

Mark Scheme (Results)

June 2011

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| Question Number | Working | Answer | Mark | | Notes | |
|--------------------|--|-------------|------|----|--|-------------------------------------|
| 1. (a) | $\frac{24.1}{0.6} - 38.44 = 40.166 38.44$ | | 2 | M1 | for 0.6 or $\frac{3}{5}$ | |
| | | | | | or 40.166 (4 figures contruncated) | orrect rounded or |
| | | | | | or $40\frac{1}{6}$ or 38.44 or 38 | <u>11</u> 25 |
| | | 1.726666667 | | A1 | Accept if first 4 figures truncated) | correct (rounded or |
| | | | | | Also accept 1.726 or $\frac{259}{150}$ | $\frac{9}{5}$ or $1\frac{109}{150}$ |
| (b) | | 1.73 | 1 | B1 | ft from (a) if answer to more than 3 sf | (a) is a decimal with |
| | | | | | | Total 3 marks |
| Question | Working | Answer | Mark | | Notes | |
| Number | | | | | | (alternative method) |
| 2 . | $(5-2) \times 180 \text{ or } 3 \times 180$ | | 4 | M1 | | 360-(83+66+53+96) |
| | or $(2 \times 5 - 4) \times 90$ or 6×90 | | | | | Condone 1 |
| | or 360 + 180 | | | | | incorrect ext angle |
| | 540 | | | A1 | 540 seen scores M1A1 | 62 |
| | "540" - (97 + 114 + 127 + 84) | | | M1 | dep on first M1 | 180 - "62" |
| | | 118 | | A1 | cao | • |
| | | | | | | Total 4 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|--|-----------------|------|---|
| 3. (a) | | w(w - 9) | 2 | B2 Award B2 also for $(w \pm 0)(w - 9)$ B1 for factors which, when expanded & simplified, give two terms, one of which is correct except B0 for $(w + 3)(w - 3)$ SC B1 for $w(w - 9w)$ |
| (b) | 3x = -6 or $3x = 1 - 7$ or $5x - 2x = -6$ oe | | 3 | M2 for correct rearrangement with x terms on one side and numbers on the other AND correct collection of terms on at least one side M1 for $5x - 2x = 1 - 7$ oe ie correct rearrangement with x terms on one side and numbers on the other |
| | | -2 | | A1 cao dep on M2 |
| (c) | y ² + 3y - 7y - 21 | | 2 | M1 for 3 correct terms out of 4 or for 4 correct terms ignoring signs or for $y^2 - 4y + n$ for any nonzero value of n |
| | | $y^2 - 4y - 21$ | | A1 cao |
| | | | | Total 7 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|-----------------|--------|------|--------------------------------------|
| 4. (a) | 1 - (0.6 + 0.3) | | 2 | M1 |
| | | 0.1 | | A1 Also accept $\frac{1}{10}$ or 10% |
| (b) | 30 × 0.6 | | 2 | M1 |
| | | 18 | | A1 cao Do not accept $\frac{18}{30}$ |
| | | | | Total 4 marks |

| Question NumberWorkingAnswerMarkNotes5. $\frac{10}{12}$ and $\frac{9}{12}$ 2B2B1 for $\frac{10}{12}$ or $\frac{9}{12}$ eg $\frac{10-9}{12}$, $\frac{10}{12} - \frac{9}{12}$ Also accept $\frac{5\times2}{6\times2}$ or $\frac{3\times3}{4\times3}$ Alternative method B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ or $\frac{5\times4}{6\times4}$ and $\frac{3\times6}{4\times6}$ B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to $\frac{1}{12}$ eg $\frac{2}{24}$ SC B1 for multiplying both sides by 12 ie 10 - 9 = 1 | | 1 | | 1 | | |
|---|----------|---------|--------|------|----|---|
| Number 5. $\frac{10}{12} \text{ and } \frac{9}{12}$ $\text{eg } \frac{10-9}{12}, \frac{10}{12} - \frac{9}{12}$ $\text{Also accept } \frac{5 \times 2}{6 \times 2} \text{ or } \frac{3 \times 3}{4 \times 3}$ Alternative method B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ or $\frac{5 \times 4}{6 \times 4}$ and $\frac{3 \times 6}{6 \times 4}$ and $\frac{3 \times 6}{6 \times 4}$ B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to $\frac{1}{12}$ eg $\frac{2}{24}$ SC B1 for multiplying both sides by 12 ie 10 - 9 = 1 | Question | Working | Answer | Mark | | Notes |
| 5. $\frac{10}{12} \text{ and } \frac{9}{12}$ $\text{eg } \frac{10-9}{12}, \frac{10}{12} - \frac{9}{12}$ $\text{B2} \text{B1 for } \frac{10}{12} \text{ or } \frac{9}{12}$ $\text{Alternative method}$ $\text{B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg \frac{20}{24} and \frac{18}{24} or \frac{5\times4}{6\times4} and \frac{3\times6}{4\times6} B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to \frac{1}{12} eg \frac{2}{24} \text{SC B1 for multiplying both sides} \text{by 12 ie 10 - 9 = 1}$ | | | | | | |
| Total 2 marks | | | | 2 | B2 | Also accept $\frac{5\times 2}{6\times 2}$ or $\frac{3\times 3}{4\times 3}$ Alternative method B1 for both fractions correctly expressed as equivalent fractions with denominators that are common multiples of 6 and 4 eg $\frac{20}{24}$ and $\frac{18}{24}$ or $\frac{5\times 4}{6\times 4}$ and $\frac{3\times 6}{4\times 6}$ B1 (dep on first B1) for evaluation as a correct fraction which is equivalent to $\frac{1}{12}$ eg $\frac{2}{24}$ SC B1 for multiplying both sides by 12 ie 10 - 9 = 1 |
| Total 2 marks | | | | | | Total 2 marks |

