

Cambridge IGCSE™

CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 4 (Extended) MARK SCHEME Maximum Mark: 120 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2021 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

© UCLES 2021 Page 2 of 9

Ma	Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

© UCLES 2021 Page 3 of 9

Question	Answer	Marks	Partial Marks
1(a)	32.4	3	M2 for $\frac{250-6.5\times26}{250}[\times100]$ oe or $\frac{6.5\times26}{250}\times100$ or M1 for $250-6.5\times26$ soi by 81 or $\frac{6.5\times26}{250}$
1(b)	320	2	M1 for $() \times \left(1 + \frac{24}{100}\right) = 396.8$ or better
1(c)	23	4	B3 for 22.49 or 22.5 or 22 as answer or M3 for $n \log \left(1 - \frac{3}{100}\right) = \log \left(\frac{200}{396.8}\right)$ oe or correct trials as far as 22 and 23 or sketch indicating value between 22 and 23 or M2 for $\left(1 - \frac{3}{100}\right)^n = \frac{200}{396.8}$ oe or at least 3 correct trials or a sketch that could lead to solution e.g. $y = 0.97^x$ and $y = 200$ or M1 for $396.8 \times \left(1 - \frac{3}{100}\right)^n = 200$ soi. or at least 2 correct trials
2(a)(i)	Triangle at (-2, 4), (0, 4), (0, 5)	2	B1 for rotation 90° clockwise about (-1, 2) or rotation anticlockwise 90° about wrong centre
2(a)(ii)	Stretch [Factor] 2 Invariant [line] $y = -1$ oe	3	B1 for each
2(b)	Translation $\begin{pmatrix} 8 \\ 0 \end{pmatrix}$	2	B1 for each
3(a)	$100 < m \leqslant 120$	1	
3(b)	$60 < m \leqslant 80$	1	
3(c)	Any correct statement	1	

Question	Answer	Marks	Partial Marks
3(d)	Correct labelled pie chart (labels indicating masses)	4	B3 for pie chart with all angles correct or B2 for pie chart with two angles correct or B1 for 2 correct angles calculated B1 for correct labels on sectors.
4(a)	Correct sketch	2	B1 for correct middle section
4(b)	± 4 ± 2	2	B1 for 2 correct solutions
4(c)	x < -4 $-2 < x < 2$ $x > 4$	3	B1 for each
4(d)	0 [k] > 10	2	B1 for each
5(a)	$20^2 + 10^2$	M1	
	22.360 to 22.361	A1	
5(b)	$\tan 35 = \frac{10}{AB} \text{oe}$	M1	$\frac{\sin 35}{10} = \frac{\sin 55}{AB}$, i.e correct implicit
	14.281	A1	
5(c)	17.4 or 17.43	2	M1 for $\sin 35 = \frac{10}{AP}$ oe or $14.28^2 + 10^2$
5(d)	30.5 or 30.52	3	M1 for $20^2 + 14.28^2 - 2 \times 20 \times 14.28 \times \cos 125$ A1 for 931.5 to 931.6
5(e)	99.2 to 99.5	3	M2 for [cos =] $\frac{22.36^{2} + (their 17.4)^{2} - (their 30.5^{2})}{2 \times 22.36 \times (their 17.4)}$ or M1 for $(their 30.5)^{2} = 22.36^{2} + (their 17.4)^{2}$ $-2 \times 22.36 \times (their 17.4) \times \cos APB$

Question	Answer	Marks	Partial Marks
6(a)(i)	31.9	1	
6(a)(ii)	0.55	2	M1 for [UQ =] 32.1 or [LQ =] 31.55 seen
6(a)(iii)	32.15	2	B1 for 128 seen
6(b)(i)	Lower median (average) oe	1	
6(b)(ii)	Smaller IQR oe	1	
7(a)	$\frac{200}{x}$	1	
7(b)	$\frac{200}{x} + \frac{50}{x - 40} = \frac{7}{2}$ oe	M1	
	400(x-40) +100x = 7x(x-40) oe	M2	FT only an equation of the correct form with equivalent difficulty M1FT for $\frac{200(x-40)+50x}{x(x-40)}$ or better
	Completion to $7x^2 - 780x + 16000 = 0$ with no errors or omissions	A1	With at least one intermediate step
7(c)	2 [h] 22 [min]	5	B4 for 2.37 or 2.371 to 2.372 or 2h 22 to 22.3 min or 142 to 142.3 or B3 for 27.1 or 27.10 to 27.11 and 84.3 or 84.3, or M2 for $\frac{-(-780) \pm \sqrt{(-780)^2 - 4 \times 7 \times 16000}}{2 \times 7}$ or sketch of parabola (positive x^2) with two positive zeros or M1 for $\sqrt{(-780)^2 - 4 \times 7 \times 16000}$ or $\frac{-(-780) \pm \sqrt{p}}{2 \times 7}$ and M1 for $200 \div their$ solution from their quadratic if > 40
8(a)(i)	$0.05 = \frac{k}{\sqrt{25}} \text{oe}$	M1	
	$k = 0.25 \text{ and } y = \frac{1}{4\sqrt{x}}$	A1	

