

Mark Scheme (Results)

January 2017

International GCSE Mathematics A 4MAO/4HR



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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
   Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

# Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

#### Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o eeoo each error or omission

### No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

# With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

# Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

## Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another. **International GCSE Maths:** Apart from Questions 8, 18 and 21, where the mark scheme states otherwise, the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Q	Working	Answer	Mark	Notes
1 (a)	e.g. $\frac{100}{24} \times 30$		2	M1 For $\frac{100}{24}$ (=4.16(66)) or $\frac{30}{24}$ or 1.25 or $\frac{24}{100} = \frac{30}{x}$ oe
		125		A1
(b)	e.g. $\frac{850}{300} \times 24$ or $850 \div \frac{300}{24}$ oe		2	M1 Complete method to find number made
		68		A1 cao
				Total 4 marks

2	(a)	0.15 + 0.4	0.55	1	B1
	(b)	$\frac{1-(0.15+0.4)}{3}$ or $\frac{0.45}{3}$ (= 0.15)		2	M1
		${3}$ or ${3}$ (= 0.15)			
			0.3		A1
	(c)	$160 \times 0.4$		2	M1
			64		A1
					Total 5 marks

1200 – "420"	780	M1	dep SC M	1 for 1620
1200 - 420	780	A1		1 for 1620
	760	AI	SC W	Total 3 marks

4	$30 \times 20 \text{ or } 600$		4	M1 For area of rectangle
	$\pi \times 8^2$ or 201.(0619298) or $64\pi$			M1 Indep for area of circle eg $\pi \times 8^2$ or 201.(0619298) or $64\pi$
	$30 \times 20 - \pi \times 8^2$			M1
		399		A1 Accept 398 -399.1
				Total 4 mark

5 (a)(i)	{3, 5, 7}	2	B1
(a)(ii)	{1, 2, 3, 5, 7, 9}		B1
(b)	6	1	B1
			Total 3 marks

6	12.8 <sup>2</sup> – 9.7 <sup>2</sup> or 163.84 – 94.09 or 69.75		3	M1	For squaring and subtracting
					$[a = \cos^{-1}\left(\frac{9.7}{12.8}\right) (= 40.7)$ and
					$\sin 40.7 = \frac{x}{12.8} \text{ or } \tan 40.7 = \frac{x}{9.7}$
	$\sqrt{12.8^2-9.7^2}$			M1dep	For square root
	V12.0 9.7				[ $x = 12.8 \sin 40.7or \ x = 9.7 \tan 40.7$ ]
		8.35		A1	Allow 8.35 - 8.352
					Total 3 marks

7	(a)		12p + 15	1	B1
	(b)		2(3r+7)	1	B1
	(c)	$(-5)^2 - 3 \times -5$ oe			M1 or +25 or +15
			40	2	A1
	(d)	$\frac{w^{13}}{w^4} \text{ or } w \times w^8 \text{ or } w^5 \times w^4$		2	M1 For $\frac{w^{13}}{w^4}$ or $w \times w^8$ or $w^5 \times w^4$
			$w^9$		A1
	(e)			2	M1 For $x \ge 3$ or $x < 9$ or $3 < x \le 9$
			$3 \le x < 9$		A1 Accept [3, 9) or $9 > x \ge 3$
					Total 8 marks

8	160 - 3x + 7x - 20 = 180  or		3	M1	For a correct equation
	2(160 - 3x) + 2(7x - 20) = 360  oe				
	4 100 140 2 7 100 20 160			3.61	
	e.g. $4x = 180 - 140$ or $-3x + 7x = 180 + 20 - 160$			M1	For isolating the terms in <i>x</i> in a
	or $4x = 40$ or $14x - 6x = 360 - 320 + 40$ oe				correct equation
		10		A1	Dep on at least M1
		_			Total 3 marks

<b>9</b> (a)	$\cos x = \frac{60}{110}  \text{or } \cos x = 0.545(4545)$		3	M1
	$(x=)\cos^{-1}\left(\frac{60}{110}\right)$			M1
		56.9		A1 56.9 – 57
(b)	90 – 56.9(4426885) oe	033	2	M1ft for complete method, ft from (a) if $"(a)" < 90, 90 - \text{their } x$ A1ft accept (0)33 - (0)33.1 or ft
(c)(i)		105	2	B1
(c)(ii)		115		B1 Accept 114.9
				Total 7 marks

