangle <br> $(h)$ | Width of diagonal <br> rectangle <br> $(w)$ | Number of dots inside <br> diagonal rectangle <br> $(d)$ |
| :---: | :---: | :---: |
| 3 | 1 |  |
| 3 | 2 |  |
| 3 | 3 |  |
| 3 | 4 |  |

(b) Use your results from part (a) and any patterns you notice to complete the following table with expressions, in terms of the width $w$, for the number of dots inside diagonal rectangles.

| Height of diagonal <br> rectangle <br> $(h)$ | Number of dots inside <br> diagonal rectangle <br> $(d)$ |
| :---: | :---: |
| 1 | $3 w-1$ |
| 2 |  |
| 3 | $9 w-4$ |
| 4 |  |
| 5 |  |

(c) (i) Find a formula, in terms of $h$ and $w$, for the number of dots, $d$, inside a diagonal rectangle.
(ii) Use your formula in part (i) to find the number of dots inside the diagonal rectangle of height 10 and width 3 .

4 (a) Diagonal squares are formed when $h=w$.
Change your formula in question 3(c)(i) to find the number of dots, $d$, inside a diagonal square of side $s$.
(b) There are 181 dots in a diagonal square. Find the length of one side.

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