# Cambridge IGCSE<sup>™</sup>

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# **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/42

Paper 4 (Extended)

February/March 2021

2 hours 15 minutes

You must answer on the question paper.

You will need: Geometrical instruments

#### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly and you will be given marks for correct methods, including sketches, even if your answer is incorrect.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For  $\pi$ , use your calculator value.

#### **INFORMATION**

- The total mark for this paper is 120.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 20 pages. Any blank pages are indicated.

### Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$

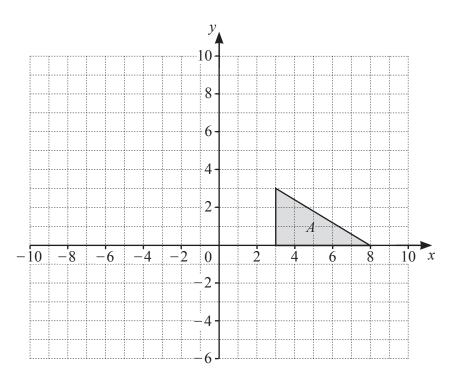
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$Area = \frac{1}{2}bc\sin A$$

# Answer all the questions.

1 (a)



(i) Rotate triangle A through  $90^{\circ}$  anticlockwise about (0, 0). Label the image B. [2]

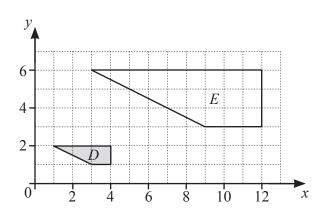
(ii) Reflect triangle A in the y-axis. Label the image C. [1]

(iii) Describe fully the **single** transformation that maps triangle B onto triangle C.

.....

......[2

**(b)** 



Describe fully the **single** transformation that maps trapezium D onto trapezium E.

2	(a)	Wri	ite 260 512 correct to 3 significant figures.		
					[1]
	(b)	Wri	ite 0.000 000 576 in standard form.		
	(c)		lculate $\sqrt{27^2 - 6 \times 31^{0.3}}$ . we your answer correct to 1 decimal place.		[1]
	(d)	(i)	Work out 37% of \$820.		[2]
		(ii)	Work out \$36 as a percentage of \$150.	\$	[2]
		(11)	work out \$50 as a percentage of \$150.		
	(e)		amount of money is shared between Alan, Bjorn and Carl- rlo receives \$695.	o in the ratio 3 : 7 : 5.	[1]
		(i)	Find the total amount of money shared.		
			;	\$	[3]
		(ii)	Carlo invests 40% of his \$695 at a rate of 1.2% per year	compound interest.	
			Calculate the value of his investment at the end of 5 years	rs.	
			:	\$	[3]

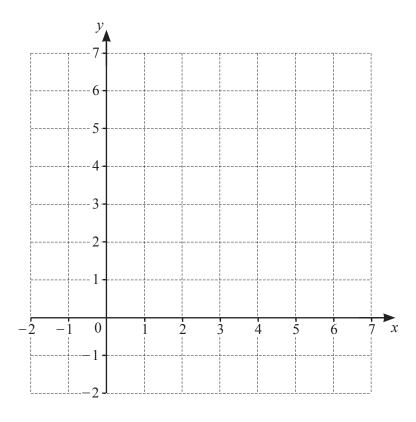
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(f)	Dana invests \$2100 for 12 years at a rate of $x\%$ per year compound interest. At the end of the 12 years, the value of her investment is \$2663.31.
	Calculate the value of $x$ .

x = [3]

3	(a)	(i)	Write down the coordinates of the point where the line $y = -2x + 3$ crosses the y-axis.
			(, ,
		(ii)	Write down the gradient of the line $y = -2x + 3$ .
			[1]
	(b)	The	line $x+y=6$ crosses the line $x=-2$ at point A.
		Fino	If the $y$ -coordinate of $A$ .
			[1]
	(c)	Fino	If the equation of the straight line that passes through the points $(3, -1)$ and $(12, 5)$ .
			[3]
	(d)	The Line	line L passes through the point $(3, 4)$ . e L is perpendicular to the line $2y = 5x + 6$ .
		Fino	If the equation of line $L$ .
			[4]

**(e)** 



- (i) On the grid, draw the lines y = 4, x + y = 3 and y = x 1. [3]
- (ii) By shading the unwanted regions, find and label the region R that satisfies these three inequalities.

$$y \le 4$$

$$x+y \ge 3$$

$$y \ge x-1$$
[1]

4 (a) The mass, m grams, of each of 50 apples is found. The results are shown in the table.

Mass (m grams)	Frequency
$70 < m \leqslant 90$	2
90 < <i>m</i> ≤ 110	7
$110 < m \le 130$	14
$130 < m \leqslant 150$	10
$150 < m \leqslant 170$	12
$170 < m \le 190$	5

(i) Write down the modal class.