| Question Number | Working | Answer | Mark | | Note | es |
|--------------------|------------------------------|---------------|------|----|---|---|
| 6. (a) | | Rotation | 3 | B1 | Accept 'rotate', 'rotated' etc | These marks are independent but |
| | | 90° clockwise | | B1 | Also accept quarter turn clockwise, -90° or 270° | award no marks if the answer is not a single transformation |
| | | (0, 0) | | B1 | Also accept origin, O | |
| (b) | vertices (4,4), (4,2), (5,2) | R correct | 2 | B2 | Condone omiss B1 for 2 correc | |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|---|--------|------|---|
| 7. | 3+5+7 or 15 | | 3 | M1 15 may be denominator of fraction or coefficient in an equation such as 15x = 90 |
| | 90 ÷ (3+5+7) or 90 ÷ "15" or 6 or $\frac{7}{15}$ oe | | | M1 dep |
| | | 42 | | A1 Also award for 18:30:42 |
| | | | | Total 3 marks |

| Question Number | Working | Answer | Mark | | Note | es |
|--------------------|---------|-------------------|------|----|---|------------------------|
| 8. (i) | | 3, 5, 7, 11 | 2 | B1 | cao | |
| (ii) | | 2, 3, 5, 7, 9, 11 | | B1 | cao (B0 if 3 or 5 or 7 or 11 repeated) | Brackets not necessary |
| | | | | | | Total 2 marks |

| Question Number | Working | | Answer | Mark | Notes |
|--------------------|--|--------------------------------|--------|------|--|
| 9. | eg $\frac{5}{100} \times 8000 = 400$ $\frac{5}{100} \times (8000 + "400")$ = 420 $\frac{5}{100} \times (8000 + "400" + "420")$ = 441 8000 + "400" + "420" + "441" | OR 8000 × 1.05 ³ | | 3 | $ \begin{array}{c c} M1 \text{ for eg} \\ \hline \frac{5}{100} \times 8000 \text{ or } 400 \\ \hline \hline M1 \text{ for} \\ \text{completing} \\ \text{method} \\ \end{array} \begin{array}{c} OR \\ M2 \text{ for} \\ 8000 \times 1.05^3 \\ (M1 \text{ for} \\ 8000 \times 1.05 \\ \text{or } 8400 \\ \text{or} \\ 8000 \times 1.05^2 \\ \text{or} \\ 8000 \times 1.05^4) \\ \hline \end{array} $ |
| | | | | | Accept (1 + 0.05) as equivalent to 1.05 throughout. |
| | | | | | SC If no other marks gained, award M1 for 8000×1.15 oe or 9200 |
| | | | 9261 | | A1 Cao |
| | | | | | Total 3 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|---------|-------------------------|------|--|
| 10. | | $C = \frac{3d+7}{2}$ oe | 3 | B3 B2 for $\frac{3d+7}{2}$ oe B2 for $C = 3d+7 \div 2$ oe B1 for $3d+7 \div 2$ B1 for $C = 1$ linear expression in $C = 1$ |
| | | | | Total 3 marks |