<b>10</b> (a)		2	M1 = 20 = b
	111275		M1 For $3^a \times 5^b \times 11$ with $a = 4$ or $b = 3$
	111375		A1 A
(1.)		2	A1 Accept $3^4 \times 5^3 \times 11$ oe
(b)		2	M1 For $3^4 \times 5^q$ or $3^p \times 5^2$ (and no 11) or $n \times 3^3 \times 5^2$ where $n \neq 11$
	2025		A1 Accept $3^4 \times 5^2$ oe
			Total 4 marks

11		2	M1 For $y = -2x + c \ (c \neq 1)$ or
			y = mx + 1
			or for a correct method to find the
			gradient
			or $m = -2$ and $c = 1$ stated
			or $-2x + 1$ or $L = -2x + 1$
	y = -2x + 1		A1
			oe
			Total 2 marks

12	(a)			2	B1	For 0.4 on LH branch
			Correct probabilities		B1	For 0.3, 0.7 and 0.3 on RH branches
	(b)			2	M1	For $0.6 \times 0.7$
			0.42		A1	oe
	(c)	$0.6 \times "0.3" \times "0.8" + "0.4" \times 0.7 \times "0.8" + "0.4" \times$		3	M2ft	For a complete method
		$"0.3" \times 0.2 \ (= 0.144 + 0.224 + 0.024) \ \text{oe}$				M1ft for $0.6 \times "0.3" \times "0.8"$ or $0.144$
						$\left(\frac{18}{125}\right)$ or "0.4" × 0.7 × "0.8" or 0.224
						$\left(\frac{28}{125}\right)$ or "0.4" × "0.3" × 0.2 or 0.024
						$\left(\frac{3}{125}\right)$
			0.392			49
					A1cao	$\frac{15}{125}$ oe
		Alternative method				
		$1 - [(0.6 \times 0.7 \times 0.2) + (0.4 \times 0.3 \times 0.8) +$			M2ft	For complete method
		$(0.6 \times 0.7 \times 0.8) + (0.6 \times 0.3 \times 0.2) +$				M1ft for 1 – (at least 2 correct
		$(0.4 \times 0.7 \times 0.2)]$				products).
			0.392		A1cao	49
						125
						Total 7 marks

13 (a)	$P = \frac{k}{q^2}$ $12.8 = \frac{k}{2^2} \text{ oe or } k = 12.8 \times 2^2 \text{ or } k = 51.2$		3	M1 Allow $Pq^2 = k$ or $q^2 = \frac{k}{p}$ Do not allow $P = \frac{1}{q^2}$ M1 For correct substitution in a correct equation. Implies first M1  Award M2 if $k = 51.2$ stated unambiguously
		$p = \frac{51.2}{q^2}$		A1 Award 3 marks if answer is $P = \frac{k}{q^2} \text{ but } k \text{ is evaluated in (a) or (b)}$ $SCB2 \text{ for } Pq^2 = 51.2 \text{ or } q^2 = \frac{51.2}{p}$
(b)	$\frac{51.2}{8^2}$	0.8	1	B1ft ft equation in the form $P = \frac{k}{q^2}$ oe
				Total 4 marks

14 (a)	e.g. $\frac{8}{5}$ or 1.6 or $\frac{5}{8}$ or 0.625 or e.g. $4 \times \frac{8}{5}$ or $4 \div \frac{5}{8}$ oe or e.g. $\frac{AZ}{4} = \frac{8}{5}$ or $\frac{AZ}{8} = \frac{4}{5}$ oe		2	M1	For correct scale factor or correct expression for AZ or for a correct equation involving AZ oe
		6.4		A1	oe e.g. $\frac{32}{5}$
(b)	Fo. 6 . 8 or 6 . 5 or 6 × 4		2	M1	Correct expression for BC
	Eg $6 \div \frac{8}{5}$ or $6 \times \frac{5}{8}$ or $\frac{6 \times 4}{"6.4"}$ oe	3.75		A1	oe
(c)	$52.48 - \frac{52.48}{1.6^2}$		3	M2	For a fully correct method or
	$32.40 - \frac{1.6^2}{1.6^2}$				M1 for $\frac{52.48}{1.6^2}$ or 20.5
		31.98		A1	Accept 32.0 or 32
					Total 7 marks

