

Cambridge IGCSE™

CAMBRIDGE INTERNATIONAL MATHEMATICS Paper 4 (Extended) May/June 2022 MARK SCHEME Maximum Mark: 120 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2022 series for most Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of **9** printed pages.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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Question	Answer	Marks	Partial Marks
1(a)	correct triangle (-4, 1) (-3, 1) (-3, 1.5)	2	B1 for translation $\binom{k}{2}$ or $\binom{-2}{k}$ or translation through $\binom{-1}{1}$
1(b)	correct triangle (-1, 1.5) (-1, 2) (-2, 2)	2	B1 for reflection in either $y = k$ or $x = 0.5$
1(c)	Rotation 180° (1, -1.5)	3	B1 for each
1(d)	correct triangle (3, 1) (3, 2) (1, 1)	2	B1 for any enlargement scale factor –2
2(a)(i)	31	1	
2(a)(ii)	260	2	B1 for 40 seen
2(a)(iii)	27	2	M1 for $\frac{70}{100} \times 300$ soi or $\frac{30}{100} \times 300$
2(b)	33.1	2	M1 for at least three mid-values soi
2(c)(i)	y = 0.618x + 13.6	2	B1 for $0.618x + k$ or $kx + 13.6$ or $0.62x + 14$
2(c)(ii)	positive	1	
2(c)(iii)	32 or 32.0 to 32.6	1	FT their (c)(i) if linear eqn
3(a)	correct sketch	3	B2 for correct branches but joined or touching y-axis B1 for one correct branch
3(b)	x = 0	1	
3(c)	(-1, 1)	1	

Question	Answer	Marks	Partial Marks
3(d)	$-2.31 \le x < 0 \text{ and } 0 < x \le 0.388$	4	B3 for $-2.3 \le x \le 0.388$ or $-2.31 \le x \le 0.39$ or B2 for $-2.3 \le x \le 0.39$
			or $-2.31 \le x$ or $x \le 0.388$
			or B1 for – 2.31 or 0.388 seen or for correct sketch
4(a)	180	2	M1 for $\frac{216}{5+1}[\times 5]$
4(b)	741	2	M1 for $\frac{171}{3}$
4(c)	1505	3	M2 for $1400 + 3(1400 \times \frac{2.5}{100})$ oe
			or M1 for $3(1400 \times \frac{2.5}{100})$ oe
4(d)(i)	3247.30 or 3250	2	M1 for $3000 \times \left(1 + \frac{2}{100}\right)^4$ oe
4(d)(ii)	15	4	B3 for 14.5 or 14.52 to 14.53 seen
			or M3 for $n \log(1.02) = \log\left(\frac{4000}{3000}\right)$ oe
			or for correct trials reaching 14 and 15 or good sketch indicating value between 14 and 15
			or M2 for $1.02^n = \frac{4000}{3000}$
			or at least three correct trials for n > 4 or suitable graph
			or M1 for $3000 \times 1.02^n = 4000$ soi by at least 2 correct trials for $n > 4$
5(a)	14 18 4 <i>n</i> + 2 oe	6	or B1 for at least two correct
	$\boxed{6 \qquad \boxed{12 \qquad \qquad n^2 - n \text{ oe}}}$		B2 for $4n + 2$ oe or M1 for $4n + k$
			B2 for $n^2 - n$ oe or M1 for any quadratic or for second differences of 2 seen
5(b)	$n^2 + 3n + 2$ or $(n+1)(n+2)$	1	FT <i>their</i> grey + white if both in terms of <i>n</i>

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Question	Answer	Marks	Partial Marks
5(c)	94	4	M1 for their $k^2 + 3k + 2 = 600$ oe M1 for correct method for solving their quadratic M1 for substituting their positive integer (from a quadratic) k into their 4n+2
5(d)	$\frac{343}{1728}$ oe	2	M1 for $\left(1 - \frac{5}{12}\right)^3$ oe
5(e)	$\frac{56}{153}$ oe	3	FT their 18 from (a) for M marks only M2 for $\frac{4}{18} \times \frac{14}{17} + \frac{14}{18} \times \frac{4}{17}$ oe M1 for one product
6(a)	26.5 or 26.47 to 26.48	4	B1 for $\angle AOC = 150$ or $\angle BOC = 75$ soi M1 for $\frac{their150 \times \pi \times 5^2}{360}$ or $\frac{their75 \times \pi \times 5^2}{360} \times 2$ M1 for $\frac{1}{2} \times 5 \times 5 \times \sin[their150]$ or $\frac{1}{2} \times 5 \times 5 \times \sin[their75 \times 2]$
6(b)	5.5[0] or 5.49 to 5.51	5	M2 for $\frac{(360-40)}{360} \times 2 \times \pi \times 12 = 2\pi r$ oe or $\frac{(360-40)}{360} \times \pi \times 12^2 = \pi r 12$ oe or M1 for $\frac{(360-40)}{360} \times 2 \times \pi \times 12$ or $\frac{(360-40)}{360} \times \pi \times 12^2$ If minor sector SC1 for radius = $\frac{4}{3}$ oe AND M2 for $12^2 - their(radius)^2$ oe dependent on at least M1 or SC1 or M1 for $h^2 + their(radius)^2 = 12^2$ oe dependent on at least M1 or SC1
7(a)	2300	2	M1 for $2 \times 23 \times 50$ oe