| Question Number | Working | Answer | Mark | | Notes |
|--------------------|---|---------------------------------------|------|----|---|
| 11. (a) | 1 × 8 + 3 × 14 + 5 × 26 + 7 × 17 + 9 × 10 + 11 × 5 or 8 + 42 + 130 + 119 + 90 + 55 | | 3 | M1 | for finding at least four products $f \times x$ consistently within intervals (inc end points) and summing them |
| | | | | M1 | (dep) for use of halfway values |
| | | 444 | | A1 | Cao |
| (b) | | 8 22 48 65 75 80 | 1 | B1 | Cao |
| (c) | | Points correct | 2 | B1 | $\pm \frac{1}{2}$ sq ft from sensible table |
| | | Curve or line segments | | B1 | ft from points if 4 or 5 correct or if points are plotted consistently within each interval at the correct heights Accept curve which is not joined to the origin |
| (d) | 5.2 indicated on cf graph | | 2 | M1 | for 5.2 indicated on cf graph |
| | | approx 36-40 from correct graph | | A1 | If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve & if answer is correct (± ½ sq tolerance), award M1 A1 |
| | | | | | Total 8 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|--|--------|------|--|
| 12. (a) | $\frac{BC}{5.2} = \frac{9}{6} \text{ oe}$ | | 2 | M1 for correct, relevant proportionality statement with 3 values substituted |
| | | 7.8 | | A1 cao |
| (b) | $\frac{CE}{7.2} = \frac{6}{9}$ oe or $\frac{CE}{6} = \frac{7.2}{9}$ oe or $\frac{CE}{7.2} = \frac{5.2}{"7.8"}$ oe or $\frac{CE}{5.2} = \frac{7.2}{"7.8"}$ oe | | 2 | M1 for correct, relevant proportionality statement with 3 values substituted |
| | | 4.8 | | A1 cao |
| | | | | Total 4 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|---|--------|------|---|
| 13. | $\frac{20(2x-1)}{4} + \frac{20(x-1)}{5} = 2 \times 20$ or $5(2x-1) + 4(x-1) = 40$ or $\frac{5(2x-1) + 4(x-1)}{20} = 2$ or $\frac{5(2x-1)}{20} + \frac{4(x-1)}{20} = 2$ $10x - 5 + 4x - 4 = 40$ or $\frac{10x - 5 + 4x - 4}{20} = 2$ | | 4 | M1 for clear intention to multiply both sides by 20 or a multiple of 20 or to express LHS as a single fraction with a denominator of 20 or a multiple of 20 or to express LHS as the sum of two fractions with denominators of 20 or a multiple of 20 May be implied by first B1 B1 expanding brackets (dep on M1) |
| | or $\frac{10x-5}{20} + \frac{4x-4}{20} = 2$ | | | |
| | 14x = 49 or 14x - 9 = 40 | | | B1 dep on both preceding marks |
| | or $10x + 4x - 9 = 40$ or $14x - 49 = 0$ | | | ie for a correct rearrangement of a correct equation |
| | | 3.5 | | A1 dep on all preceding marks |
| | | | | Total 4 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|-----------|--------|------|---------------|
| 14. | 1.75 seen | | 2 | M1 |
| | | 8 | | A1 |
| | | | | Total 2 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|--|-------------------------|------|--|
| 15. (a) | Splits shape into rectangle & semicircle | | 4 | M1 May be implied by working |
| | $\frac{\pi \times 2.7^2}{2}$ or value rounding to 11.4 or 11.5 | | | M1 $\pi \to 11.451105$ $3.14 \to 11.4453$ $3.142 \to 11.45259$ Also award for equivalent multiple of π eg 3.645π, $\frac{729\pi}{200}$ |
| | 2 × 2.7 × 7.1 or 38.34 | | | M1 Also accept 38.3 |
| | | 49.8 | | A1 for 49.8 or for answer rounding to 49.78 or 49.79 |
| (b) | $P-2L=\pi r+2r$ oe | | 3 | M1 for rearranging with both r terms on one side |
| | $P - 2L = (\pi + 2)r$ oe | | | M1 for factorising a correct expression (does not depend on a correct rearrangement) |
| | | $\frac{P-2L}{\pi+2}$ oe | | A1 |
| | | | | Total 7 marks |