..... 
$$< m \le .....$$
 [1]

(ii) Calculate an estimate of the mean.

Cumulative Frequency

8

- **(b)** The mass, *x* grams, of each of 120 different apples is found. The results are shown in Table 1.
  - (i) Complete the cumulative frequency column in Table 2.

Mass (x grams)	Frequency
$70 < x \le 90$	8
90 < <i>x</i> ≤ 110	8
$110 < x \le 120$	22
$120 < x \le 130$	39
$130 < x \le 140$	27
$140 < x \le 150$	9
$150 < x \le 170$	7

	Table 2
<i>x</i> ≤ 170	
<i>x</i> ≤ 150	

Table 1 Table 2 [2]

Mass (x grams)

 $x \le 90$ 

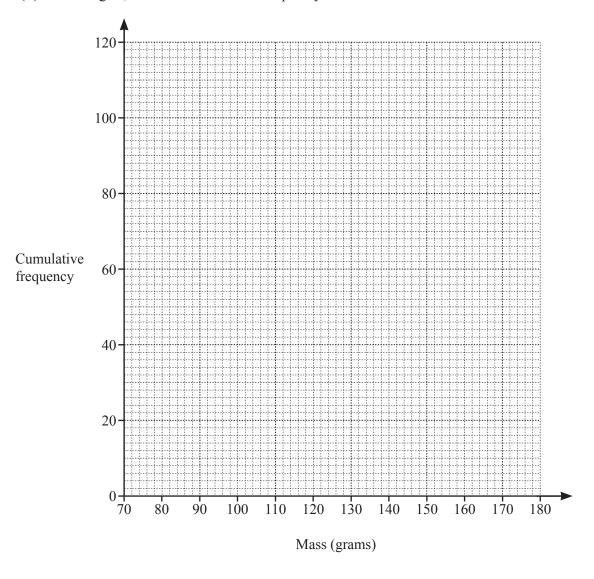
 $x \le 110$ 

*x* ≤ 120

*x* ≤ 130

*x* ≤ 140

(ii) On the grid, draw the cumulative frequency curve to show the results in Table 2.



(iii) Use your cumulative frequency curve to estimate

(a) the median,

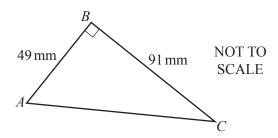
\_\_\_\_\_\_ g [1]

[3]

**(b)** the interquartile range.

..... g [2]

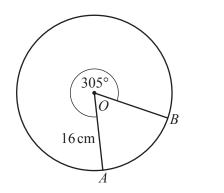
5 (a)



Calculate the length of AC.

 $AC = \dots mm [2]$ 

**(b)** 

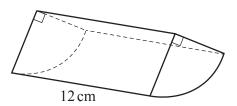


NOT TO SCALE

The diagram shows a circle with centre O and radius 16 cm.

Calculate the length of the major arc AB.

(c)



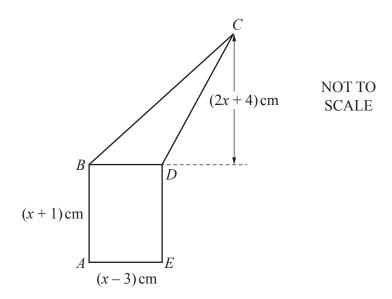
NOT TO SCALE

The diagram shows a prism with length 12 cm. The cross-section of the prism is a quarter of a circle. The radius of the circle is 6 cm.

Calculate the volume of the prism.

..... cm<sup>3</sup> [2]

**(d)** 



Shape ABCDE is made by joining rectangle ABDE and triangle BCD. The perpendicular height of triangle BCD is (2x + 4) cm. The total area of ABCDE is  $11 \text{ cm}^2$ .

(i) Show that  $2x^2 - 3x - 20 = 0$ .

[3]

(ii) Factorise  $2x^2 - 3x - 20$ .

.....[2]

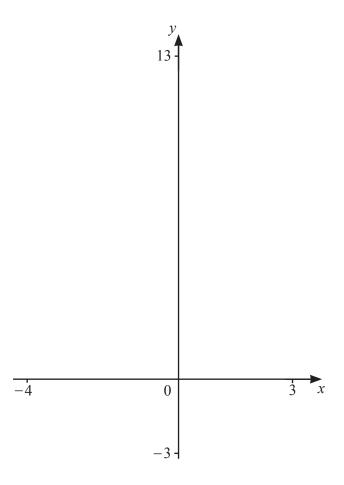
(iii) Use your answer to part (ii) to solve the equation  $2x^2 - 3x - 20 = 0$ .

x = or x = [1]

(iv) Find the perpendicular height of triangle *BCD*.