Question	Answer	Marks	Partial Marks
8(a)(ii)	$[\pm]\frac{1}{12}$ oe	1	
8(a)(iii)	$\frac{1}{16y^2} \text{ or } \frac{1}{\left(4y\right)^2} \text{ oe}$	2	M1 for $4y\sqrt{x} = 1$ or better or for $y^2 = \frac{1}{16x}$
8(a)(iv)	$\frac{1}{4}$ oe cao	1	
8(b)	3	2	B1 for 2 ³ soi
9(a)	204 or 204.2	3	M2 for $\pi \times 5 \times \sqrt{(5^2 + 12^2)}$ or M1 for $5^2 + 12^2$ (implied by 13)
9(b)(i)	$\frac{r}{12-r} = \frac{5}{their13}$ oe	M1	$\frac{r}{13-5} = \frac{5}{12}$
	$r(their\ 13) = 5(12 - r)$	M1	M1 dep on first M1 for $12r = 5(13-5)$
	Completion to $r = 3.\dot{3}$ or $3\frac{1}{3}$ or $\frac{10}{3}$ or 3.333 with no errors	A1	
9(b)(ii)	159 or 159.0 to 159.5	3	M1 for $\frac{1}{3} \times \pi \times 5^2 \times 12$ M1 for $\frac{4}{3} \times \pi \times 3.33^3$
10(a)	(0.7) 0.25 oe 0.05 oe	B1	
	0.2 oe 0.4 oe (0.55) 0.25 oe	B1	
10(b)(i)	0.13 oe	3	M2 for $0.6 \times their \ 0.05 + their \ 0.4 \times their \ 0.25$ oe or M1 for one of above products

Question	Answer	Marks	Partial Marks
10(b)(ii)	0.63 oe	3	M2 for <i>their</i> (b)(i) + 0.6 × 0.7 + <i>their</i> 0.4 × <i>their</i> 0.2 or M1 for 0.6 × 0.7 + <i>their</i> 0.4 × <i>their</i> 0.2
			OR
			M2 for $0.6 \times their 0.75$ + their $0.4 \times their 0.45$ oe or M1 for one of above products
			OR
			M2 for $1 - 0.6 \times their \ 0.25$ - their 0.4×0.55 or M1 for $0.6 \times their \ 0.25$ and their 0.4×0.55
10(c)	0.36[0] or 0.3601 to 0.3602 oe	3	M2 for $5 \times 0.7^4 \times 0.3$ oe or M1 for $0.7^4 \times 0.3$ oe
11(a)	8-2=10, 3: 2=6:4, x=-2+6=4 oe	M2	M1 for each coordinate
	4 to -1 = 5, y = 4 - 3 = 1 oe		
11(b)	y = 2x - 7 oe final answer	4	B3 for $2x - 7$ as final answer
			OR 1 4
			M1 for gradient of $AB = \frac{-1-4}{8-(-2)}$
			M1 for $m = \frac{-1}{their\left(-\frac{1}{2}\right)}$
			M1 for $1 = (their2) \times 4 + c$ or $y - 1 = their2(x - 4)$
11(c)	$2 \times 6 - 7 = 5$ oe	1	
11(d)(i)	$5\sqrt{5}$ or $\sqrt{125}$ final answer	2	M1 for $(8 - (-2))^2 + ((-1) - 4)^2$ oe
11(d)(ii)	25 [.0] cao nfww	3	M1 for $(6-4)^2 + (5-1)^2$ M1 dep on first M1 for $\frac{1}{2} \times their(d)(i) \times their\sqrt{20}$
12(a)	-10	1	
12(b)	$\frac{1}{4}$ oe	3	M2 for $5 = 8 - 12x$ oe or M1 for $\frac{5}{2 - 3x} = 4$

Question	Answer	Marks	Partial Marks
12(c)	$\frac{2-x}{3}$ oe	2	M1 for $3x + y = 2$ or $x = 2 - 3y$ or $\frac{y}{3} = \frac{2}{3} - x$ or better
12(d)	$\frac{5}{-4+9x}$ oe final answer	2	M1 for $\frac{5}{2-3(2-3x)}$
12(e)	$\frac{9x^2 - 12x - 1}{2 - 3x}$ oe final answer	3	M1 for $\frac{(2-3x)(2-3x)-5}{2-3x}$ B1 for $4-6x-6x+9x^2$
13(a)	Correct sketch	3	B1 for each branch
13(b)	x = 1, $x = -3$	2	B1 for each
13(c)	-3.79 or -3.791 -1 0.791 or 0.7912 to 0.7913	3	B1 for each If 0 scored SC1 for $y = 2x + 3$ sketched and cutting both axes