Question	Answer	Marks	Partial Marks
7(b)(i)	4.6	3	M2 for $1.15 \times \sqrt[3]{\frac{18400}{287.5}}$ oe or M1 for $\frac{h^3}{1.15^3} = \frac{18400}{287.5}$ or $\sqrt[3]{\frac{18400}{287.5}}$ or $\sqrt[3]{\frac{287.5}{18400}}$ seen
7(b)(ii)	2 : their (b)(i) or their (a) : 18400 soi	M1	FT their figures
	showing comparison of length ratio or volume ratio	M1	
	not similar	A1	Dep on M1M1
8(a)	27.6 or 27.58 to 27.59	3	M2 for $((-11)-8)^2 + (7-(-13))^2$ oe or M1 for $((-11)-8)$ or $(7-(-13))$ oe
8(b)	$y = -\frac{1}{4}x + 8\frac{1}{4}$ oe	6	B5 for answer $-\frac{1}{4}x + 8\frac{1}{4}$ OR B2 for (5, 7) or B1 for (5, k) or (k, 7) M1 for $\frac{115}{6 - 2}$ oe (=m ₁) M1 for grad = $-\frac{1}{their m_1}$ M1 for substituting their (5, 7) into $y = (their m)x + c$
9(a)(i)	13	1	
9(a)(ii)	-8x-10 oe final answer	2	M1 for $2-4(2x+3)$ or better seen
9(a)(iii)	$\frac{2-x}{4}$ oe final answer	2	M1 for correct first step $y + 4x = 2 \text{ or } \frac{y}{4} = \frac{1}{2} - x \text{ or } x = 2 - 4y$ $y - 2 = -4x$
9(a)(iv)	$3.52 \text{ or } 3.523 \text{ to } 3.524 \text{ or } \log_3 48 \text{ or } \frac{\log 48}{\log 3}$	2	M1 for $\log 48 = \log 3^x$ or better or suitable sketch

Question	Answer	Marks	Partial Marks
9(b)(i)	5 5	1	
9(b)(ii)	2m(x)	1	
10(a)	$16xy^2$ Final answer	2	M1 for $\frac{4x^2y}{3} \times \frac{12y}{x}$ or better
10(b)	$\frac{-x^2 + 6x - 7}{2(x - 3)}$ Final answer	3	B1 for $2[\times 1] - (x-3)(x-3)$ B1 for $2(x-3)$ as denominator
10(c)	$2^{2} \times a + 2 \times b - 5 = -3$ oe $3^{2} \times a + 3 \times b - 5 = 4$ oe	M2	M1 for either
	correctly equating one set of coefficients or making a or b subject of one equation	M1	FT
	correct method for eliminating one variable or correctly substituting in other equation	M1	FT
	[a=] 2 [b=] -3	B2	B1 for each
11(a)	349 or 350 or 349.4 to 349.5	4	M3 for $[0.9 \times 2.1 + 2 \times \frac{1}{2}(2.1 \times 2.1 \tan 20)] \times 100$ oe or $\frac{1}{2}(0.9 + (2 \times 2.1 \tan 20 + 0.9)) \times 2.1 \times 100$ oe or M2 for area of cross section $0.9 \times 2.1 + 2[\frac{1}{2}(2.1 \times 2.1 \tan 20)]$ oe or $\frac{1}{2}(0.9 + (2 \times 2.1 \tan 20 + 0.9)) \times 2.1$ oe or M1 for $\tan 20 = \frac{x}{2.1}$ If 0 scored SC1 for triangle marked/drawn with 20 or 70

Question	Answer	Marks	Partial Marks
11(b)	19 h 50 (or 51) min	4	B3 for 19.8 or 19.84 or M2 for $\frac{300 \times 1000}{4.2 \times 60 \times 60}$ oe or M1 for 300×1000 or $4.2 \times 60 \times 60$ or for <i>their</i> volume divided by <i>their</i> rate
12(a)	160 or 159.5	2	M1 for $\frac{1}{2} \times 16 \times 22 \times \sin 115$ oe
12(b)	84[.0] or 84.02 to 84.03	6	B3 for 32.2 or 32.21 soi OR M2 for $ \sqrt{16^2 + 22^2 - 2 \times 16 \times 22 \times \cos 115} $ or M1 for $16^2 + 22^2 - 2 \times 16 \times 22 \times \cos 115$ AND M2 for $ \frac{9 \sin 80}{their(32.21)} $ dependent on cosine rule used or M1 for $ \frac{\sin ABD}{9} = \frac{\sin 80}{their(32.21)} $

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