......cm [1]

6	(a) $y$ is inversely proportional to the square of $x$ .	
	(i) When $x = 2$ , $y = 8$ .	
	Find $y$ in terms of $x$ .	
		y =  [2]
	(ii) Find the value of y when $x = 4$ .	
		y =  [1]
	(iii) Find the value of x when $y = 128$ .	
		$x = \dots $ [2]
	(b) $r$ is directly proportional to the cube of $(p + 1)$ . When $p = 1$ , $r = 16$ .	
	Find the value of $r$ when $p = 4$ .	
		r =  [3]



$$g(x) = \frac{1}{x-2} , \quad x \neq 2$$

- (a) On the diagram, sketch the graph of y = g(x) for values of x between -4 and 3. [3]
- **(b)** Write down the equations of the asymptotes of the graph of y = g(x).

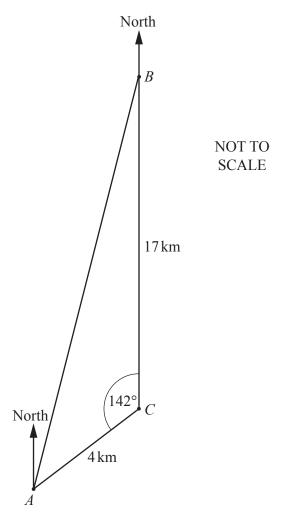
.....

.....[2]

(c)  $h(x) = (x+1)^2 - 3$ 

Solve the inequality g(x) > h(x).

.....[4]



Rani sails in a boat race around a triangular course. She sails from A to B to C and then directly back to A. B is due north of C.

(a) Find the bearing Rani sails on from C to A.

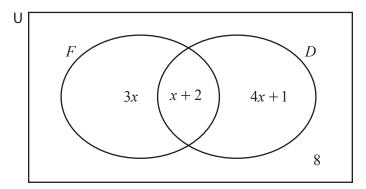
.....[1]

**(b)** Show that AB = 20.3 km, correct to 1 decimal place.

	13		
(c)	Calculate the bearing of $B$ from $A$ .		
( I)	D : 4 4 4 1222		[3]
(d)	Rani starts the race at 08 57 and returns to <i>A</i> at 12 33.		
	Calculate the average speed of her boat in km/h.		
		km/h	[3]

9	(a)	The Venn	diagram	shows	informa	ation abo	ut 115	neor	ole who	nlay	musical	instrument	S
	(44)	I IIC VCIIII	aragram		IIIIOIIII	illoll abo	ut IIJ	POOP	710 77110	piu	illusicui	IIIou aillett	v.

 $F = \{ \text{people who play the flute} \}$  $D = \{ \text{people who play the drums} \}$ 



(i) Calculate the number of people who play both the flute and the drums.

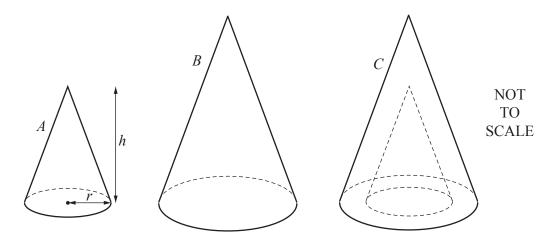
	[3]
•••••	[~]

- (ii) On the Venn diagram, shade  $F' \cap D$ . [1]
- (iii) Briony plays both the flute and the drums.

Use set notation to complete the statement.

Briony ...... 
$$(F \cap D)$$
 [1]

(b)	Brio	ony has 6 red socks, 4 green socks and 8 white socks.	
	(i)	She picks a sock at random.	
		Find the probability that the sock is green.	
			[1]
	(ii)	Briony replaces the sock. She now picks two socks at random, without replacement.	
		Calculate the probability that the two socks are different colours.	
			[4]



Cone A has radius r and perpendicular height h. Cone B is mathematically similar to cone A. Solid C is formed by removing cone A from cone B.

The ratio height of cone A: height of cone B = 2:3.

(a) Find the ratio volume of cone A: volume of solid C.

.....[3]

(b)	Cone A has radius 4 cm and height 10 cm.				
	Calculate the <b>total</b> surface area of solid <i>C</i> .				
		cm <sup>2</sup> [8]			
	Ouestion 11 is printed on the next page.				

11 
$$f(x) = 3x + 1$$
  $g(x) = x^2 - 5$   $h(x) = 3^x$ 

(a) Find g(3).

**(b)** Find f(h(2)).

(c) Find the value of r when f(r) = r.

$$r = \dots [2]$$

(d) Solve g(f(x)) = 20.

$$x =$$
 or  $x =$  [3]

(e) Find  $h^{-1}(x)$ .

$$h^{-1}(x) = \dots [2]$$

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