## Cambridge IGCSE ${ }^{\text {TM }}$

CANDIDATE NAME

CENTRE NUMBER


## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/52
Paper 5 Investigation (Core)

You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.


## INFORMATION

- The total mark for this paper is 36 .
- The number of marks for each question or part question is shown in brackets [ ].

Answer all the questions.

## INVESTIGATION

## DOT PATTERNS

This investigation looks at patterns in sequences of dots, and of dots and crosses.
1 This is a sequence of dot patterns.

(a) Draw Pattern 4.
(b) Complete the table.

| Pattern number, $n$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of dots | 2 | 3 | 4 |  |  |  |

(c) How many dots are in Pattern 9?
(d) Write down an expression, in terms of $n$, for the number of dots in Pattern $n$.
$\qquad$
(e) Find the number of the pattern that has 26 dots.

2 This is another sequence of dot patterns.
Pattern 1
Pattern 2
Pattern 3

(a) Complete the table.

You may use the grid below to help you.

| Pattern number, $n$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of dots |  |  |  |  |  | 21 |


(b) Find an expression, in terms of $n$, for the number of dots in Pattern $n$.
(c) Work out the number of dots in Pattern 40.

3 (a) Oliver draws this sequence of patterns called centred squares.

Pattern 1
Pattern 2
Pattern 3

(i) Pattern 3 is drawn on the grid.

Complete the diagram to show Pattern 4.

(ii) Complete the table.

| Pattern number, $n$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of dots | 1 | 5 | 13 |  |  |

(iii) Work out the number of dots in Pattern 6.
(b) Oliver draws the patterns of centred squares using dots and crosses.

## Pattern 1

Pattern 2
Pattern 3

Pattern 4

(i) Pattern 4 is drawn on the grid.

Complete the diagram to show Pattern 5.

(ii) Complete the table.

| Pattern number, $n$ | Number of dots | Number of crosses | Total number <br> of dots and crosses |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 1 |
| 2 | 1 | 4 | 5 |
| 3 | 9 | 4 | 13 |
| 4 |  | 16 |  |
| 5 |  |  |  |
| 6 |  |  |  |

(iii) Complete the table.

| Pattern number, $n$ | Number of dots | Number of crosses | Total number <br> of dots and crosses |
| :---: | :---: | :---: | :---: |
| 1 | $1=1^{2}$ | $0=0^{2}$ | $1^{2}+0^{2}=1$ |
| 2 | $1=1^{2}$ | $4=2^{2}$ | $2^{2}+1^{2}=5$ |
| 3 | $9=3^{2}$ | $4=2^{2}$ | $3^{2}+2^{2}=13$ |
| 4 |  | $16=$ |  |
| 5 |  |  |  |
| 6 |  |  |  |

(iv) Complete the formula for the total number of dots and crosses, $T$, in Pattern $n$.

$$
T=
$$

4 Sophia draws the patterns of centred squares using dots and crosses in a different way.

## Pattern 1

Pattern 2
Pattern 3

(a) Complete the table.

| Pattern number, $n$ | Number of dots | Number of crosses | Total number <br> of dots and crosses |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 0 | 1 |
| 2 | 5 | 0 | 5 |
| 3 | 9 | 4 | 13 |
| 4 | 13 |  | 25 |
| 5 |  |  |  |

(b) Complete the table.

| Pattern <br> number, $n$ | Number <br> of dots | Number of crosses | Total number <br> of dots and crosses |
| :---: | :---: | :--- | :--- |
| 1 | 1 | $0=4 \times 0$ | $1+4 \times 0=1$ |
| 2 | 5 | $0=4 \times 0$ | $5+4 \times 0=5$ |
| 3 | 9 | $4=4 \times 1$ | $9+4 \times 1=13$ |
| 4 | 13 | $12=4 \times(1+2)$ | $13+4 \times(1+2)=25$ |
| 5 |  | $=4 \times(1+2+\quad)$ | + |
| 6 |  |  |  |

(c) (i) In Sophia's patterns, Pattern $k$ has 112 crosses.

Find the value of $k$.

$$
\begin{equation*}
k= \tag{3}
\end{equation*}
$$

(ii) Work out the total number of dots and crosses in Pattern $k$.

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