## Cambridge IGCSE ${ }^{\text {TM }}$



CENTRE NUMBER


## CANDIDATE

 NUMBER

## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/52
Paper 5 Investigation (Core)
May/June 2022
1 hour 10 minutes
You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.


## INFORMATION

- The total mark for this paper is 36 .
- The number of marks for each question or part question is shown in brackets [ ].

Answer all the questions.

## INVESTIGATION

## OPPOSITE CORNERS

This investigation is about the difference between the products of the numbers in the opposite corners of a square window on a grid.

To calculate the opposite difference for any window:

- multiply the numbers in the opposite corners
- subtract the smaller answer from the larger answer.

| 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 22 | 24 | 26 | 28 | 30 | 32 | 34 | 36 | 38 | 40 |
| 42 | 44 | 46 | 48 | 50 | 52 | 54 | 56 | 58 | 60 |
| 62 | 64 | 66 | 68 | 70 | 72 | 74 | 76 | 78 | 80 |
| 82 | 84 | 86 | 88 | 90 | 92 | 94 | 96 | 98 | 100 |
| 102 | 104 | 106 | 108 | 110 | 112 | 114 | 116 | 118 | 120 |
|  |  |  |  |  |  |  |  |  |  |

Consecutive even numbers fill a grid of width 10 as shown.
The grid continues downwards.
A 2 by 2 window moves on the grid.

## Example

This is the first window.


$$
\begin{array}{ll}
22 \times 4=88 \\
2 \times 24 & =48
\end{array} \quad 88-48=40
$$

The opposite difference is 40 .

1 (a) Use the grid to complete each window and find the opposite difference.

| 14 |  |
| :---: | :---: |
| 34 | 36 |



Opposite difference $=$ $\qquad$
$\qquad$

(b) What do you notice about the opposite difference for each of these windows on this grid?

2 A 3 by 3 window moves on the same grid.
(a) Complete the corner squares in the first window.

(b) Complete the opposite difference calculations for this window.
$\qquad$ .$\times 6$
$=$ $\qquad$
$2 \times$ $\qquad$

$$
=\text {. }
$$

$\qquad$
$\qquad$ - $\qquad$ $=$
(c) Complete the corner squares for each window and find the opposite difference.


3 A 4 by 4 window moves on the grid on page 2 .
(a) Complete the corner squares in the first window.

(b) Complete the opposite difference calculations for this window.
$\qquad$ .$\times 8$
$=$ $\qquad$

$$
2 \times \ldots \ldots . . . .=\ldots . . . . . .
$$

$\qquad$ - $\qquad$ $=$ $\qquad$
(c) Complete the corner squares for each window and find the opposite difference.


4 (a) Copy the opposite differences that you have found and complete the table.

| Size of window |  |  | Opposite difference |
| :---: | :---: | :---: | :---: |
| 2 by 2 | $(2-1)^{2}$ | $=1$ |  |
| 3 by 3 | $(3-1)^{2}$ | $=4$ |  |
| 4 by 4 | $(4-1)^{2}$ | $=9$ |  |
| 5 by 5 |  |  |  |
|  |  |  |  |
| $w$ by $w$ |  |  | $40($ |

(b) Find the greatest possible opposite difference for a square window on the grid on page 2.
(c) Can a square window on this grid have an opposite difference of 1400 ? Show how you decide.

5 Another grid of consecutive even numbers has width 5.
The diagram shows the start of the grid.

| 2 | 4 | 6 | 8 | 10 |
| :--- | :--- | :--- | :--- | :--- |
| 12 |  |  |  |  |
|  |  |  |  |  |

The diagram shows a 2 by 2 window on the grid.
$n$ is the first number in the window.

(a) Complete the window using expressions in terms of $n$.
(b) Use your expressions to show that the opposite difference for a 2 by 2 window is 20 .

6 A square window moves on the grid of width 5 with squares numbered $2,4,6, \ldots$. The opposite difference for this window is 180 .

Find the size of the window.

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