| Question Number | | Working | Answer | Mark | | Notes |
|--------------------|-----|---|--------|------|----|--|
| 16. (a)(| i) | | 114 | 2 | B1 | cao |
| | ii) | eg angle at the centre = 2 × angle at circumference | | | B1 | Three key points must be mentioned 1. Angle at centre/middle/ O /origin 2. Twice, double, $2 \times$ or half/ $\frac{1}{2}$ as appropriate 3. angle at circumference/edge/perimeter (NOT e.g. angle D , angle ADB , angle at top, angle at outside) |
| (b) | · | | 74 | 1 | B1 | cao |
| | | | | | | Total 3 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|--|-------------------------------------|------|---|
| 17. (i) | $\frac{1}{7} \times \frac{2}{6}$ and no other terms | | 2 | M1 |
| | | $\frac{2}{42}$ or $\frac{1}{21}$ oe | | A1 Also accept 0.05, 0.04, 0.047, 0.048 etc Sample space method - award 2 marks for a correct answer; otherwise no marks |
| (ii) | $\frac{1}{7} \times \frac{1}{6}$ or $\frac{2}{7} \times \frac{3}{6}$ | | 3 | M1 SC M1 for $\frac{1}{7} \times \frac{1}{7}$ or $\frac{2}{7} \times \frac{3}{7}$ |
| | $\frac{1}{7} \times \frac{1}{6} + \frac{2}{7} \times \frac{3}{6}$ | | | M1 for $\frac{1}{7} \times \frac{1}{7} + \frac{2}{7} \times \frac{3}{7}$ |
| | | $\frac{7}{42}$ or $\frac{1}{6}$ oe | | Also accept 0.16, 0.16, 0.17, 0.166, 0.167 etc but not 0.2 Sample space method - award 3 marks for a correct answer; otherwise no marks |
| | | | | Total 5 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|---|--------|------|--|
| 18. | (BC =) 47 sin 32° | | 5 | or for $(CD =) \frac{47 \sin 32^{\circ}}{\sin 129^{\circ}}$ |
| | 24.906 at least 3 sf (may be implied by correct <i>BD</i>) | | | A1 or for CD = 32.048 at least 2 sf (may be implied by correct BD) |
| | $\tan 51^\circ = \frac{"24.906"}{BD}$ or | | | M1 or for $\cos 51^{\circ} = \frac{BD}{"32.048"}$ |
| | $\tan 39^\circ = \frac{BD}{"24.906"}$ | | | |
| | $(BD =) \frac{"24.906"}{\tan 51^{\circ}}$ or "24.906" $\tan 39^{\circ}$ | | | M1 or for $(BD =)$ "32.048"cos51° |
| | | 20.2 | | A1 for answer rounding to 20.2 (20.1686) |
| | | | | Total 5 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|------------------------|-------------------|------|---|
| 19. (a) | $P = kQ^3$ | | 3 | M1 for $P = kQ^3$ but not for $P = Q^3$ |
| | $1350 = k \times 3375$ | | | M1 for $1350 = k \times 3375$ |
| | | | | Also award for $1350 = k \times 15^3$ |
| | | $P = 0.4Q^{3}$ oe | | A1 $P = 0.4Q^3$ oe |
| | | | | Award 3 marks if answer is |
| | | | | $P = kQ^3$ oe but k is evaluated as |
| | | | | 0.4 in part (a) or part (b) |
| (b) | | 3200 | 1 | B1 ft from "0.4" × 8000 except for |
| | | | | k = 1, if at least M1 scored in (a) |
| | | | | (at least 1 d.p. accuracy in |
| | | | | follow through) |
| | | | | Total 4 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|----------------------|-----------------------------------|------|--|
| 20. | $a^2 \times 10^{2n}$ | | 3 | M1 |
| | | $\frac{a^2}{10} \times 10^{2n+1}$ | | A1 for $\frac{a^2}{10}$ oe A1 for $\times 10^{2n+1}$ oe $\times 10^{2n+1}$ oe $\times \frac{a^2}{10} \times 10^{2n+1}$ even if M1 not awarded. Award M1 A1 A0 if $\frac{a^2}{10}$ oe seen. Award M1 A0 A1 if $\times 10^{2n+1}$ oe seen. |
| | | | | Total 3 marks |