15	(a)				M1 For $(y \pm 8)(y \pm 6)$
			(y - 8)(y + 6)	2	A1 cao
	(b)	$4 = 5(e - 3)$ or $4 = 5e - 15$ or $\frac{4}{5} = e - 3$			M1
					A1
			$\frac{19}{5}$	2	$3\frac{4}{5}$ or 3.8
	(c)	$\frac{3(x-1)-2(x+1)}{(x+1)(x-1)} \text{ or } \frac{3(x-1)}{(x+1)(x-1)} - \frac{2(x+1)}{(x+1)(x-1)}$		3	M1 oe e.g. $\frac{3(x-1)-2(x+1)}{x^2-1}$
		$\frac{3x-3-2x-2}{(x+1)(x-1)}$ oe			M1
			$\frac{x-5}{(x+1)(x-1)}$		A1 oe e.g. $\frac{x-5}{x^2-1}$
					Total 7 marks

10	<b>6</b> (a)	$\frac{10}{2.72 - 2.47}$ or 40		2	M1 Or bar of height 40 wrong width
			Correct bar		A1
	(b)		5	1	B1
					Total 3 marks

<b>17</b> (a)	$0.5 \times (360 - 260) \text{ or } 0.5 \times 100$			M1 For a complete method
		50	2	A1
(b)	e.g. 360 - ("50" + 260 + 30) (= 20), 90 - "20"		2	M1ft For a complete method.
	or $\frac{180-100}{2} + 30$			
		70		A1
				Total 4 marks

<b>18</b> (a)		_	M1 Line $y = -5$ drawn or clear attempt
	-3.4	2	A1 to take reading at $y = -5$ Accept $-3.35$ to $-3.45$ inclusive
			A1 Accept -3.35 to -3.45 inclusive
(b)		3	M2 $y = -5x$ drawn.
			M1 for $x^3 - 0.2x^2 - 9x + 7 = -5x$ or
			y = -5x oe
	-2.5		A1 dep on at least M1 (-2.452.55)
	-2.3		Total 5 marks

19	$(\pi \times 5^2) + \pi \times 5 \times l$ $(25\pi) + 5\pi l$		5	M1	For a correct expression for total surface area
	( <i>l</i> =) 13			A1	For the correct slant height
	$(h=) \sqrt{13^2-5^2} \text{ or } \sqrt{144} \text{ or } 12$			M1	For the correct method to find <i>h</i> ft if first M1 scored
	$(V =) \frac{1}{3} \times \pi \times 5^2 \times 12 (= 314 - 314.3)$			M1	For the correct method to find <i>V</i> ft if first M1 scored
		$100\pi$		A1	
					Total 5 marks

<b>20</b> (a)	$6\sqrt{c} - 9 + 2c - 3\sqrt{c} \text{ or } 3\sqrt{c} - 9 + 2c$		3	M1 Accept $\sqrt{c}\sqrt{c}$ or $(\sqrt{c})^2$ instead of $c$
		<i>c</i> = 5		A1
		k = 3		B1
(b)	$\frac{1}{2}$ or $p^{m+1+\frac{2}{3}} = 1$		3	M1
	$\frac{2}{2}$ or $p = 3 = 1$			
	$\frac{1}{p \times p^{\frac{2}{3}}} \text{ or } p^{\frac{m+1+3}{3}} = 1$			
	$\frac{1}{\frac{5}{p^{\frac{5}{3}}}} or \ p^{\frac{-5}{3}} or \ m+1+\frac{2}{3}=0$			M1
	$\frac{1}{5}$ or $p^{3}$ or $m+1+\frac{2}{2}=0$			
	$p^{\overline{3}}$			
		5		A1 <u>-5</u>
		$-\frac{1}{3}$		$\begin{array}{cc} A1 & \frac{-5}{3} \\  & p^{\frac{-5}{3}} \text{ gains M2 only} \end{array}$
				Total 6 marks

21	(a)		3x - 13 - 50	1	B1	or $3x - 13 - 25 - 25$
	(b)	x - 52		5	B1	or $x-2-25\times 2$
		$25(3x - 63)(x - 52) \ (= 81900)$			M1	For a correct expression for volume of box
		eg $3x^2 - 156x - 63x + 3276 (= 3276)$			M1	For brackets correctly expanded
		or $75x^2 - 3900x - 1575x + 81900 (= 81900)$				
		eg $3x^2 - 219x = 0$ or $3x(x - 73) = 0$ or $75x^2 - 5475x = 0$			M1	For correctly reducing to 2 term quadratic equation
		(x = 0) or $x = 73$	73		A1	For $x = 73$ NB: A1 dependent on at least 2 method marks
						Total 6 marks