| Question Number | Working | Answer | Mark | | Notes |
|--------------------|---|----------------|------|----|---|
| 21. (a) | Use of areas to obtain a correct expression for <i>A</i> , which must be correctly punctuated. For example $ (A =) 80 - 2 \times \frac{1}{2} x (10 - x) - 2 \times \frac{1}{2} x (8 - x) $ or $ 10 \times 8 - \frac{1}{2} x (10 - x) - \frac{1}{2} x (10 - x) - \frac{1}{2} x (8 - x) - \frac{1}{2} x (8 - x) $ or $ 80 - x (10 - x) - x (8 - x) $ or $ 80 - 2 \left(\frac{10x - x^2}{2} \right) - 2 \left(\frac{8x - x^2}{2} \right) $ | | 3 | B2 | B1 for expression for area of triangle or pair of congruent triangles, for example $\frac{1}{2}x(10-x) \text{ or } \frac{1}{2}x(8-x)$ or $x(10-x)$ or $x(8-x)$ Condone omission of brackets for award of B1 |
| | Correct simplification of a correct expression for A to obtain an expression which is equivalent to $2x^2 - 18x + 80$ For example $(A =) 80 - 10x + x^2 - 8x + x^2$ or $80 - (10x - x^2) - (8x - x^2)$ or $80 - (5x - \frac{1}{2}x^2) - (5x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2) - (4x - \frac{1}{2}x^2)$ | | | B1 | dep on B2 |
| (b)(i) | | 4 <i>x</i> –18 | 5 | B2 | B1 for 2 of 3 terms differentiated correctly |
| (ii) | " $4x - 18$ " = 0 | | | M1 | |
| | | 4.5 oe | | A1 | cao |
| (iii) | eg positive coefficient of x^2 or U shape or $\frac{d^2 A}{dx^2} = 4$ which > 0 | | | B1 | |
| | | | | | Total 8 marks |

| Question Number | Working | Answer | Mark | Notes |
|--------------------|--|---|------|---|
| 22. | $x^2 + (2x - 3)^2 = 2$ | | 6 | M1 for correct substitution |
| | $x^2 + 4x^2 - 6x - 6x + 9 = 2$ or $x^2 + 4x^2 - 12x + 9 = 2$ | | | B1 (indep) for correct expansion of $(2x-3)^2$ even if unsimplified |
| | $5x^2 - 12x + 7(=0)$ | | | B1 for correct simplification Condone omission of '= 0' |
| | or $\frac{12 \pm \sqrt{4}}{10}$ or $\frac{12}{10} \pm \frac{\sqrt{4}}{10}$ | | | B1 for correct factorisation or for correct substitution into quadratic formula and correct evaluation of 'b² – 4ac' |
| | or $\frac{6}{5} \pm \frac{1}{5}$ | | | or for using square completion correctly as far as indicated |
| | $x = 1$ or $x = 1\frac{2}{5}$ | | | A1 for both values of x dep on all preceding marks |
| | | x = 1, y = -1 $x = 1\frac{2}{5}, y = -\frac{1}{5}$ | | A1 for complete, correct solutions (need not be paired) dep on all preceding marks No marks for $x = 1$, $y = -1$ with no working |
| | | | | Total 6 marks |

| O ti | NA/ = valueius = | A | NA =I - | Maka a |
|----------|---|------------------|---------|--|
| Question | Working | Answer | Mark | Notes |
| Number | | | | |
| 23. | $\frac{2\pi r^2 + 2\pi rh}{4\pi r^2} = 2$ | | 5 | Also award for $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$ |
| | $\frac{2}{1}$ = 2 | | | Also award for $\frac{2}{2} = 2$ |
| | 4πr² | | | |
| | $2\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe | | | M1 for $2\pi r^2 + 2\pi rh = 2 \times 4\pi r^2$ oe |
| | | | | $2\pi r(r+h)$ |
| | | | | or $\frac{2\pi r(r+h)}{4\pi r^2}=2$ |
| | | | | |
| | | | | If first M1 awarded for |
| | | | | $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2$ award this |
| | | | | $\frac{3}{2} = 2$ award this |
| | | | | |
| | | | | second M1 also for |
| | | | | $\pi r^2 + 2\pi r h = 2 \times 4\pi r^2$ oe |
| | h = 3r oe | | | A1 If first M1 awarded for |
| | | | | $\pi r^2 + 2\pi rh$ |
| | | | | $\frac{\pi r^2 + 2\pi rh}{4\pi r^2} = 2 \text{ and second M1}$ |
| | | | | $4\pi r^2$ |
| | | | | for $\pi r^2 + 2\pi r h = 2 \times 4\pi r^2$ oe |
| | | | | Award this A1 also for $h = 3.5r$ oe |
| | 2 | | | |
| | $\pi r^2 \times "3r"$ | | | M1 dep on first two M1s |
| | oe | | | h must be of the form kr |
| | $\frac{3}{3}\pi \Gamma^{2}$ | | | |
| | | $\frac{9}{4}$ oe | | A1 |
| | | 4 | | Total 5 marks |
| | | | | Total Jillaiks |

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